

# Fission and the Origin of Heavy Elements in the Universe






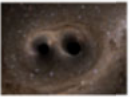
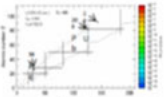
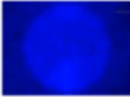
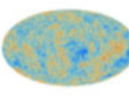
Taka KAJINO

Beihang University, China

The University of Tokyo, National Astronomical Observatory of Japan

**New Frontier Field — Cosmo-Nuclear Physics**

Universe is the Laboratory for Four Fundamental Interactions.

GW Gravity	Atomic Nuclei Strong Nuclear Force	$\nu$ Weak Force	Opt.-IR-X- $\gamma$ Electromagnetism	
 Kip Thorne Nobel Prize 2017	 Akira Hara Nobel Prize 1987	 Akira Hara Bonner Prize 1993	 Masahito Koshiro Nobel Prize 2002	 George Smoot Nobel Prize 2006
				
Astronomy & Astrophysics (Inductive) Finding the principle behind the phenomena.		Nuclear Physics (Deductive) Deriving the phenomenon from the principle.		

*Universe is the Laboratory for Fundamental Physics*

Taka ...

Astrophysics and cosmology is a field  
which requires imagination.

**Be brave enough to propose even crazy ideas.**

**Let's discuss together !**

**Because we are the collaborators !**

**William A. Fowler in 1987**

# Purpose

## To elucidate the roles of Fission & $\nu$ s in Explosive Nucleosynthesis

2. Roles of  $\nu$ s in conjugate  $\nu$ - &  $\nu p$ -process  
-  $\nu$  flavor oscillation and mass hierarchy

$\nu$ -process

$\nu p$ -process

s - process

(Pb) 82

1. Roles of Fission in r-process

- Supernova, Collapsar & Neutron-Star Merger ?

Go beyond

Origin of Elements in Stars  
B2FH 1957



Margaret & Geoffrey Burbidge,  
William A. Fowler and Fred Hoyle  
(1957)

n) 50

82

50

e - captur

stellar fusion

CNO - cycle

Neutrons

The 11 Greatest Unanswered Questions in Physics !



- What is the origin of Uranium ?
- Why do neutrinos have mass ?

The National Research Council's Board on Physics, USA (2002)



# GW170817/SSS17a

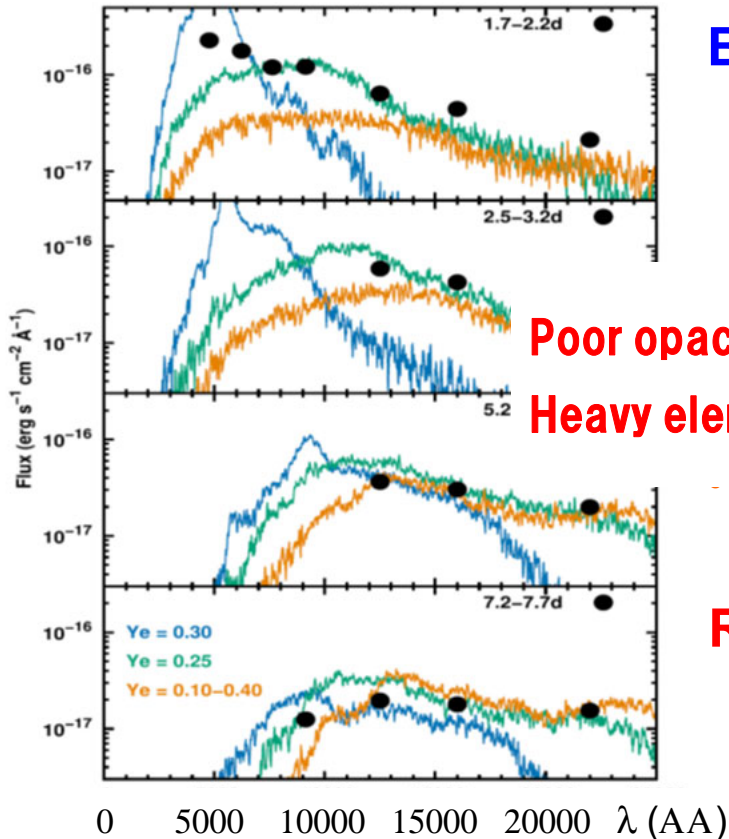
Abbott et al. (LIGO-Virgo), PRL 119, 16101 (2017)



GW170817/SSS17a

1. GW170817 (LIGO-Virgo) :  $0.86 < M/M_{\odot} < 2.26 \rightarrow$  EoS
2. GRB170817A (Fermi-GBM) : 1.7 s  $\rightarrow$  Central Engine
3. No  $\nu$ -Signal: 10
4. X-rays & Radio
5. Optical and Near-IR

**Caution!**  
**Today's astronomers' consensus:**  
**No clear evidence for**  
**Lanthanoid in Neutron-Star-Merger !**



Blue



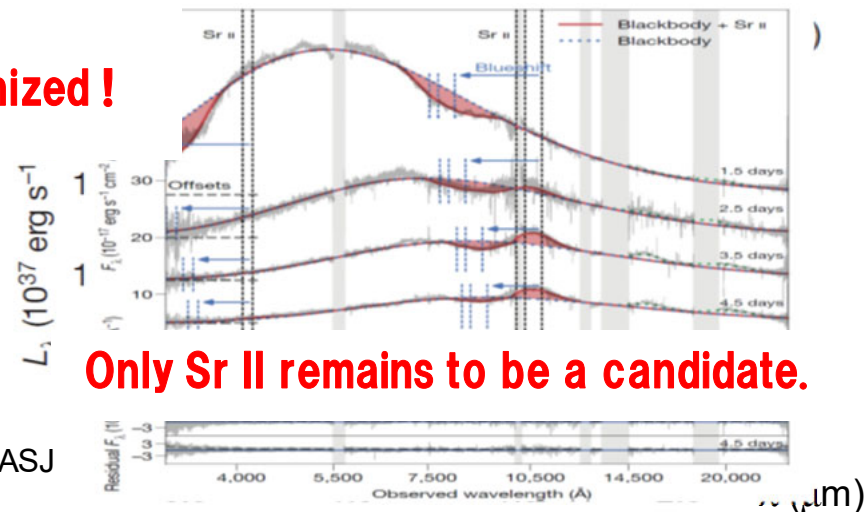
Red

**Poor opacity table !**  
**Heavy elements are ionized !**

- ◆ Color change over one week seems consistent with radioactive decay of r-elements. (Probably Lanthanoids)
- ◆ Many neutral lines of heavy elements.

Watson et al., Nature 574 (2019), 497

~~Smartt et al. Nature, 551, 75 (2017)~~



**Only Sr II remains to be a candidate.**

Tanaka et al. PASJ 00, 1-7 (2017)

# Cosmic Evolution & Origin of Heavy Elements

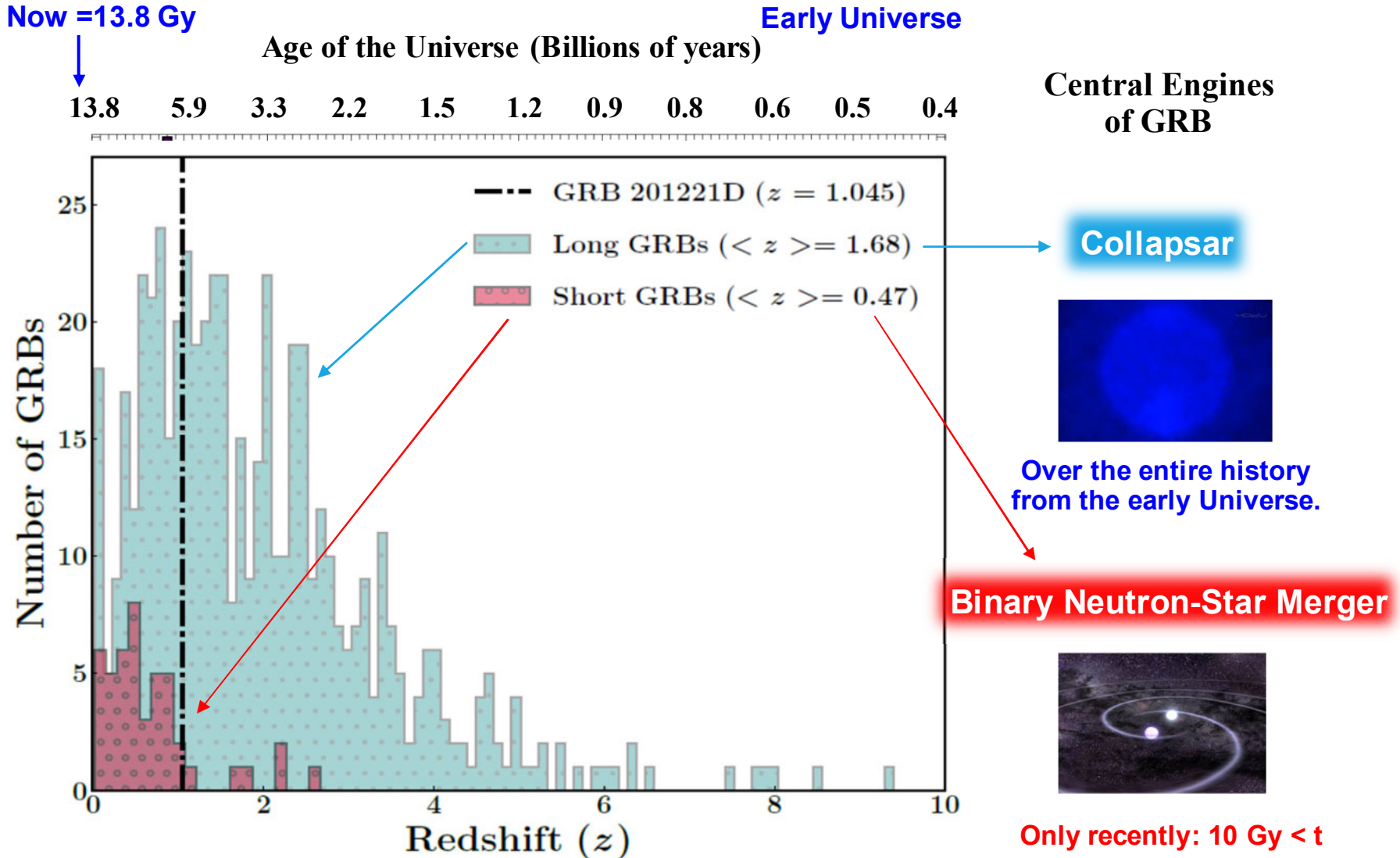
Multi-messenger Era with GW,  $\gamma$ ,  $\nu$ , Nuclei

Gravity, EM, Weak, Strong — 4 fundamental forces



# Redshift – Age relation of Gamma-Ray Bursts

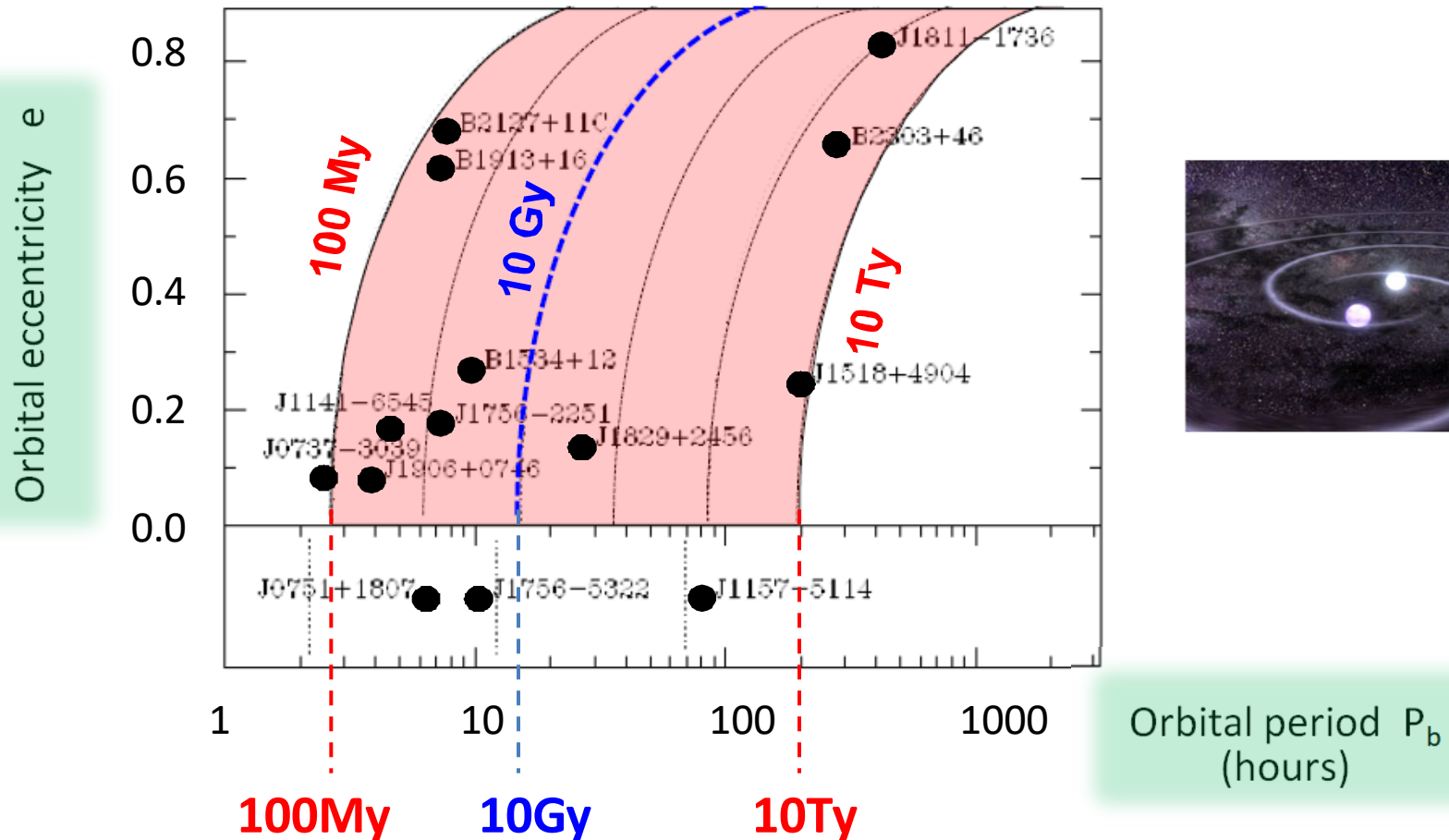
Dimple, et al., MNRAS (2022) 516, Issue 1, pp.1-12



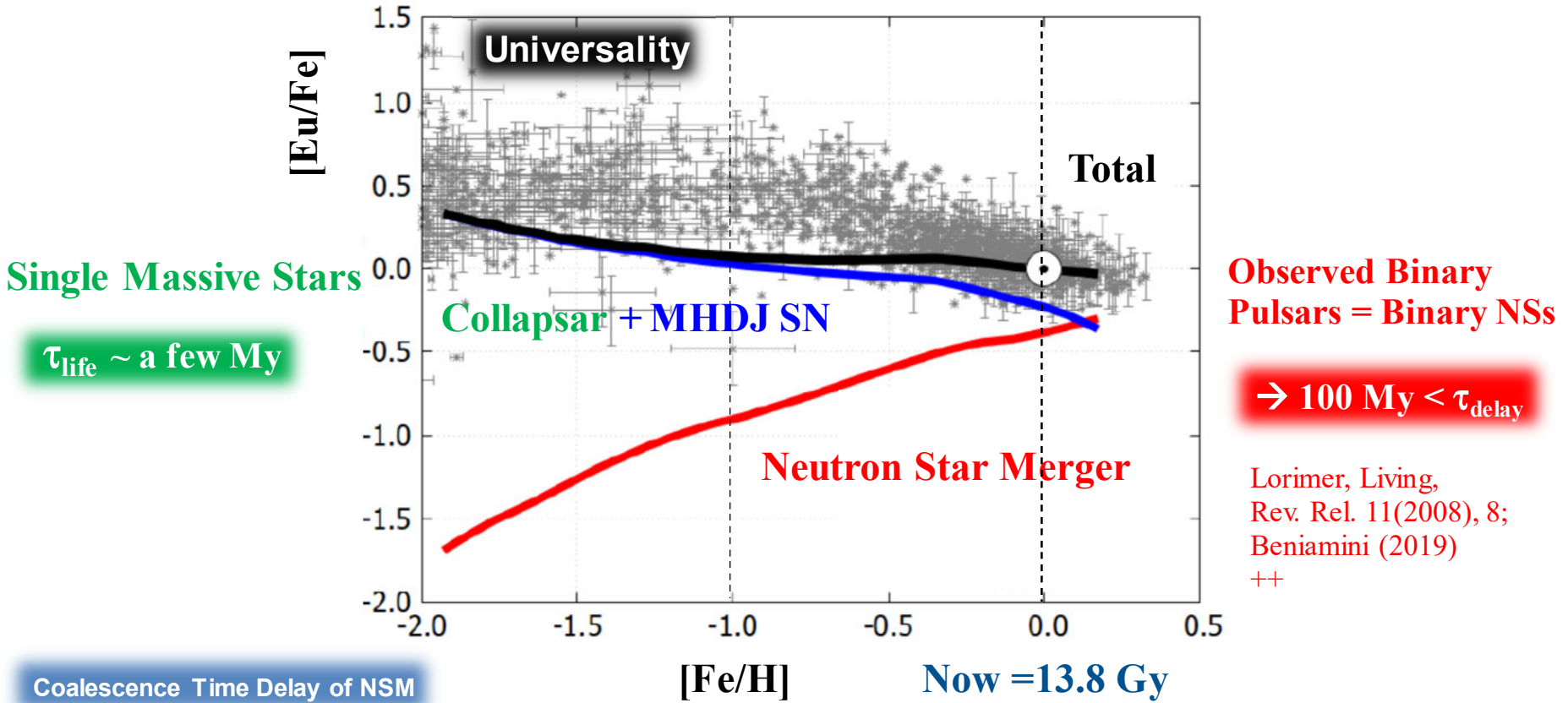
# Binary Pulsars : Merger Time-Delay

**General Relativity :**  $\tau_{\text{delay}} = 9.83 \text{ Myr} \times \left(\frac{P_b}{\text{hr}}\right)^{8/3} \times \left(\frac{m_1 + m_2}{M_\odot}\right)^{-2/3} \left(\frac{\mu}{M_\odot}\right)^{-1} (1 - e^2)^{7/2}$

**14 BINARY PULSARS :** Lorimer, Living Rev. Rel. 11(2008), 8; Beniamini+ (2019).



Kim, Kim, He, Choi, Luo, Kajino, Tanihata, Diehl, ApJ 998 (2026), 253; He, Kajino, et al., ApJ Lett 966 (2024), L34; Yamazaki, He, Kajino, et al., ApJ 933 (2022), 112; Kobayashi, Karakas & Lugaro, ApJ 900 (2020), 179.



$t / 10\text{Gy} = 10^{[\text{Fe}/\text{H}]}$   $\longleftrightarrow$   $[\text{Fe}/\text{H}] = \log(N_{\text{Fe}}/N_{\text{H}}) - \log(N_{\text{Fe}}/N_{\text{H}})_{\odot}$

Sneden, Cowan, Gallino, ARAA 46 (2008) 241.

HST-obs: Roederer et al., ApJ 747 (2012) L8.

$$\frac{t}{10^{10} \text{y}} \doteq 10^{[\text{Fe}/\text{H}]}$$

$$\log \frac{\text{Fe}/\text{H}_{\star}}{\text{Fe}/\text{H}_{\odot}} \quad 7$$

||  
[Fe/H]

— 3.1

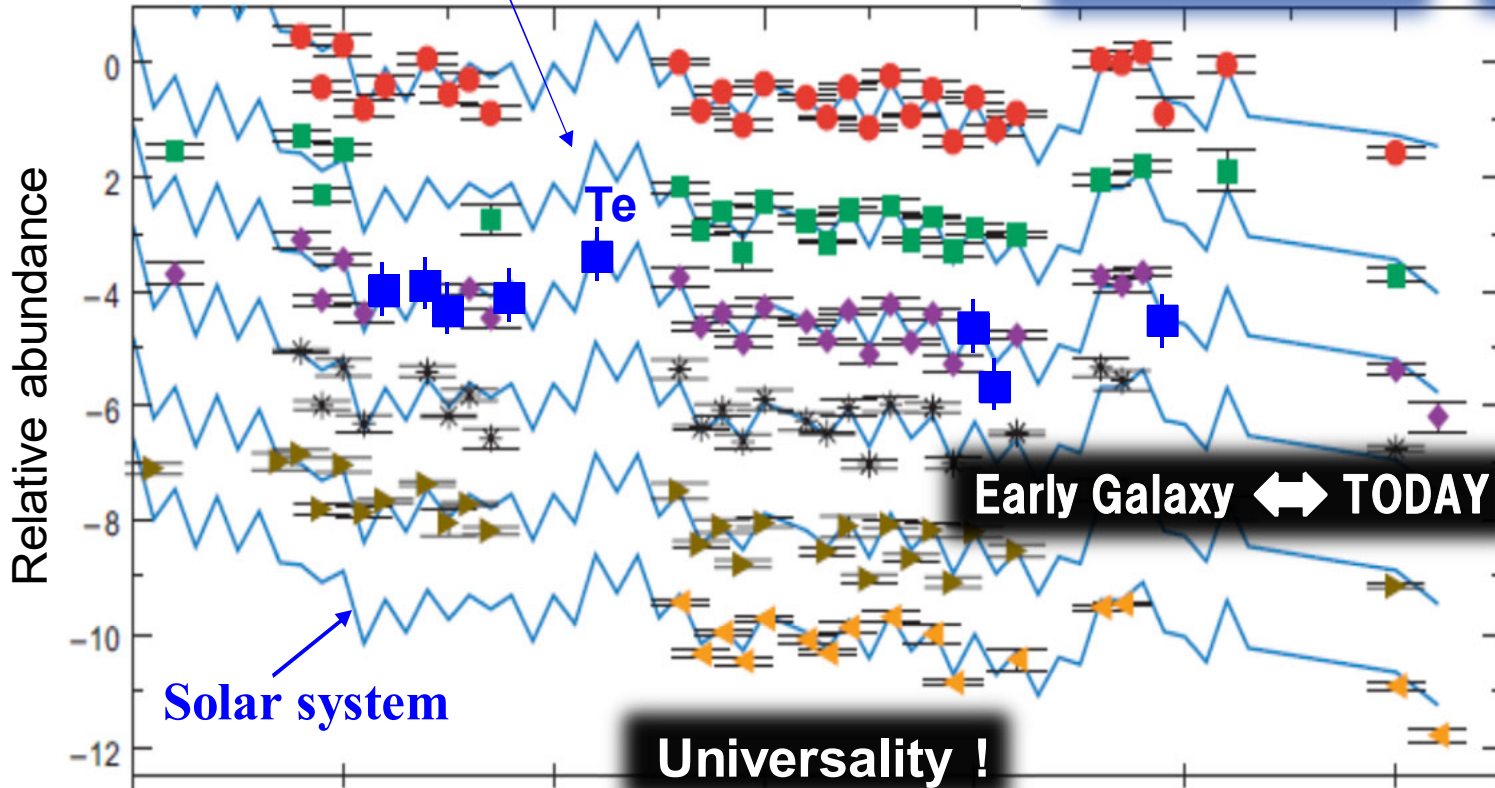
— 3.0

— 2.1

— 2.9

— 2.2

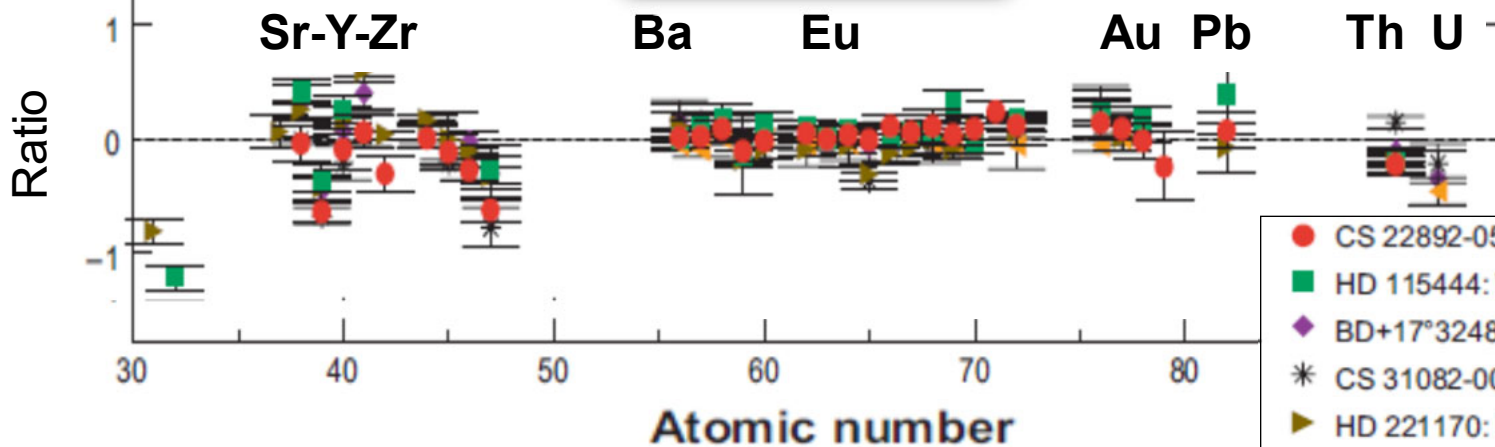
— 3.0



Solar system

Early Galaxy  $\leftrightarrow$  TODAY

Universality !

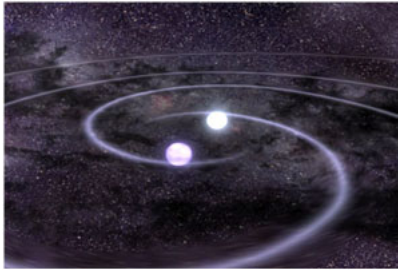


born in the early Galaxy

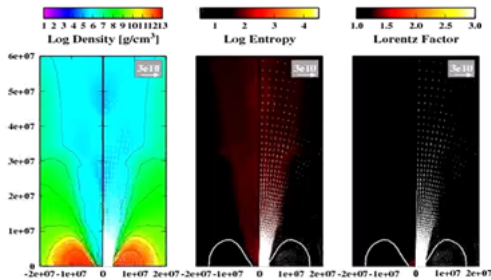
- CS 22892-052: Sneden et al. (2003)
- HD 115444: Westin et al. (2000)
- ◆ BD+17°324817: Cowan et al. (2002)
- \* CS 31082-001: Hill et al. (2002)
- ▶ HD 221170: Ivans et al. (2006)
- ◀ HE 1523-0901: Frebel et al. (2007)

Kajino, Aoki, Balantekin,  
Diehl, Famiano, Mathews,  
Prog. Part. Nucl. Phys. 107  
(2019) 109-166.

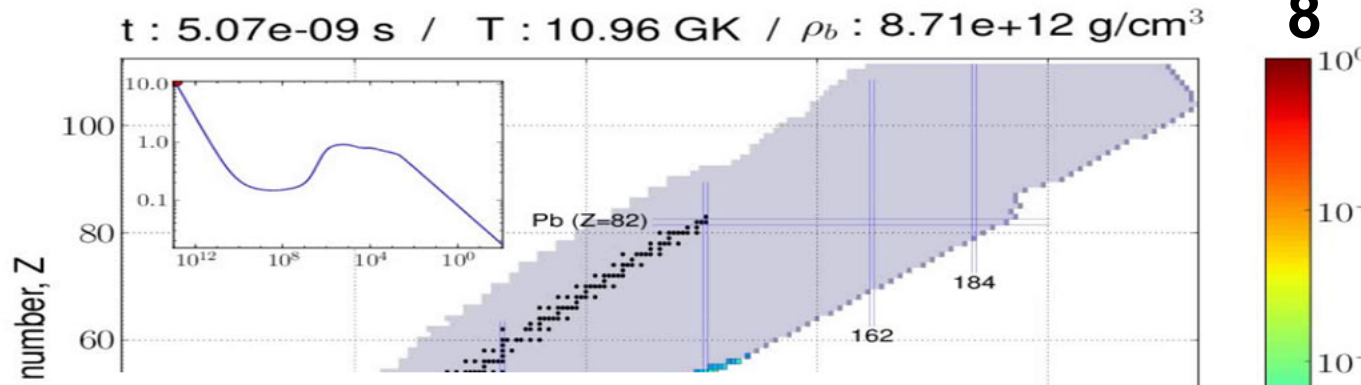
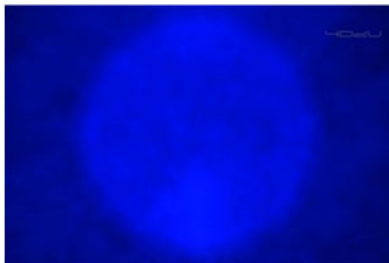
## Neutron Star Merger



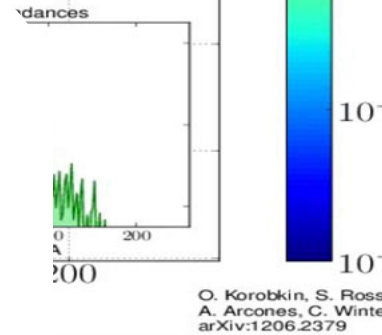
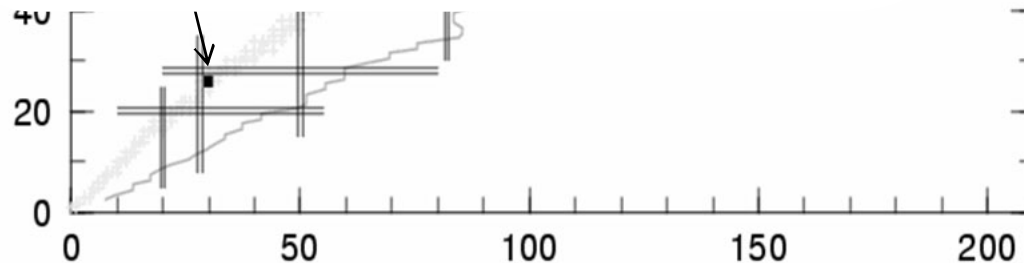
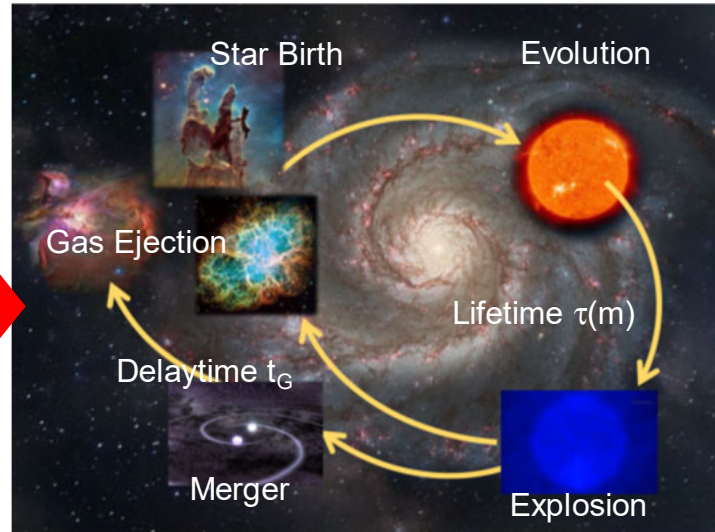
## Collapsar Jet



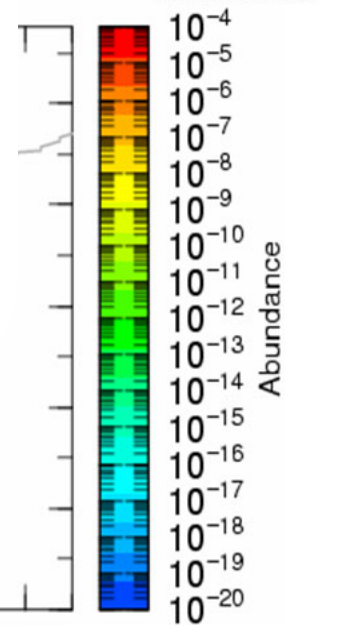
## MHD Jet Supernova



## Cosmic & Galactic Evolution



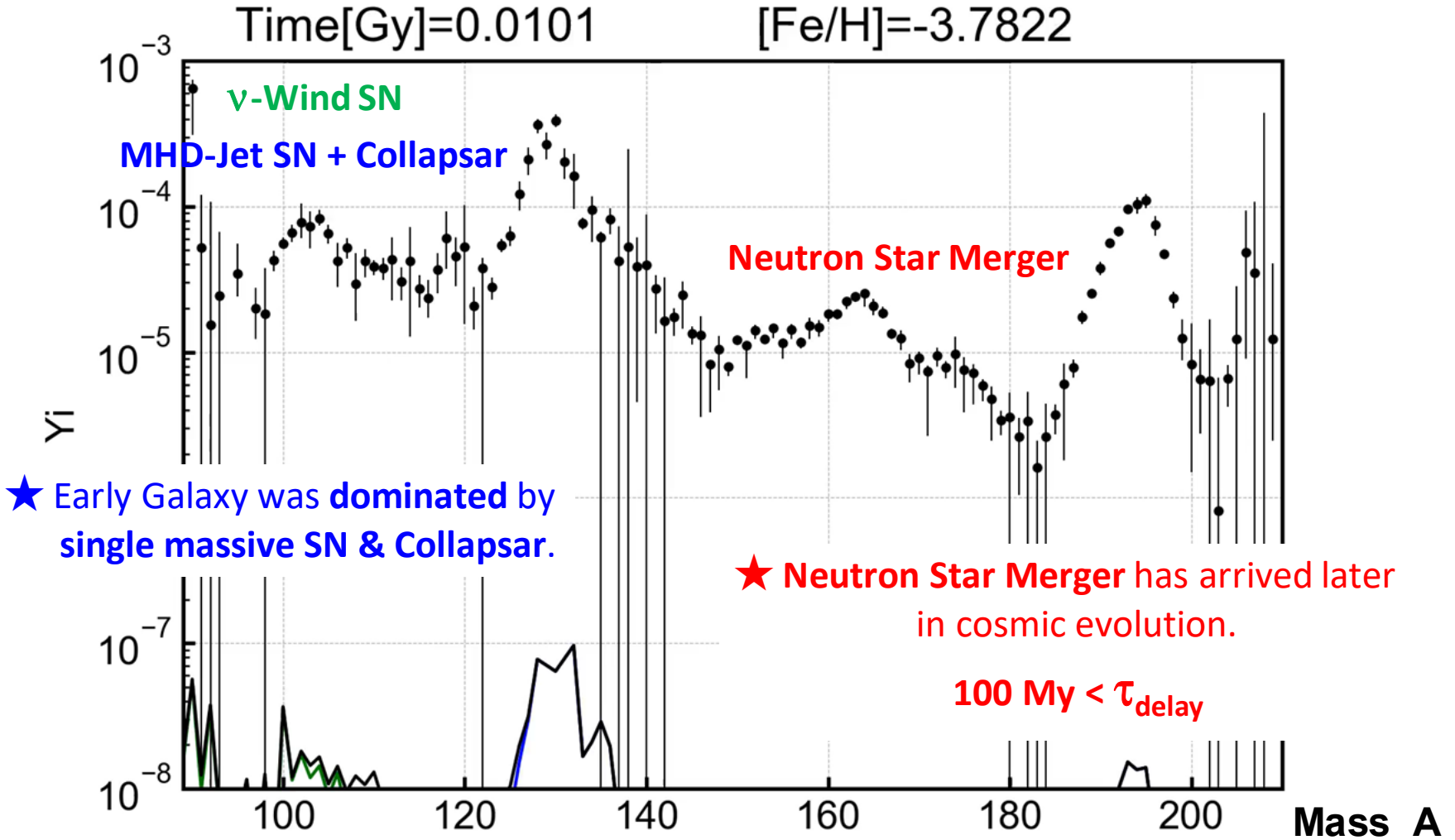
O. Korobkin, S. Rosswater,  
A. Arcones, C. Woosley,  
arXiv:1206.2379



$$t/10\text{Gy} = 10^{[\text{Fe}/\text{H}]}$$



$$[\text{Fe}/\text{H}] = \log(N_{\text{Fe}}/N_{\text{H}})_{\star} - \log(N_{\text{Fe}}/N_{\text{H}})_{\odot}$$

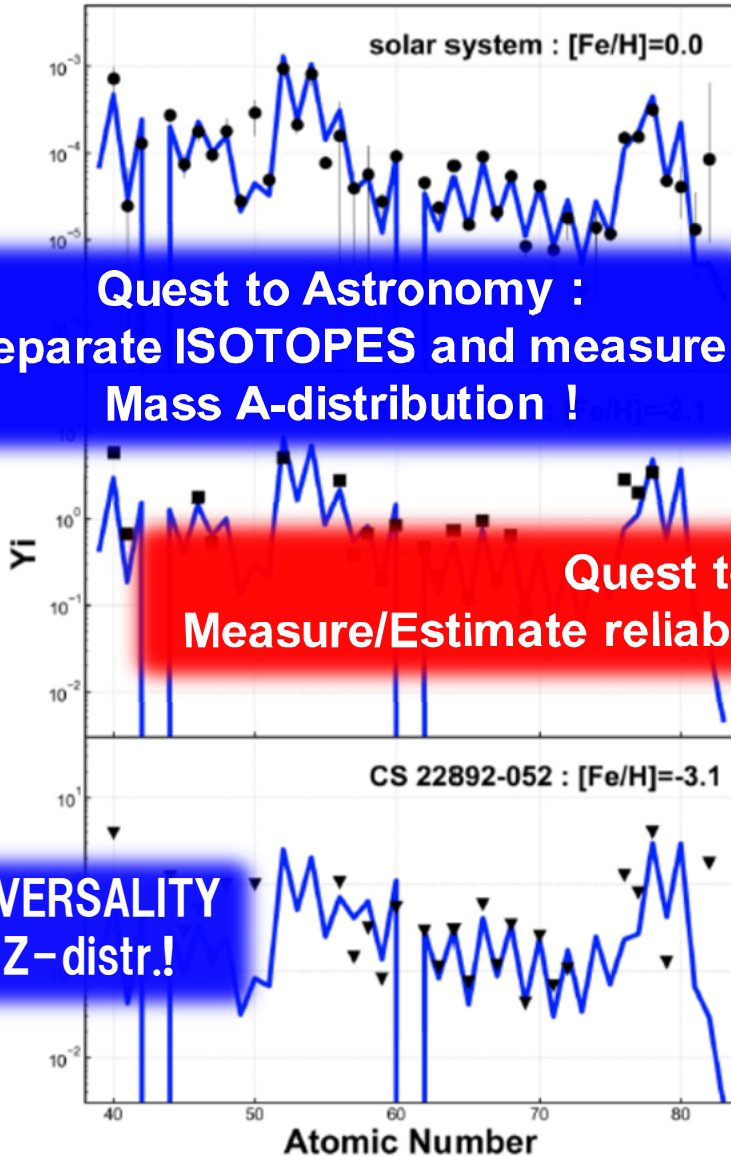


# Galactic Chemical Evolution

Yamazaki, He, Kajino, Mathews, Famiano, Tang, Shi, ApJ 933 (2022), 112.

◻ Solar abund.  
[Fe/H]=0.0

Symm. + Asymm. fission

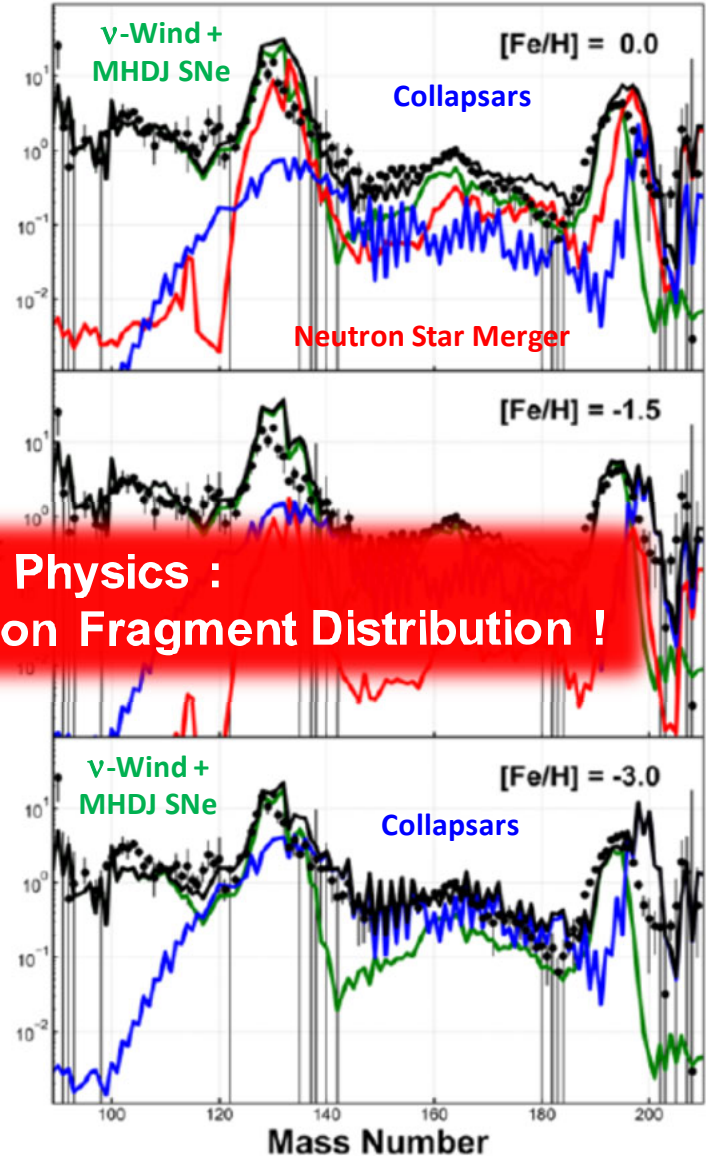


Quest to Astronomy :  
Separate ISOTOPES and measure  
Mass A-distribution !

Quest to Nucl. Physics :  
Measure/Estimate reliable Fission Fragment Distribution !

UNIVERSALITY  
in Z-distr.!

Symm. fission



Cosmic Time ↑

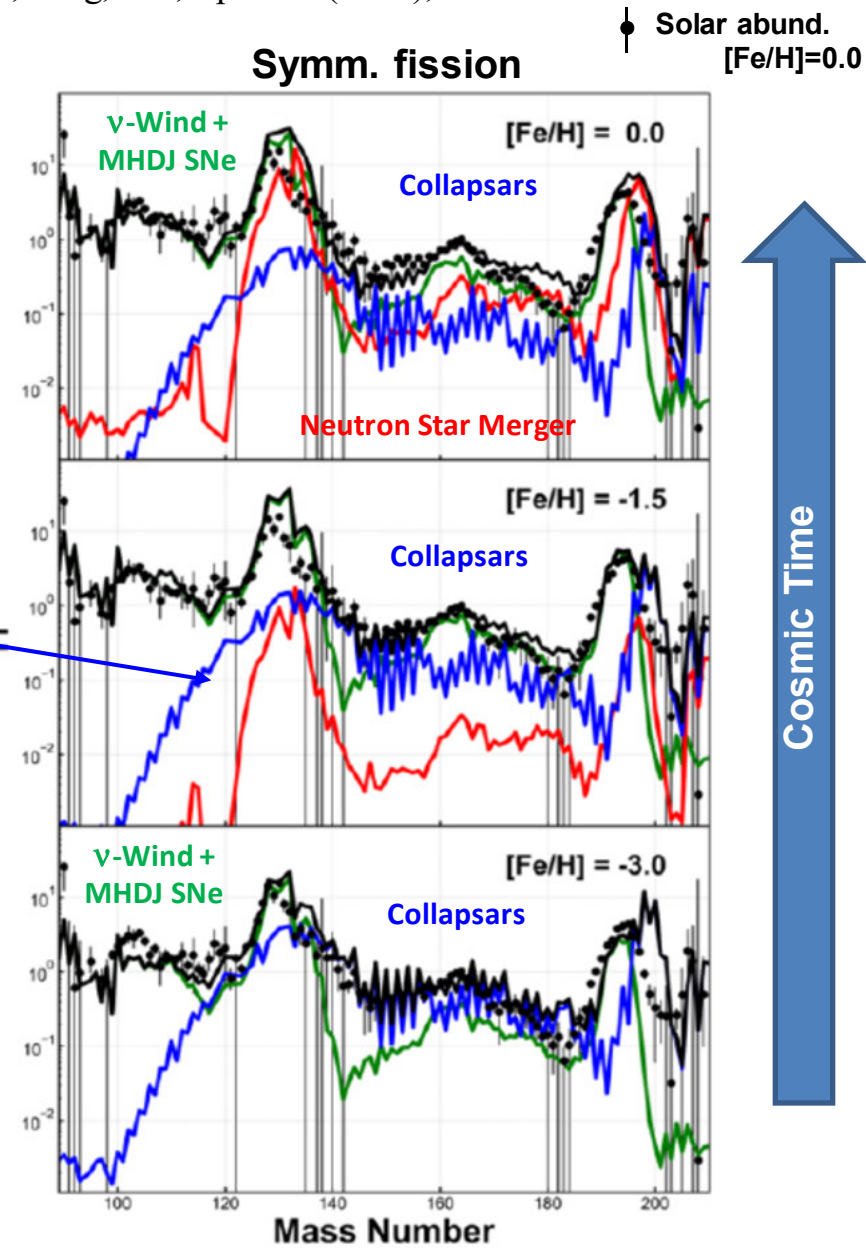
Yamazaki, He, Kajino, Mathews, Famiano, Tang, Shi, ApJ 933 (2022), 112.

He, Kajino, Kusakabe, Zhou, Koura, Chiba, Li and Lin, ApJ Lett 966 (2024), L34;  
He, Lin, Luo, Kajino and Li, ApJ 1000 (2026), 177.

**Discovery of New Process in Collapsar  
(BH forming supernova)**

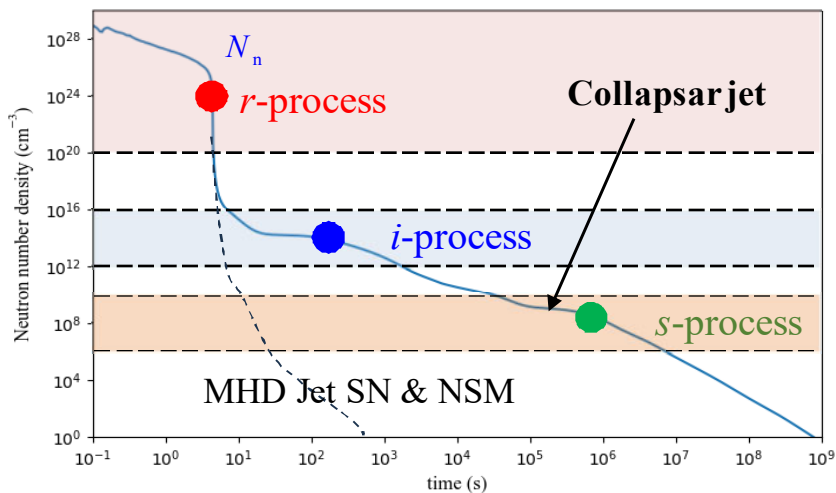
**Three n-capture processes can coexist.**

- r (rapid)
- i (intermediate)
- s (slow)



# Coexistence of r-, i-, s-processes in Collapsar r-process

He, Kajino, Kusakabe, Zhou, Koura, Chiba, Li and Lin, ApJ Lett 966 (2024), L34; He, Lin, Luo, Kajino & Li, ApJ 1000 (2026), 177.



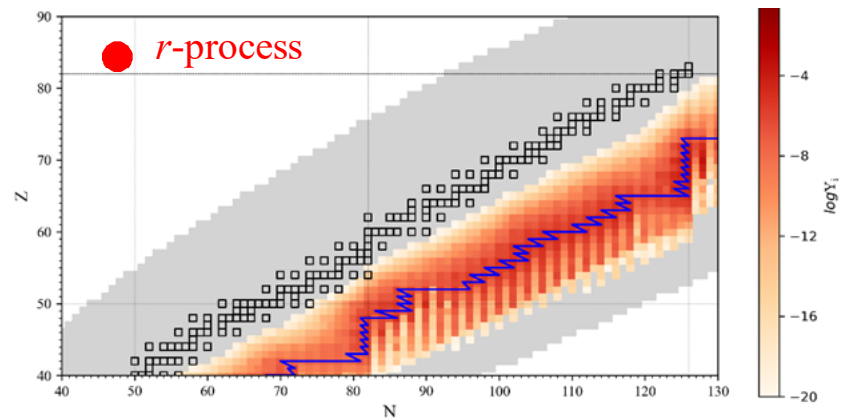
	$N_n$ ( $\text{cm}^{-3}$ )
<i>r</i> -process:	$>10^{20}$
<i>i</i> -process:	$10^{12} \sim 10^{16}$
<i>s</i> -process:	$10^6 \sim 10^{10}$

## Fissions Neutrons from $^{276}\text{Rf}$ , $^{260}\text{Fm}$ & Trans-Uranium Isotopes for i-process

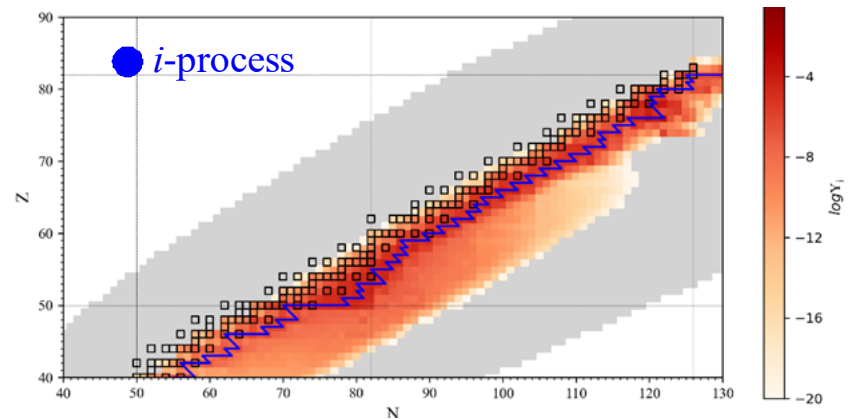
(n,  $\gamma$ ) collision time      Expansion time-scale

$$\tau_{(n,\gamma)} = \frac{1}{\rho Y_n N_A \langle \sigma v \rangle} < \tau_{\text{dyn}} = - \left( \frac{d \ln T_9}{dt} \right)^{-1}$$

time(s) = 4.5;  $T_9 = 0.86$ ;  $\rho(\text{gcc}) = 1.8 \times 10^2$ ;  $Y_n = 1.6 \times 10^{-6}$ ;  $N_n(\text{cm}^{-3}) = 1.8 \times 10^{20}$



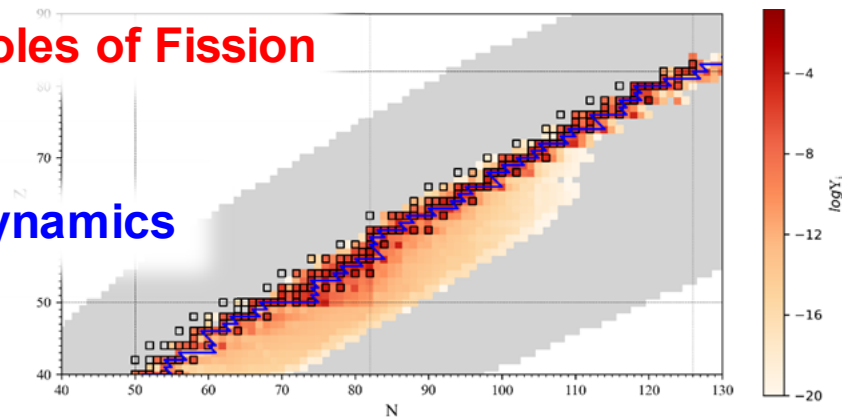
time(s) =  $3.8 \times 10^2$ ;  $T_9 = 0.056$ ;  $\rho(\text{gcc}) = 5.1 \times 10^{-2}$ ;  $Y_n = 7.7 \times 10^{-10}$ ;  $N_n(\text{cm}^{-3}) = 2.4 \times 10^{13}$



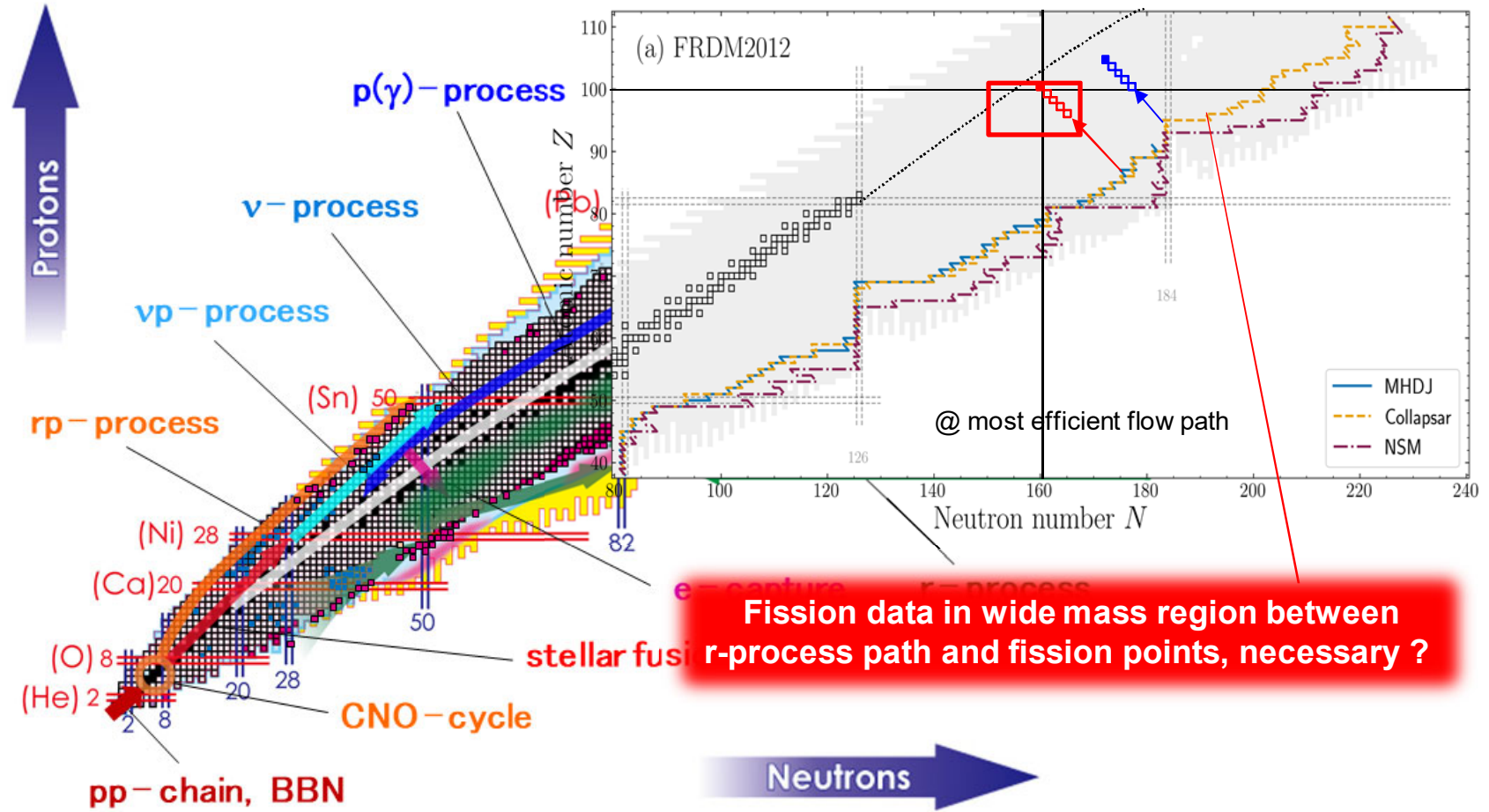
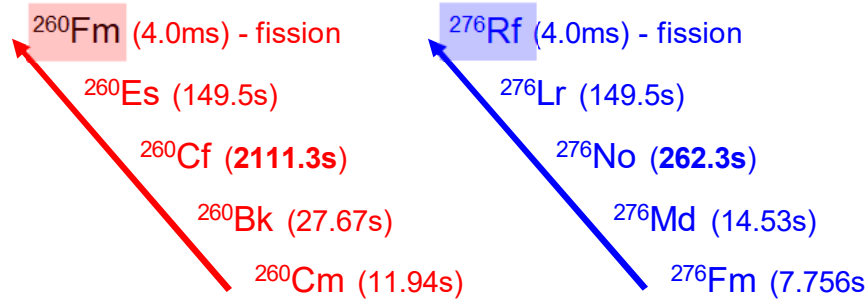
time(s) =  $2.1 \times 10^6$ ;  $T_9 = 0.01$ ;  $\rho(\text{gcc}) = 6.3 \times 10^{-9}$ ;  $Y_n = 5.6 \times 10^{-9}$ ;  $N_n(\text{cm}^{-3}) = 2.1 \times 10^7$

## Roles of Fission

## Dynamics

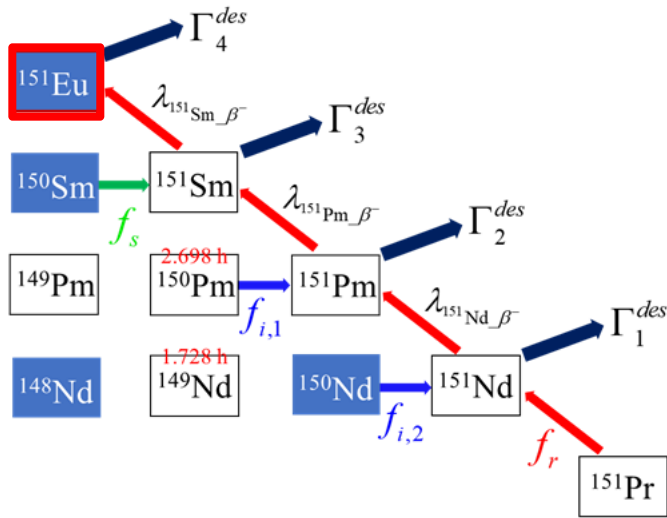


262Fm	263Fm	264Fm	265Fm	266Fm	267Fm	268Fm	269Fm	270Fm	271Fm	272Fm	273Fm	274Fm	275Fm	276Fm
30.07 s	2.59 s	1.001 s	370 $\mu$ s	1.5 s	4 ms	1.20 s	2.74 s	18.8 s	2.74 s	18.8 s	140.3 s	11.2 s	1.36 s	9.83 s
262Es	263Es	264Es	265Es	266Es	267Es	268Es	269Es	270Es	271Es	272Es	273Es	274Es	275Es	276Es
275.7 d	19.4 s	87.8 s	20.4 s	138.0 s	13.9 s	3.38 s	6.78 s	13.3 s	23.4 s	32.7 s	1.44 s	1.44 s	1.44 s	1.44 s
262Cf	263Cf	264Cf	265Cf	266Cf	267Cf	268Cf	269Cf	270Cf	271Cf	272Cf	273Cf	274Cf	275Cf	276Cf
11.01 s	10.0 s	1.4 s	12.3 s	12.3 s	12.3 s	12.3 s	12.3 s	12.3 s	12.3 s	12.3 s	12.3 s	12.3 s	12.3 s	12.3 s
262Bk	263Bk	264Bk	265Bk	266Bk	267Bk	268Bk	269Bk	270Bk	271Bk	272Bk	273Bk	274Bk	275Bk	276Bk
1.8 m	1.40 s	3.70 s	23.4 m	39.7 s	1.43 m	12.8 s	12.8 s	12.8 s	12.8 s	12.8 s	12.8 s	12.8 s	12.8 s	12.8 s
261Cm	262Cm	263Cm	264Cm	265Cm	266Cm	267Cm	268Cm	269Cm	270Cm	271Cm	272Cm	273Cm	274Cm	275Cm
34.8 m	132.3 y	23.5 m	1.337 y	46.9 m	1.66 m	1.66 m	1.66 m	1.66 m	1.66 m	1.66 m	1.66 m	1.66 m	1.66 m	1.66 m



Astronomers

He, Kajino, et al. with Li & Lin,  
ApJ Lett 966 (2024), L34.

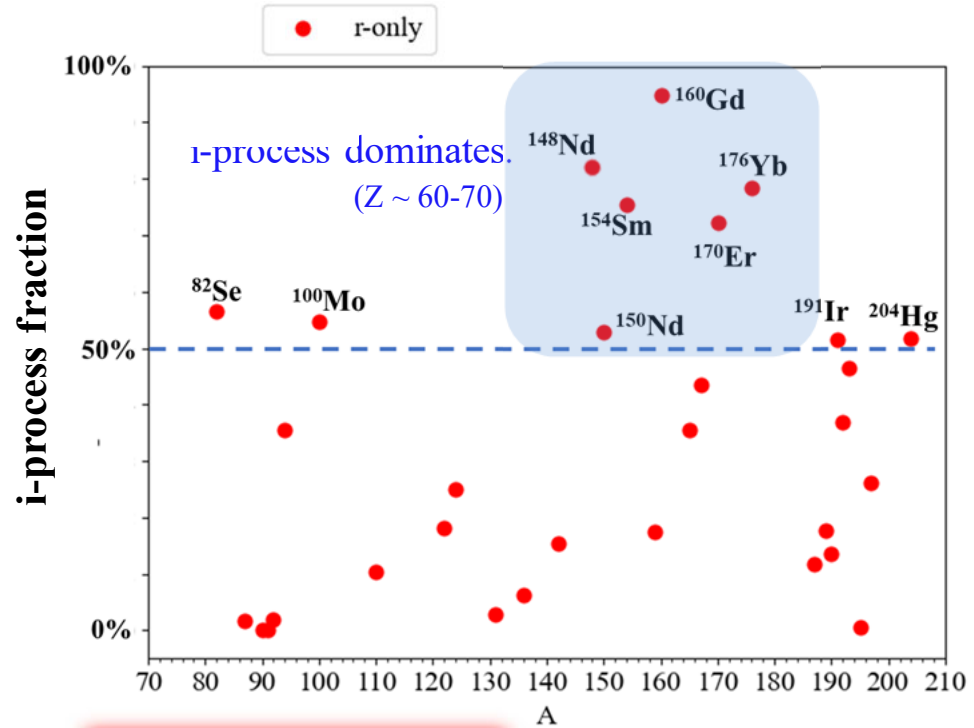


Theoretical Formulae:

$$Y_s = \int_0^T dt P_4^{sur}(t; T) \left[ \lambda_{151Sm\beta^-} \int_0^t d\tau f_s(\tau) P_3^{sur}(\tau; t) \right]$$

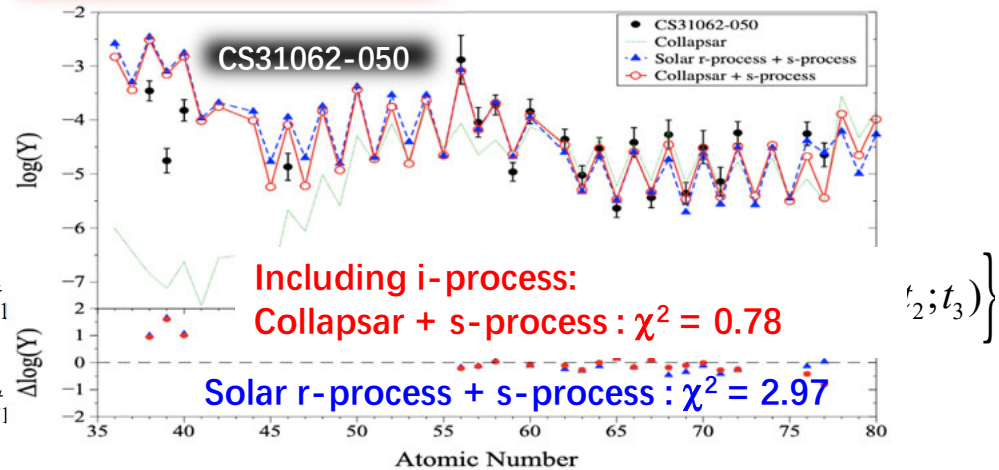
$$Y_i = \int_0^T dt_3 P_4^{sur}(t_3; T) \left\{ \lambda_{151Sm\beta^-} \int_0^{t_3} dt_2 \left[ \lambda_{151Pm\beta^-} \int_0^{t_2} dt_1 \right. \right.$$

$$\left. \left. Y_r = \int_0^T dt_3 P_4^{sur}(t_3; T) \left\{ \lambda_{151Sm\beta^-} \int_0^{t_3} dt_2 \left[ \lambda_{151Pm\beta^-} \int_0^{t_2} dt_1 \right. \right. \right. \right.$$



Observational Signal

Hempel et al. (2016)

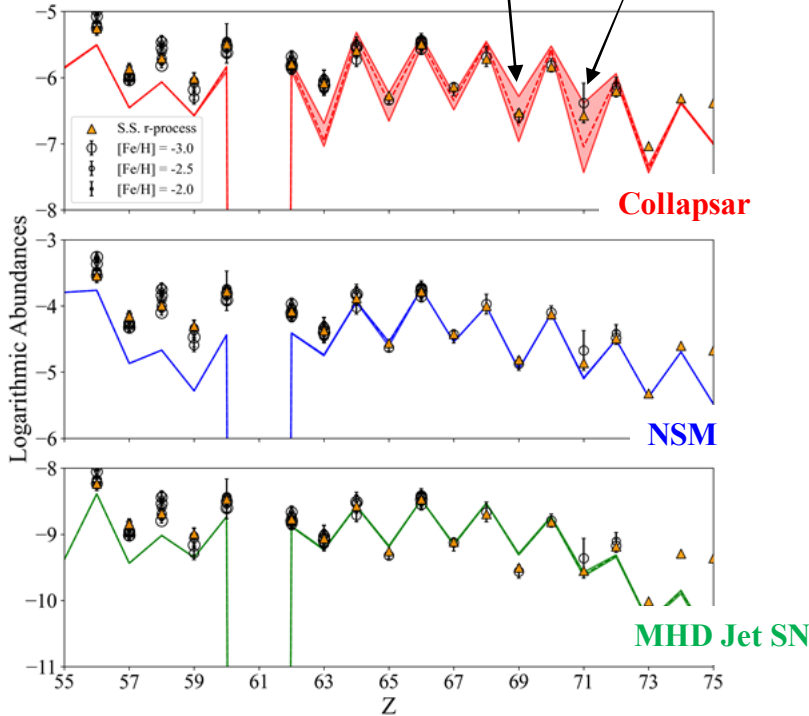


Astronomers

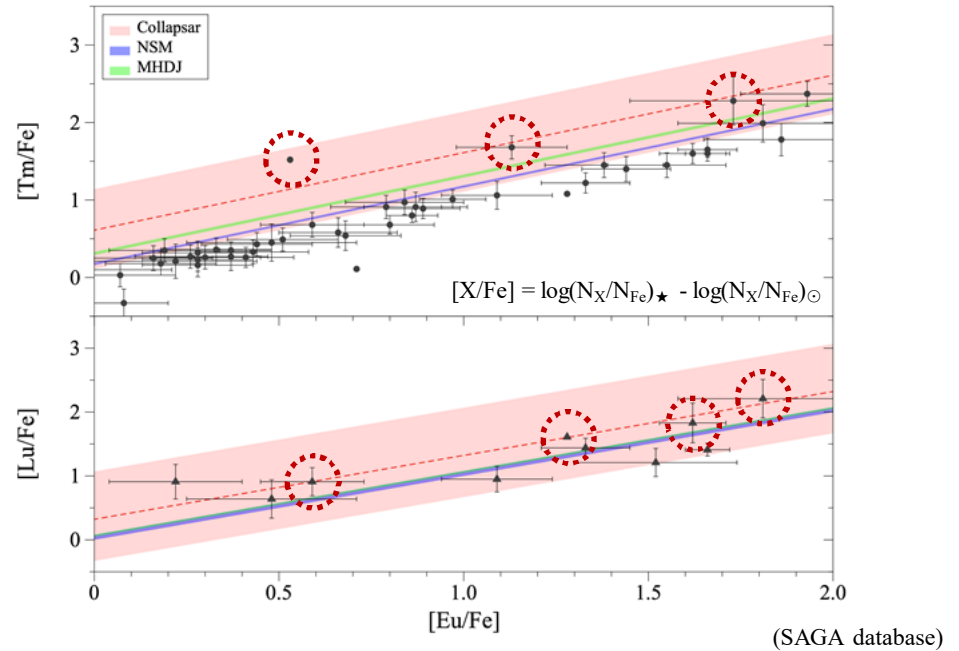
He, Lin, Luo, Kajino & Li, ApJ 1000 (2026), 177.

## I. Observational Signal ?

Tm (Z = 69) Lu (Z = 71)



**[Tm/Eu] or [Lu/Eu], enhanced !**



## II. Precise Experimental Input ?

- (n,  $\gamma$ ) Reaction Rates

- Fission Frag. Distr.

➤ Top 10 important (n, $\gamma$ ) reactions for **Tm**

$^{175}\text{Yb}(n,\gamma)^{176}\text{Yb}$ ,  $^{153}\text{Sm}(n,\gamma)^{154}\text{Sm}$ ,  $^{151}\text{Pm}(n,\gamma)^{152}\text{Pm}$ ,  $^{172}\text{Er}(n,\gamma)^{173}\text{Er}$ ,  $^{175}\text{Tm}(n,\gamma)^{176}\text{Tm}$ ,  $^{166}\text{Ho}(n,\gamma)^{167}\text{Ho}$ ,  $^{151}\text{Nd}(n,\gamma)^{152}\text{Nd}$ ,  $^{152}\text{Pm}(n,\gamma)^{153}\text{Pm}$ ,  $^{149}\text{Nd}(n,\gamma)^{150}\text{Nd}$ ,  $^{147}\text{Nd}(n,\gamma)^{148}\text{Nd}$

➤ Top 10 important (n, $\gamma$ ) reactions for **Lu**

$^{169}\text{Er}(n,\gamma)^{170}\text{Er}$ ,  $^{153}\text{Sm}(n,\gamma)^{154}\text{Sm}$ ,  $^{166}\text{Dy}(n,\gamma)^{167}\text{Dy}$ ,  $^{151}\text{Pm}(n,\gamma)^{152}\text{Pm}$ ,  $^{168}\text{Ho}(n,\gamma)^{169}\text{Ho}$ ,  $^{174}\text{Tm}(n,\gamma)^{175}\text{Tm}$ ,  $^{151}\text{Nd}(n,\gamma)^{152}\text{Nd}$ ,  $^{152}\text{Pm}(n,\gamma)^{153}\text{Pm}$ ,  $^{149}\text{Nd}(n,\gamma)^{150}\text{Nd}$ ,  $^{147}\text{Nd}(n,\gamma)^{148}\text{Nd}$

# Fission Fragments

## Quantum Tunneling

### KTUY - mass model

Koura, Tachibana, Uno, Yano  
Prog. Theor. Phys. 113 (2005)

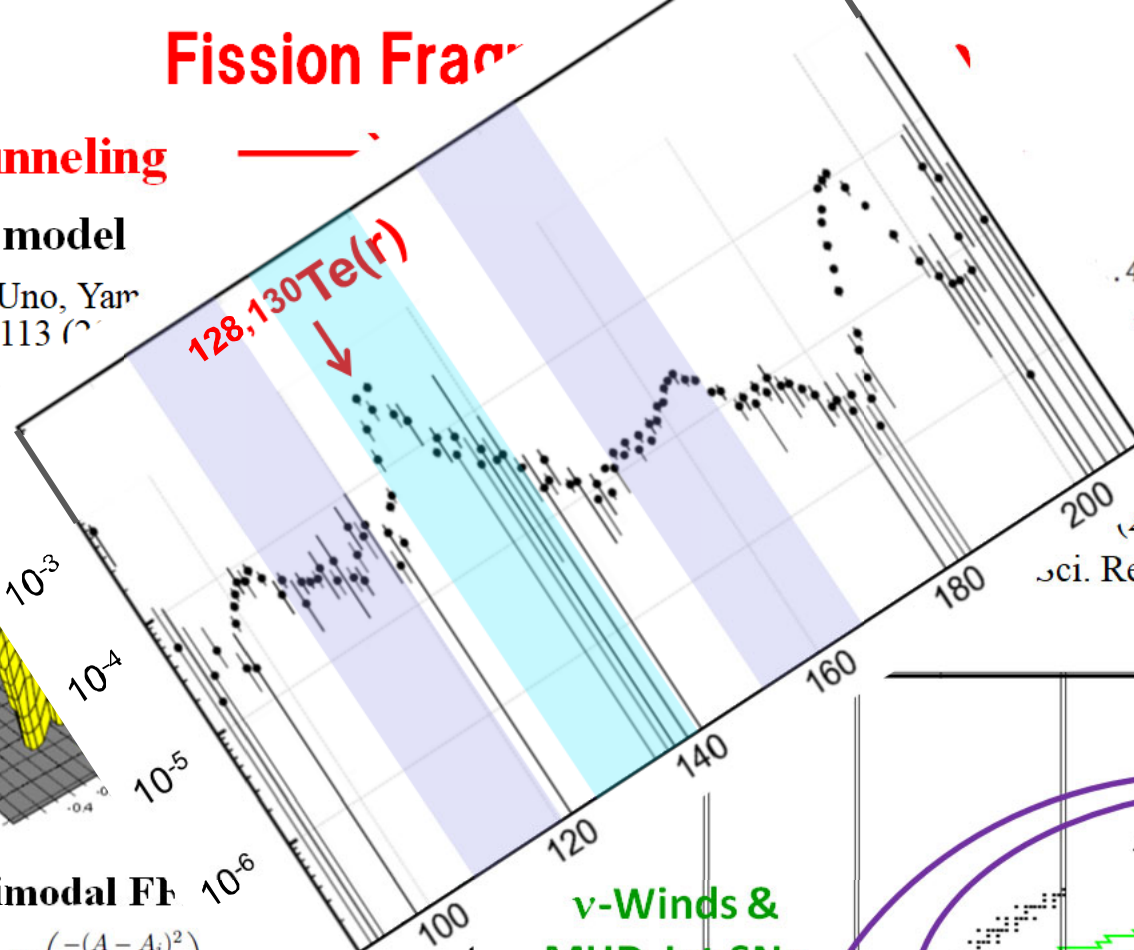
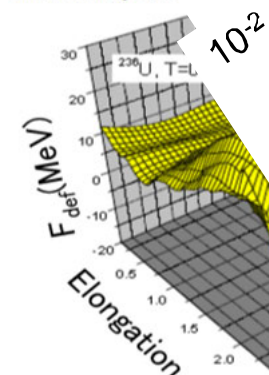
$$V_4 = [ZZ_0, \alpha, \delta_L, \delta_R]$$

$$V_{\text{term}}^{-1} = \sum_{jk} p_j p_k + \sum_{ij} g_{ij} R_j(t)$$

Wiener term

$$F = E - T$$

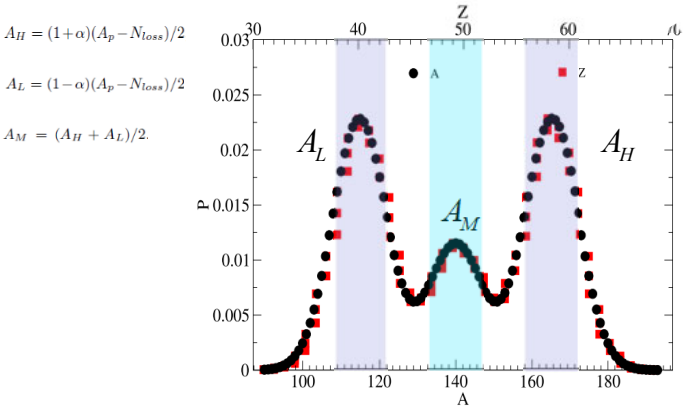
DM+Strutinsky+BCS



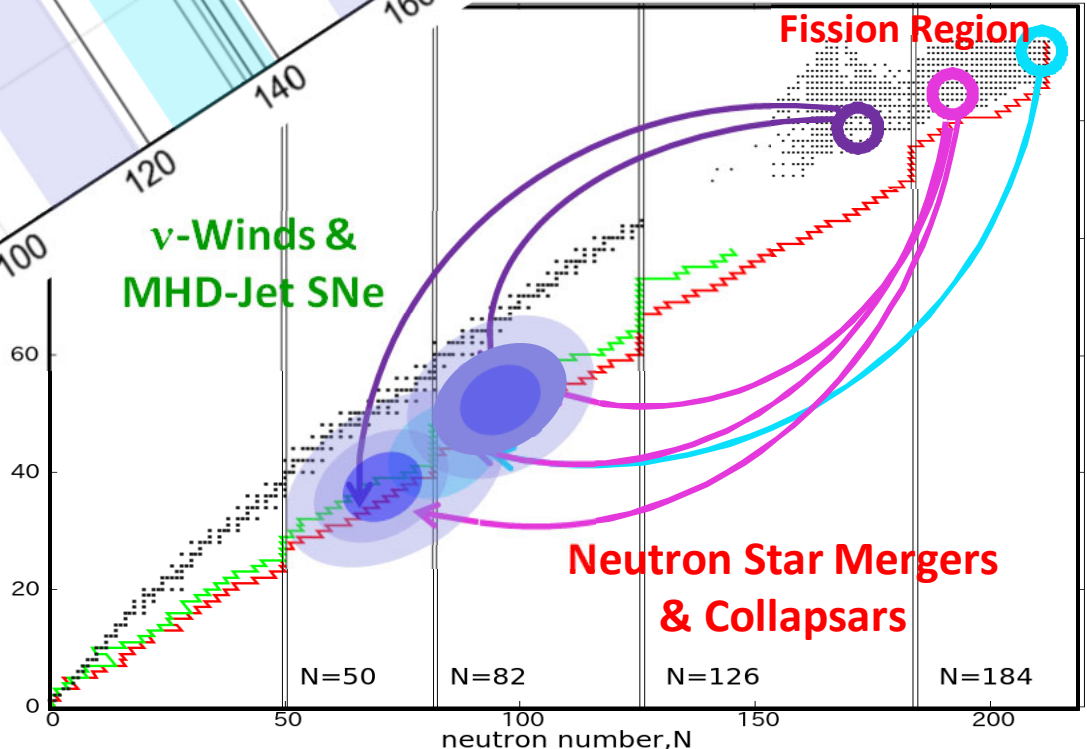
(2018), 054331; Okumura  
Sci. Reports, 9 (2019), 1525.

### Bimodal or Trimodal Fission

$$f(A, A_p) = \sum_{A_i} \frac{1}{\sqrt{2\pi}\sigma} W_i \exp\left(\frac{-(A - A_i)^2}{2\sigma^2}\right)$$



ν-Winds & MHD-Jet SNe



Neutron Star Mergers & Collapsars

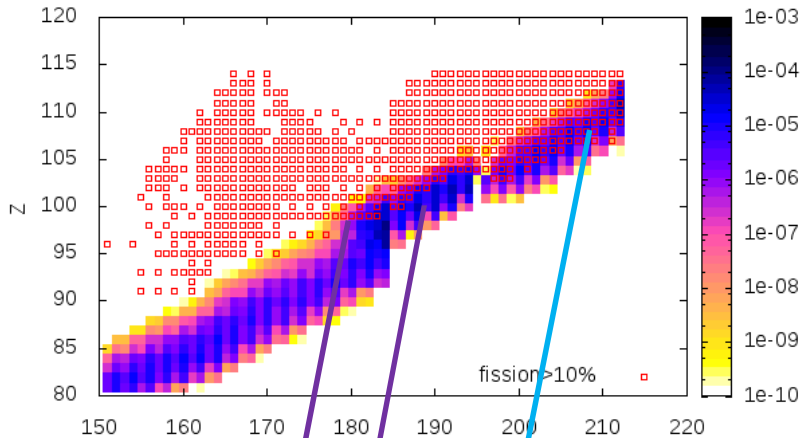
N=50    N=82    N=126    N=184

# Abundance Evolution of Fission Recycling

**Collapsar Model:** Yamazaki, He, Kajino, Mathews, Famiano, Tang, Shi, ApJ 933 (2022), 112.

Later time

2.62E+00



Fission

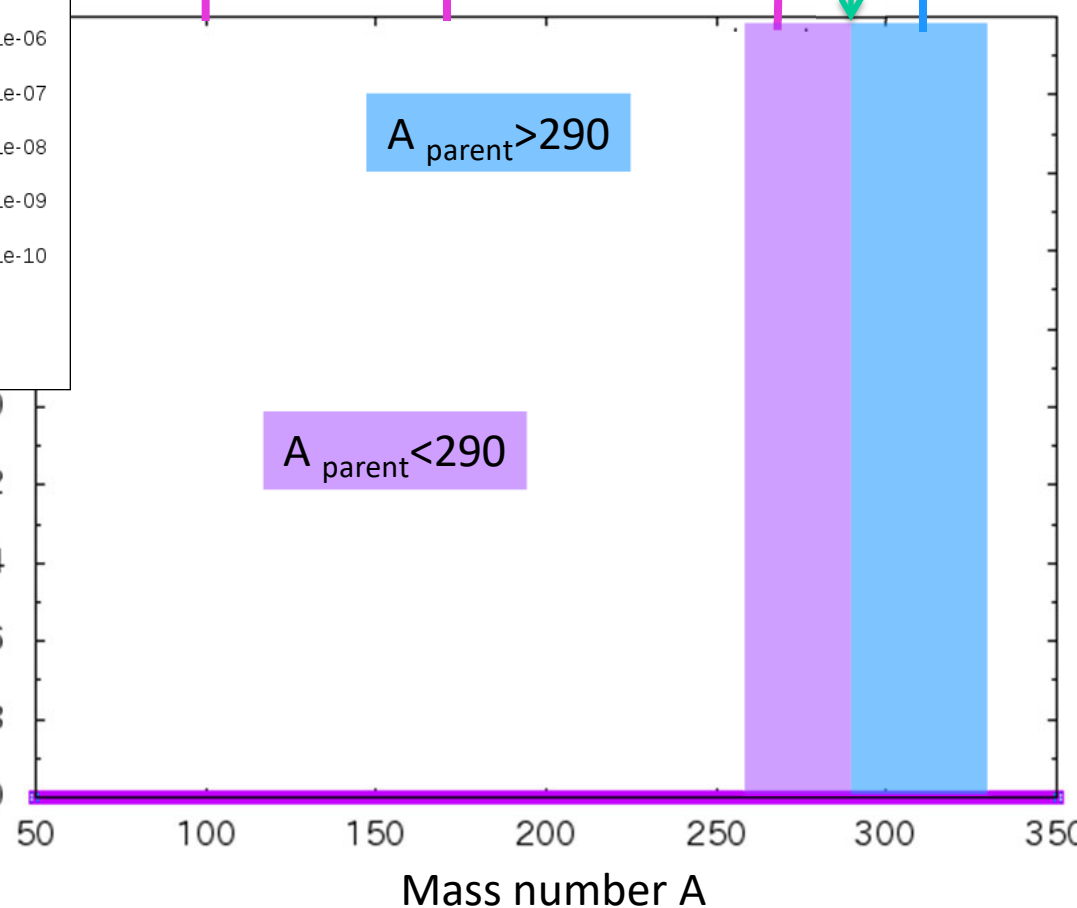
Parent

0.00E+00[sec]

A=310

$A_{parent} > 290$

$A_{parent} < 290$



Yield of Fission Fragment

- Z=99, A=279
- Z=101, A=288
- Z=104, A=303
- Z=113, A=325

Mass number

Mass number A

# Nuclear Mass Models

## Finite-Range Droplet Model (FRDM)

- Global nuclear mass model,
- Coupled macroscopic and microscopic theories.

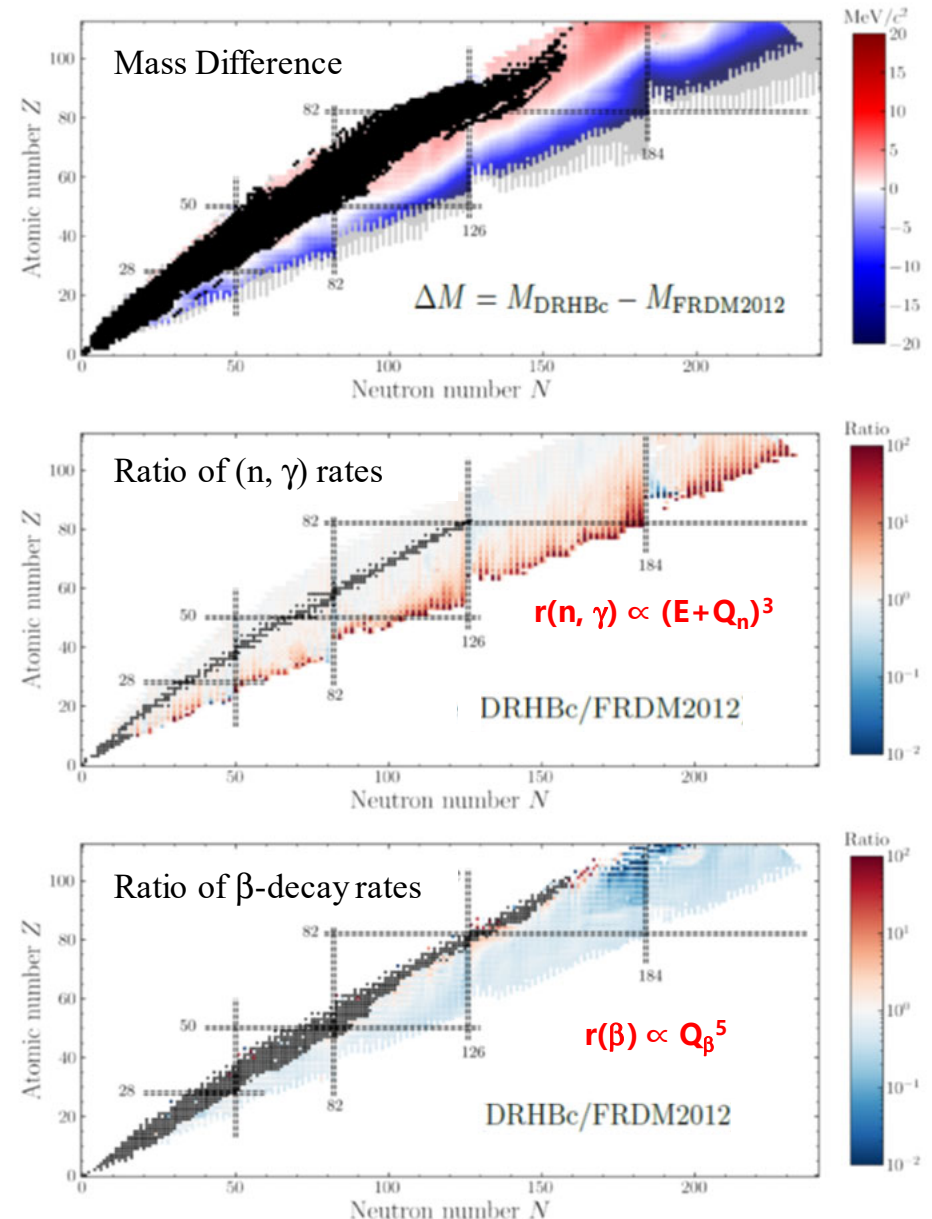
## Deformed Relativistic Hartree-Bogoliubov Theory in continuum (DRHBc)

- Axial deformation symmetry, considered,
- Meson-exchange interactions, included,
- Deformed relativistic Hartree-Bogoliubov eq. is solved in a Dirac Woods-Saxon basis,
- With contact interactions, applying to even-even, odd- $A$ , and odd-odd nuclei.

Choi, Kim, He, Choi, Kim, Kajino,  
Phys. Rev. C113 (2026), 024329,  
Application to r-process with deep learning for nuclear masses in DRHBc.

Choi, He, kim, Kim, Kajino  
Astrophys. J. (2026), to be submitted,  
Application of DRHBc to r-process in MHDJ Supernova,  
Collapsar, and Neutron Star Merger.

Choi, He, Kim, Kim, Kajino (2026), to be submitted.



# TDDFT for Nuclear Fission/Fusion and Systematic DFT Calculations of Ground-state Properties

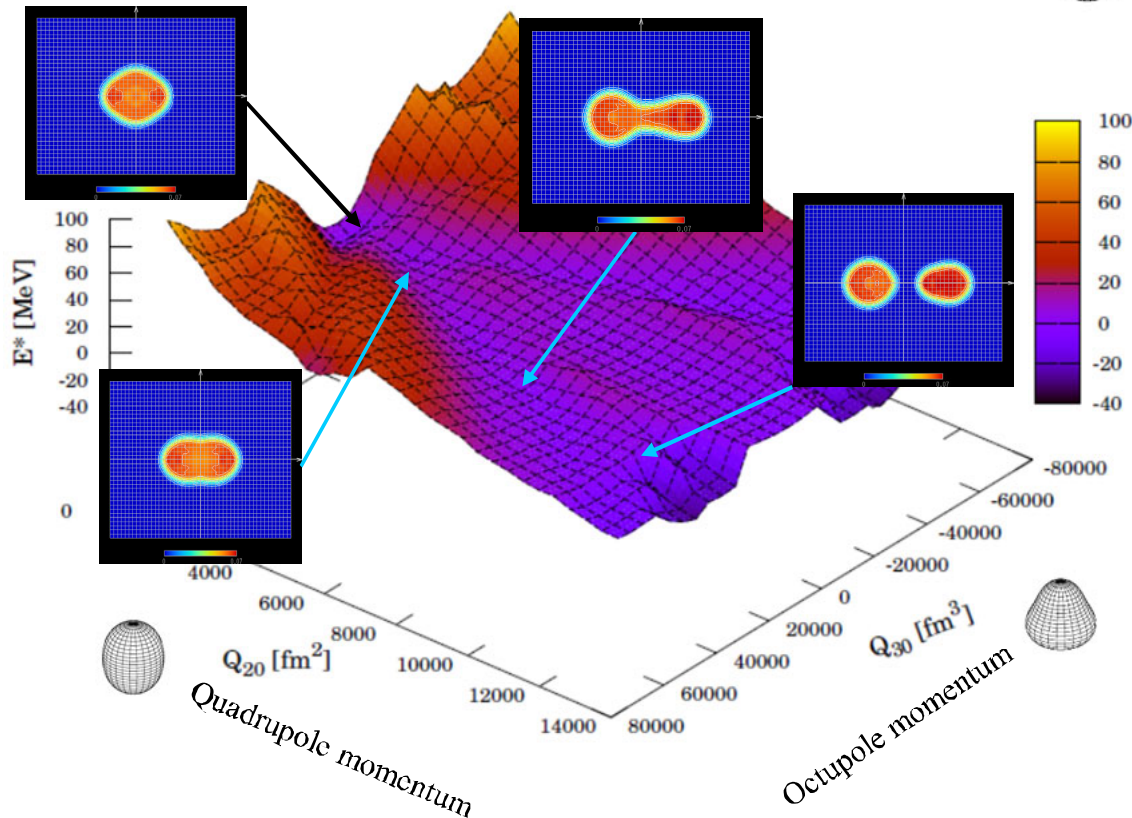
~ DFT applications on nuclear physics ~

Shuichiro Ebata (Saitama Univ.) & Takashi Nakatsukasa (Tsukuba Univ.)

S.Ebata, T.Nakatsukasa,  
Phys. Scr. **92** (2017) 064005;  
S. Ebata et al.,  
Int. J. Mod. Phys. E **32** (2023) 235003;  
EPJ Web of Conf. **284** (2023) 04008

## Large amplitude collective motion: Fission

Potential energy surface in Quadrupole-Octupole Collective space is obtained by the constraint 3D Skyrme HF+BCS (Static calculation).



## About 60% nuclei are deformed!



- ✓ From the density distributions of fission fragments, their charge distributions are obtained.
- ✓ The charge distribution is important quantity to estimate neutron emission.
- ✓ The microscopic results can contribute to the nuclear engineering.

Courtesy from S. Ebata

CENS-TOPTIER Theory Collaborative Working Meeting, 2026. Apr. 13 – 18,  
@ Yeosu, Expo Convention Center

## TDDFT Results

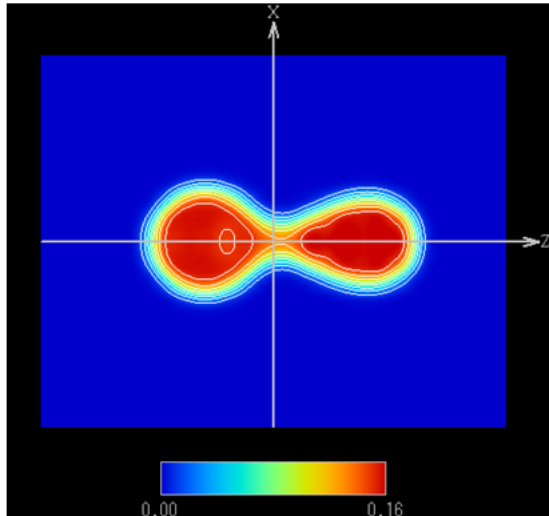
Large amplitude collective motion: Fission

### Charge polarization(CP) of fission fragments (FFs)

The distribution of atomic numbers in the FFs is an essential quantity to evaluate neutron emission from the FFs.

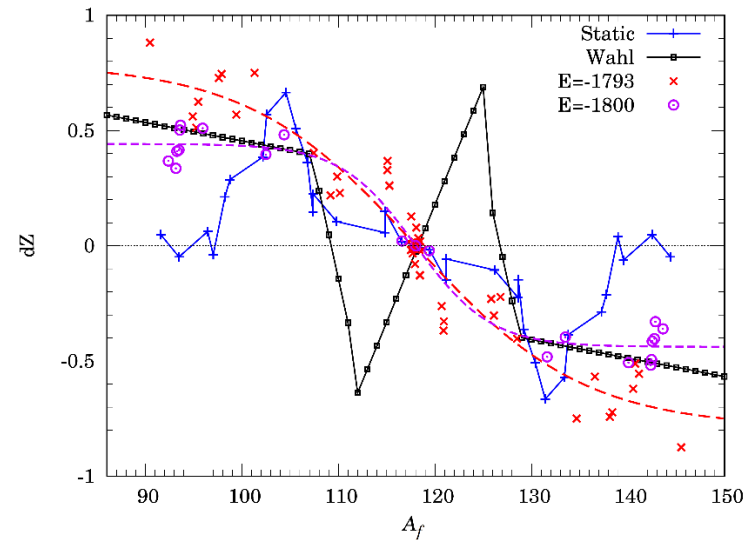
Prediction of the CP consistent with existing data is one of the reasons to justify the theoretical description of fission.

Time-evolution of nuclear density with the well deformed initial state.



S. Ebata et al., Int. J. Mod. Phys. E **32** (2023) 235003;  
EPJ Web of Conf. **284** (2023) 04008.

Dynamic model calculation shows  
qualitatively consistent results with existing nuclear data.



Next stage is to connect the theoretical results to statistical decay calculations to confirm the neutron multiplicity of fission fragments.

**Call for Systematic Prediction of FFD (TDDFT/TDGCM) for r-process!**

Fission-Astrophys. Collab. Project, underway

TDDFT (S. Ebata) → Langevin Simulation (Y. Aritomo) → r-process (T. Kajino)

# Purpose

To elucidate the roles of Fission &  $\nu$ s in Explosive Nucleosynthesis

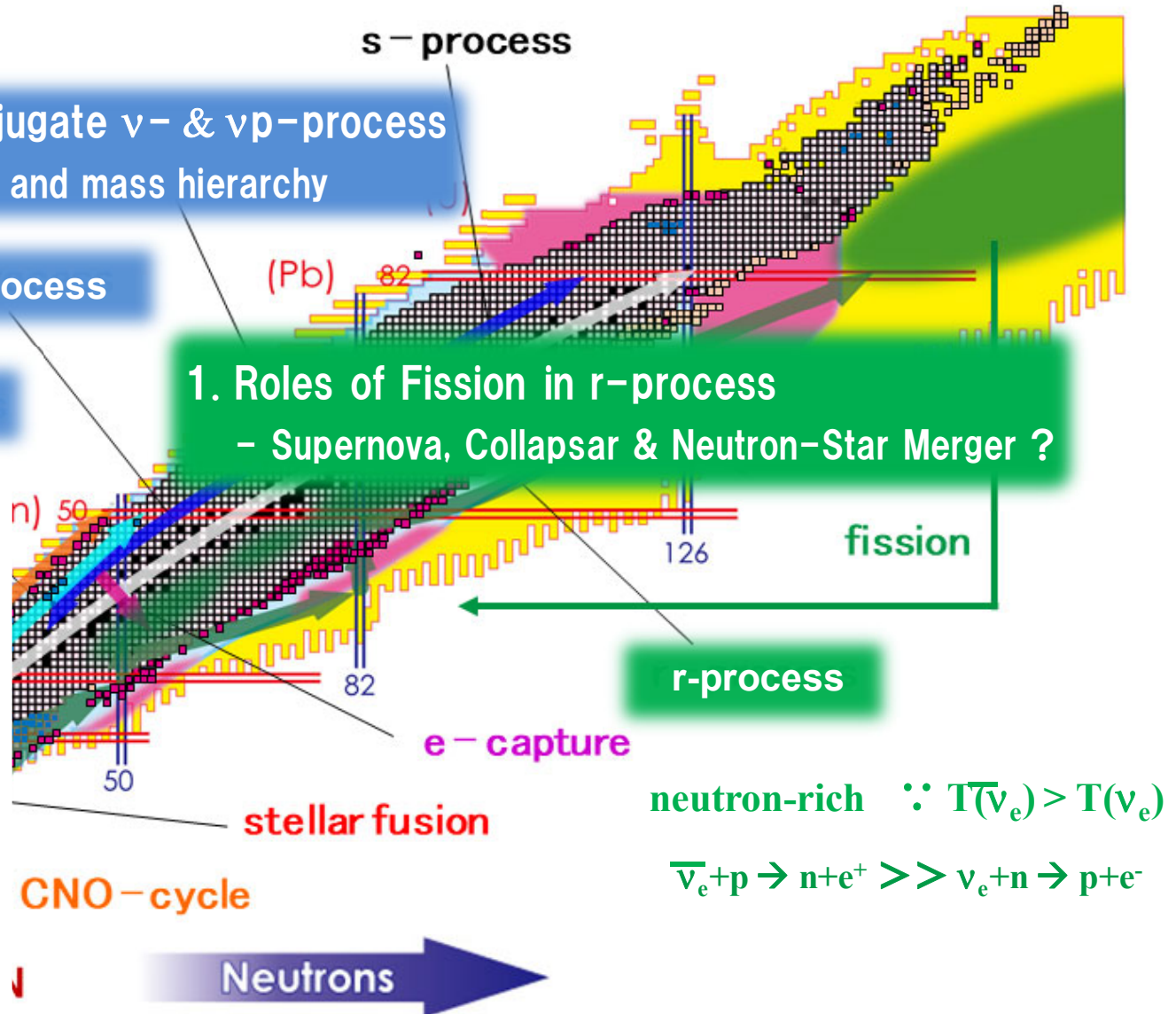
2. Roles of  $\nu$ s in conjugate  $\nu$ - &  $\nu p$ -process  
-  $\nu$  flavor oscillation and mass hierarchy

$\nu$ -process

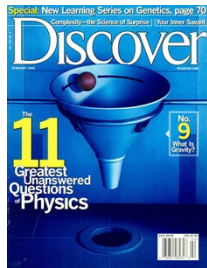
$\nu p$ -process

1. Roles of Fission in r-process

- Supernova, Collapsar & Neutron-Star Merger ?



The 11 Greatest Unanswered Questions in Physics !



- What is the origin of Uranium ?
- Why do neutrinos have mass ?

The National Research Council's Board on Physics, USA (2002)

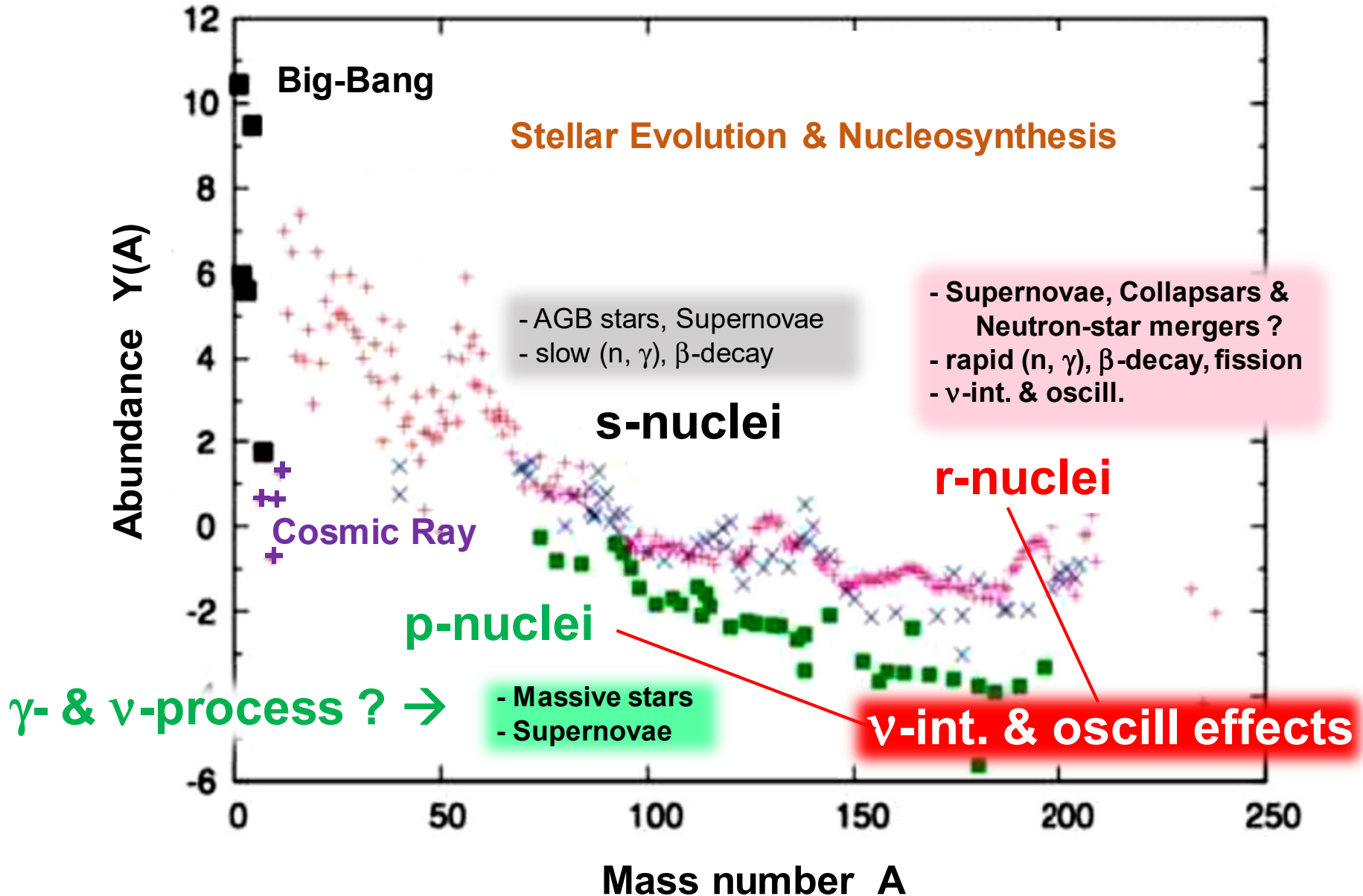
r-process

neutron-rich  $\because T(\bar{\nu}_e) > T(\nu_e)$



Neutrons

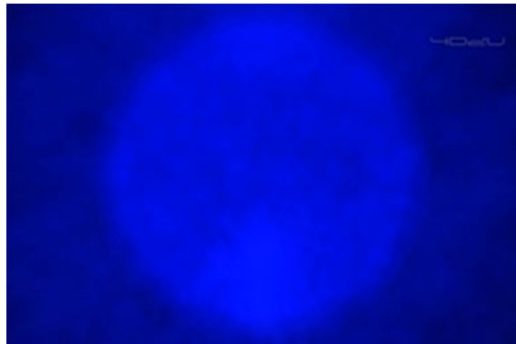
# Solar-system Abundances





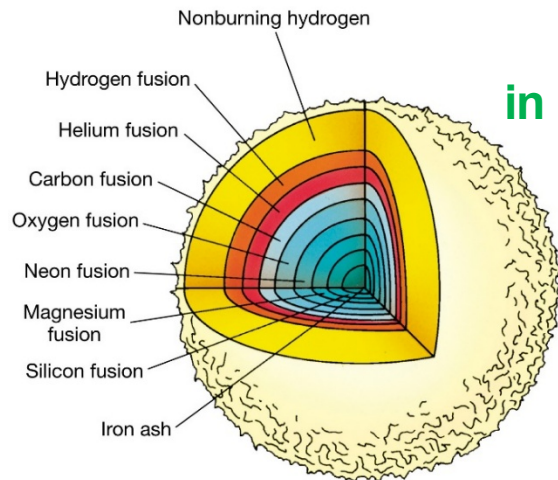
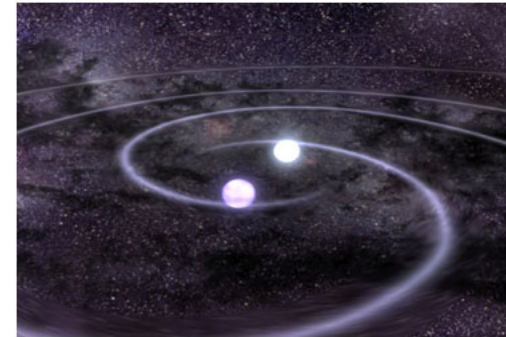
# Can correlated anomaly between r-nuclei & $\nu$ -nuclei be seen in Neutron-Star-Merger ?

## Single Massive Stars (SNe, HNe, Collapsars)



“r-process”  
in  
both Dynamical  
Ejecta

## Neutron-Star Mergers



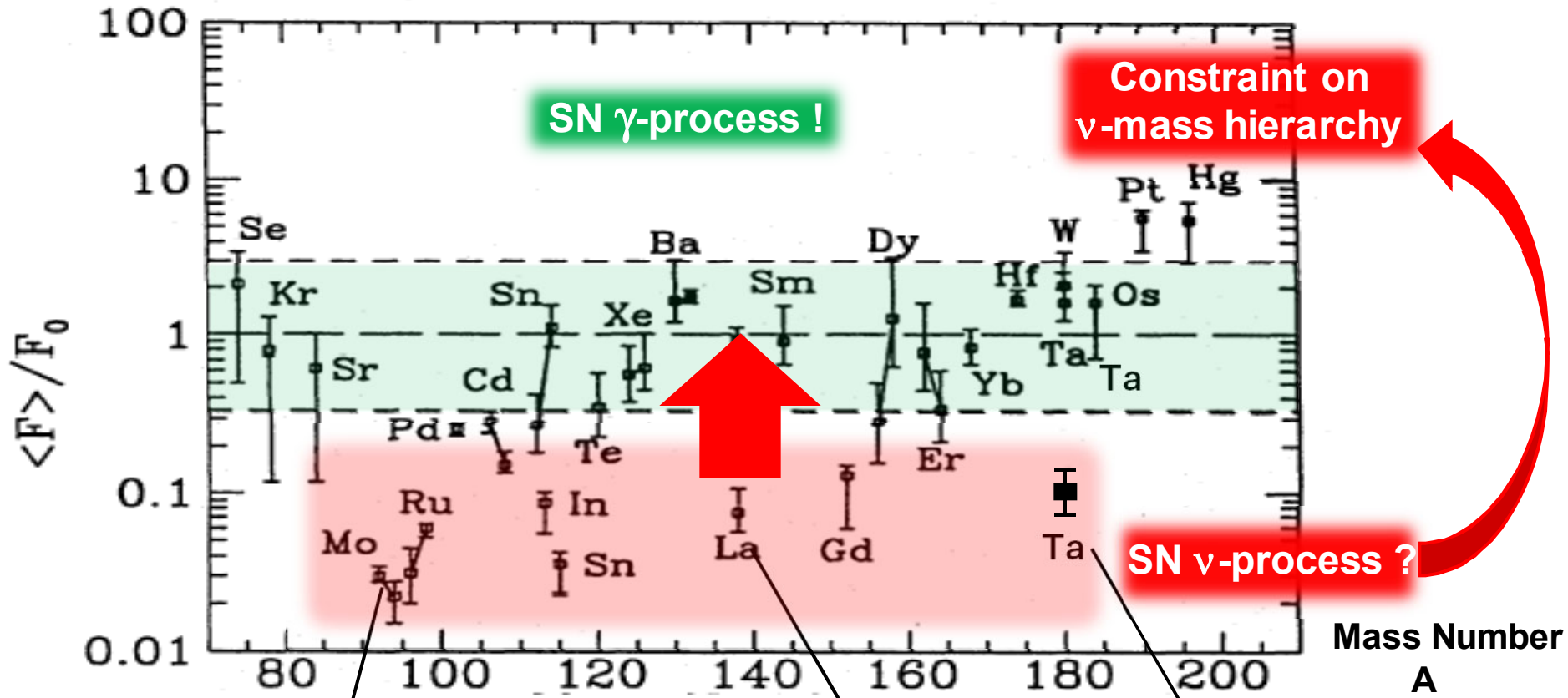
“ $\nu$ -rocess”  
in Outer Layers

**NO !**

# Origin of p-nuclei (n-deficient side) $\rightarrow$ $\gamma$ -process ?

Rare isotopes

Rayet, M., Arnould, M., Hashimoto, M., Prantzos, N., Nomoto, A. & Ap. **298** (1995), 517.  
 M. Arnould Stephane Goriely, Phys. Rep. **384** (2003) 1–84.



**92,94Mo, 96,98Ru**

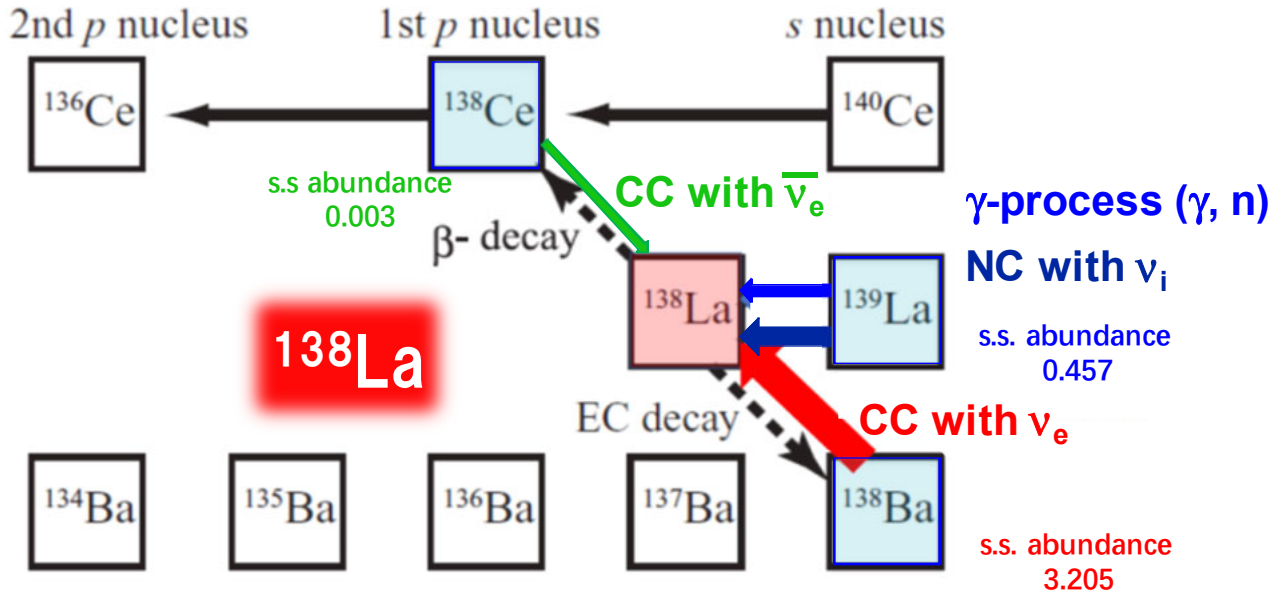
**138La 139La**  
**0.089% 99.91%**

**180Ta 181Ta**  
**0.012% 99.988%**

# Why $^{138}\text{Ba}(\nu, e^-)^{138}\text{La}$ dominates over $^{139}\text{La}(\gamma, n)^{138}\text{La}$ ? 25

*Weak - process*

*EM - process*

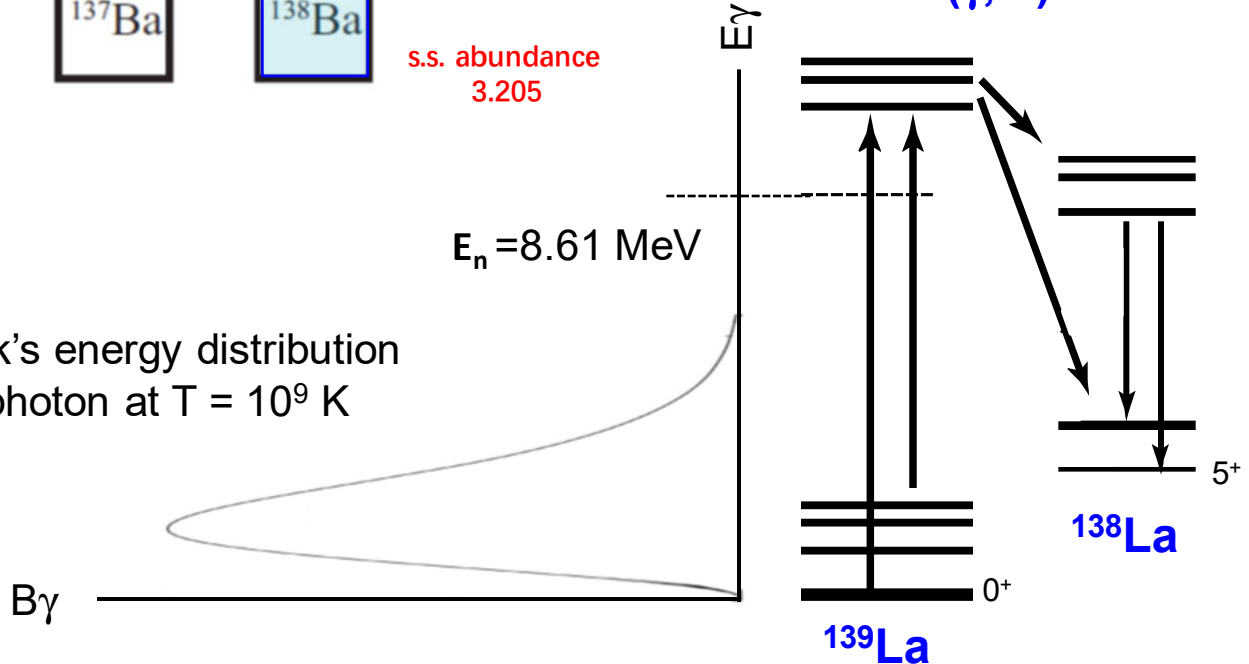


**$^{138}\text{La}$**

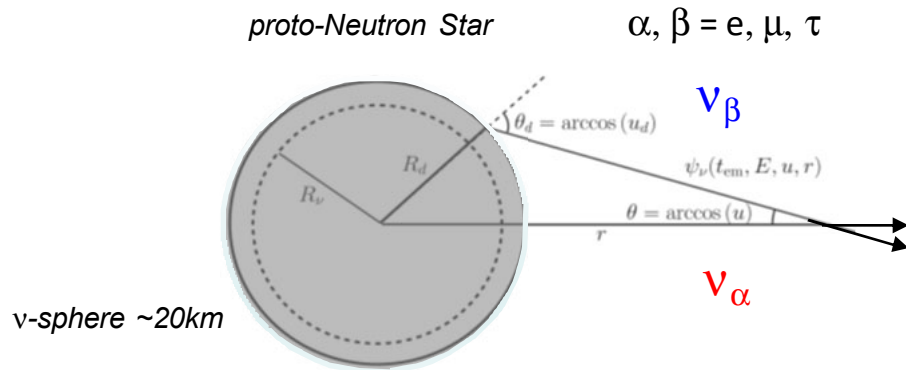
$\gamma$ -process

$^{139}\text{La}(\gamma, n)^{138}\text{La}$

Planck's energy distribution of photon at  $T = 10^9$  K



Balantekin, Pehlivan & Kajino, PR D84 (2011), 065008; PR D90 (2014), 065011; PR D98 (2018), 083002; Duan, Fuller, Carlson & Qian, PRL 97 (2006), 241101; Fogli, Lisi, Marrone & Mirizzi, JCAP 12 (2007) 010; Sasaki, Kajino, Takiwaki, Hayakawa, Balantekin, Pehlivan, PR D96 (2017), 043013; Yao, Kajino, Luo et al. (2025), ApJ 980, 247.



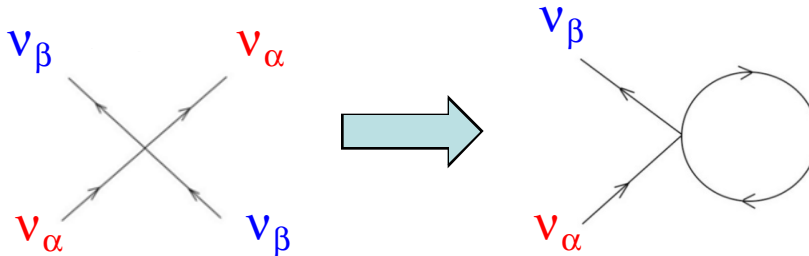
GWS standard model

$$\left\{ \begin{array}{l} i \frac{d\psi_\nu}{dt} = (H_\nu + H_e + H_\nu) \psi_\nu(t_{em}, E, u, r), \\ H_\nu = U \frac{M^2}{2E} U^\dagger, \quad \text{Vacuum} \\ H_e = \sqrt{2} G_F n_e(r) \text{diag}(1, 0, 0), \quad \text{MSW} \end{array} \right.$$

## Collective flavor oscillation in coherent ν-ν scattering

$$H_\nu = \sqrt{2} G_F \sum_\alpha \int \frac{dE' d\Omega' (1 - uu')}{\dots} \left[ \frac{d^2 n_{\nu_\alpha}}{dE' d\Omega'} \rho_{\nu_\alpha}(t'_{em}, E', u', r) - \frac{d^2 n_{\bar{\nu}_\alpha}}{dE' d\Omega'} \rho_{\bar{\nu}_\alpha}^*(t'_{em}, E', u', r) \right]$$

ν angle dep !



Unified Electroweak Theory  
Nobel Prize 1979



Steven Weinberg   Sheldon Glashow   Abdus Salam

10<sup>58</sup> ν' s with 3-flavors & multi-angles !

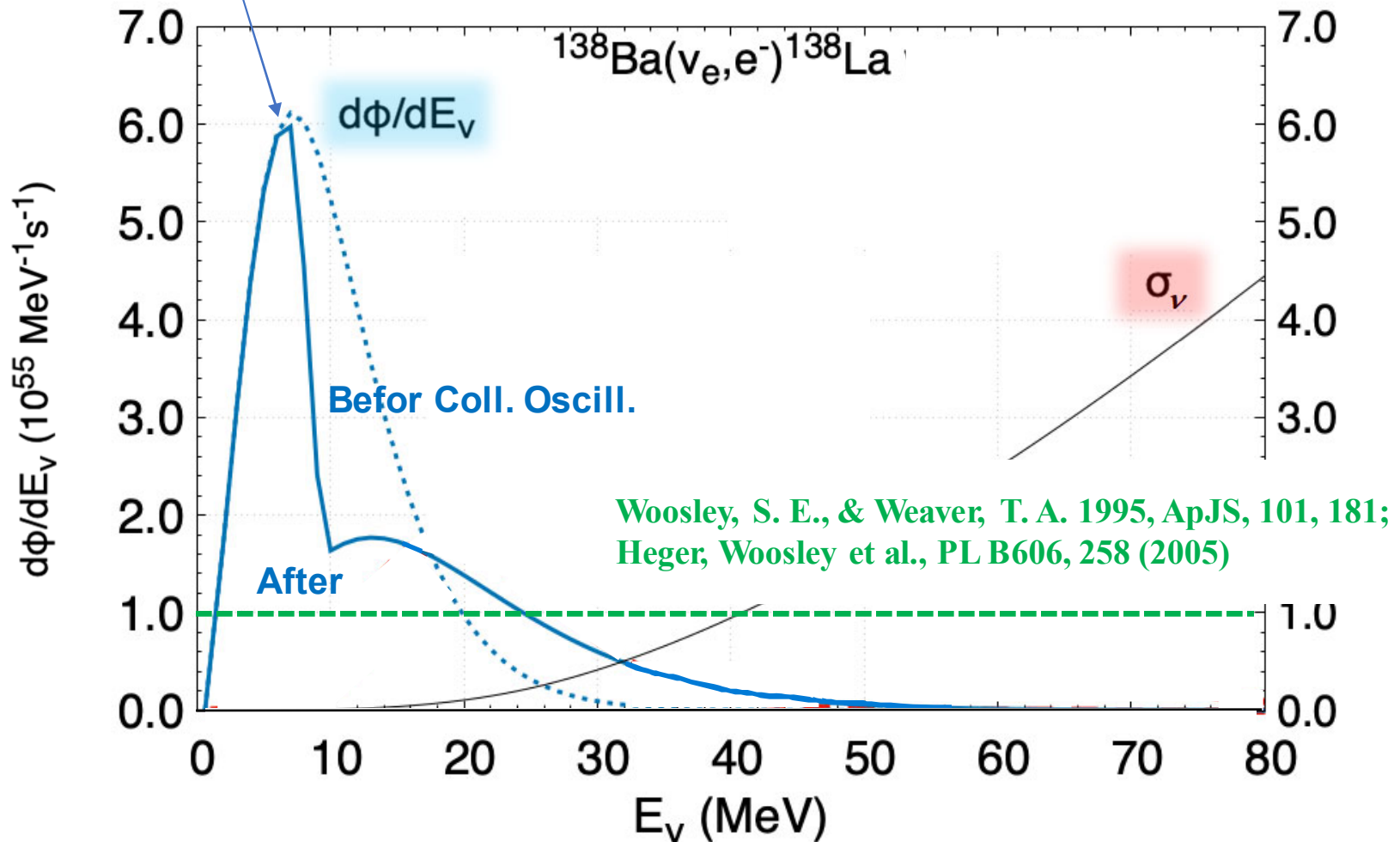
Mean Field Approx.

# $^{138}\text{Ba}(\nu_e, e^-)^{138}\text{La}$

Yao, Kajino, Luo et al. (2025), ApJ 980, 247;  
 Yao, Luo, Kajino, Hayakawa, Yamaguchi, Tang, Gao,  
 Liu (2025), CPC 49, 084003.

$\nu$ -Energy Spectral Change due to  
 Collective Oscill. (Mean-field approx.)

Inverted case



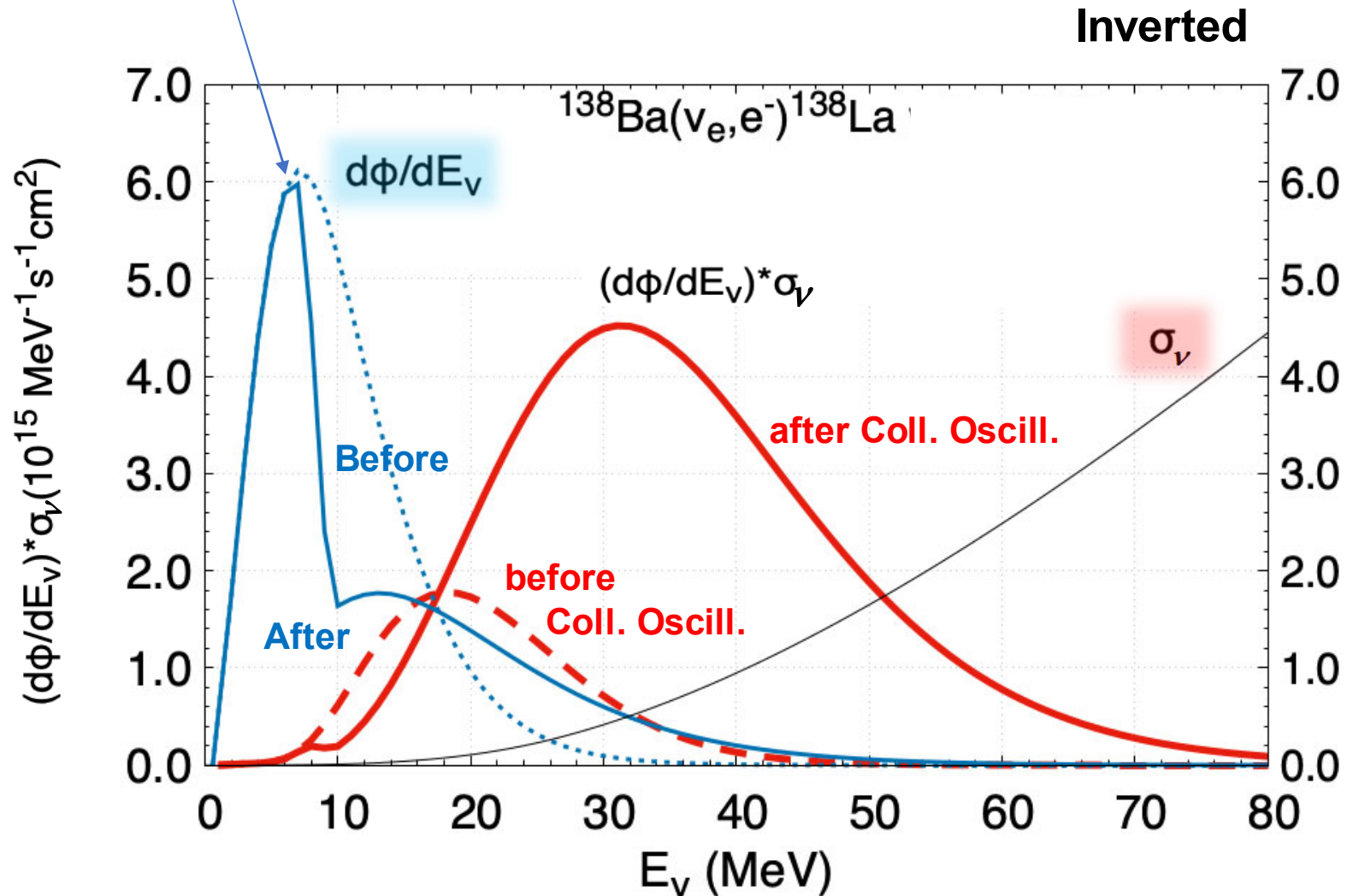


$$dn_{^{138}\text{La}}/dt = \langle d\phi_\nu/dE_\nu \sigma_\nu c \rangle_R n_{^{138}\text{Ba}}$$

$$d\phi_\nu/dE_\nu \propto \nu\text{-spectrum}$$

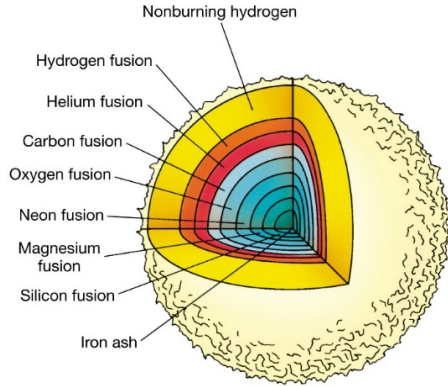
$$\sigma_\nu \propto E_\nu^2$$

$\nu$ -Energy Spectral Change due to Collective Oscill. (Mean-field approx.)



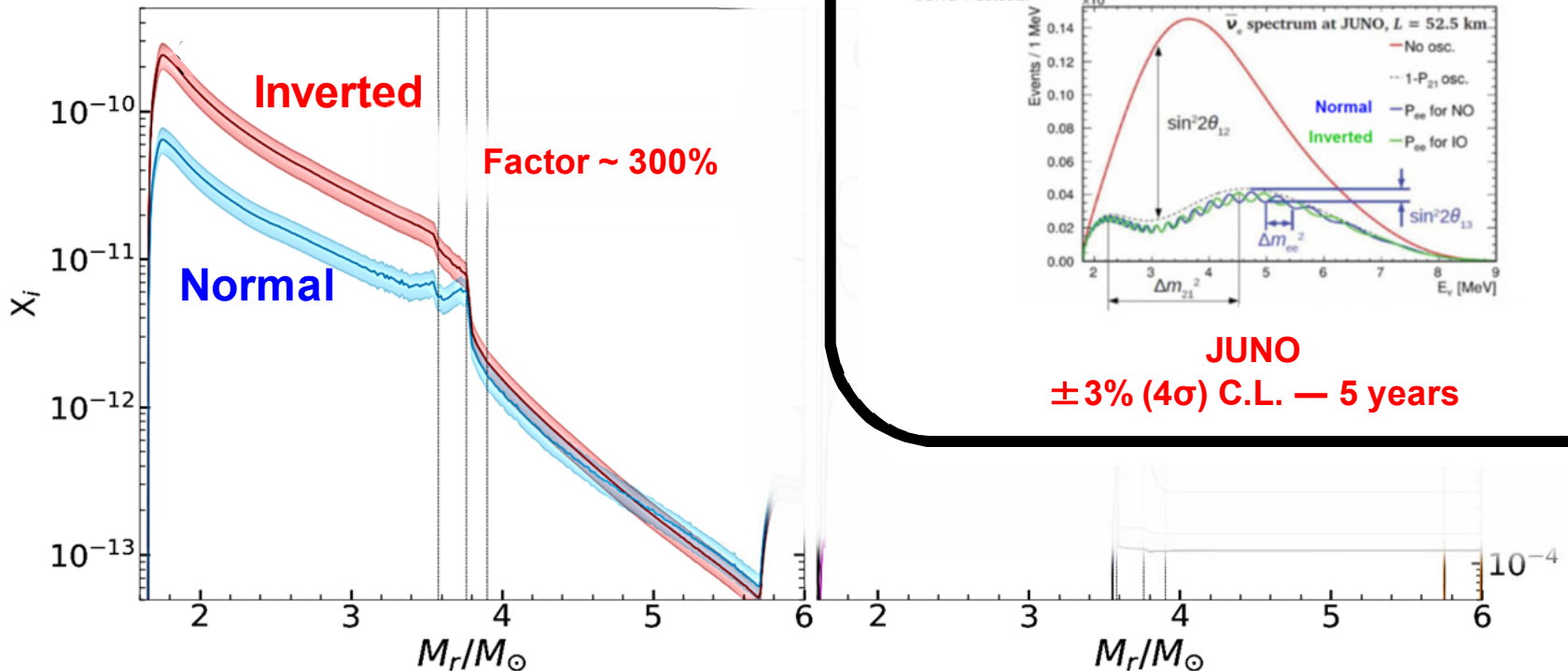
# Calculated Result

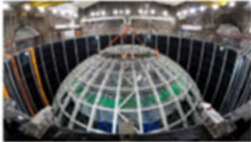
Yao, Kajino, Luo et al. (2025), ApJ 980, 247.  
 Yao, Luo, Kajino, Hayakawa, Yamaguchi, Tang, Gao, Liu (2025), CPC 49, 084003.



Difference between **normal** and **inverted** hierarchy in  $^{138}\text{La}$  is more than **factor of 3 (> 300%)!**

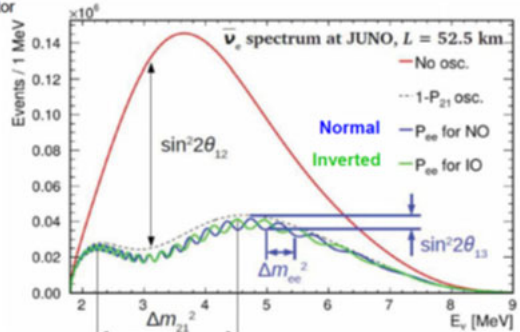
$^{138}\text{La}$





**Jiangmen Underground Neutrino Observatory (JUNO)**  
<http://juno.ihep.cas>

JUNO  $\nu$ -detector



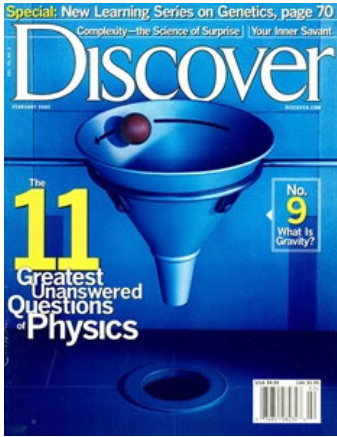
$\nu_e$  spectrum at JUNO,  $L = 52.5$  km.

- No osc.
- - -  $1-P_{21}$  osc.
- $P_{ee}$  for NO (Normal)
- $P_{ee}$  for IO (Inverted)

Annotations:  $\sin^2 2\theta_{12}$ ,  $\Delta m_{21}^2$ ,  $\Delta m_{31}^2$ ,  $\sin^2 2\theta_{13}$ .

**JUNO**  
 $\pm 3\%$  ( $4\sigma$ ) C.L. — 5 years

# 11 Unsolved Mysteries of Physics in the 21st Century



US Academy of Science selected 11 greatest unanswered questions in modern physics:

**Q3 How were the heavy elements made?**

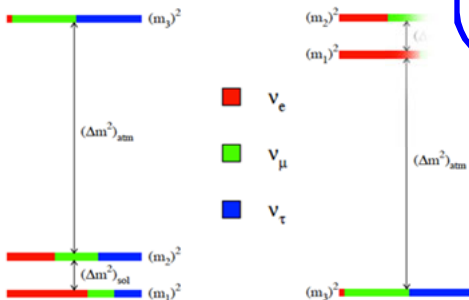
**Q4 Why do neutrinos have mass?**

Finite  $\nu$ -mass, the only unique evidence to go "beyond the standard model".

## Why Neutrinos and Element Genesis?

(1) ~~Mass~~, (2) ~~Hierarchy~~, (3)  ~~$\delta_{CP}$~~  Di  
?

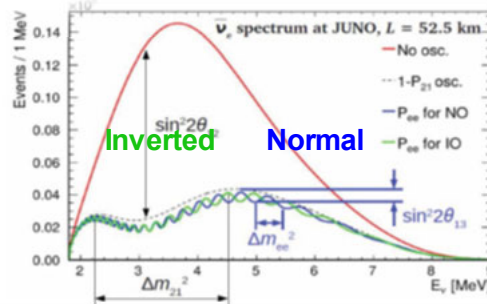
$\sim 0.05$  eV



$$\Delta m_{12}^2 = 7.9 \times 10^{-5} \text{ eV}^2$$

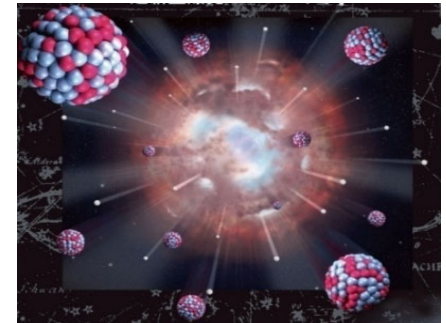
$$|\Delta m_{23}^2| = 2.4 \times 10^{-3} = (0.05 \text{ eV})^2$$

Any observables in flavor oscillations do not depend on  $\delta_{CP}$  when  $E\nu_e < E\bar{\nu}_e < E\nu_\mu, \bar{\nu}_\mu = E\nu_\tau, \bar{\nu}_\tau$ .  
(Yokomakura et al., Phys. Lett. B544, 286)



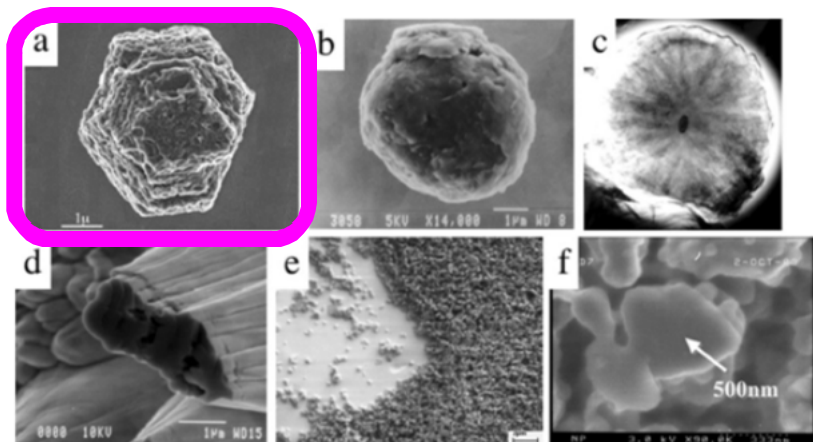
< a few % precision is required!

$\nu$ -oscillations at high density



Supernova:  $E\nu_e < E\bar{\nu}_e < E\nu_\mu = E\nu_\tau$

Factor  $\sim 3$  (300%) sensitivity!



## Pre-solar dust grains scanning e-micrographs

E. Zinner (2008), **Meteorite Scientist**

(a) **Silicon-carbide**

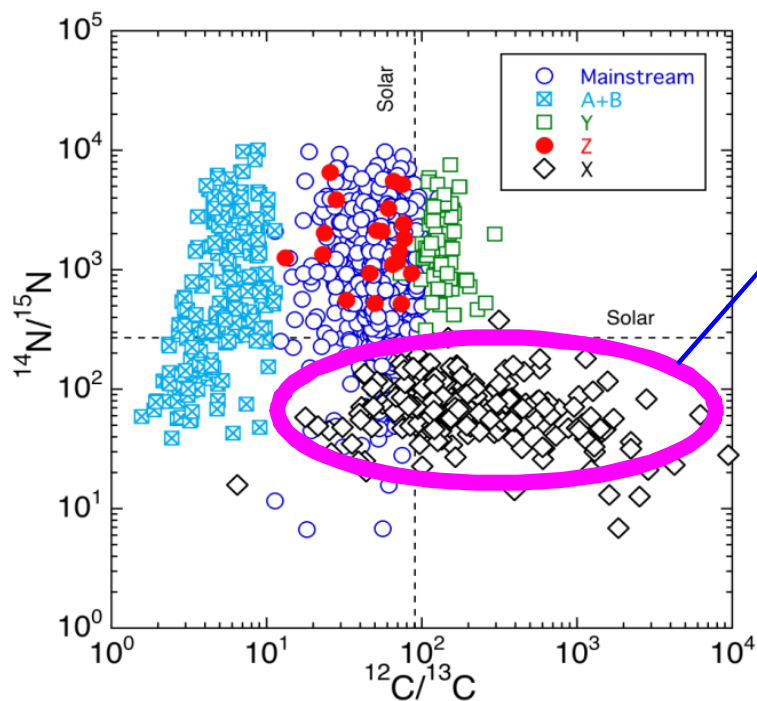
(b) Graphite,

(c) Graphite slice with inner TiC grain,

(d) Aluminum oxide, (e) Spinel, (f) Silicate

## Characteristics of SiC X-Grains

- Enhanced  $^{12}\text{C}$  ( $^{12}\text{C}/^{13}\text{C} > \text{Solar}$ )
- Enhanced  $^{28}\text{Si}$  ( $^{28}\text{Si}/^{29,30}\text{Si} > \text{Solar}$ )
- Decay of  $^{26}\text{Al}$  ( $t_{1/2}=7 \times 10^5 \text{yr}$ ),  $^{44}\text{Ti}$  ( $t_{1/2}=60 \text{yr}$ )
- Deficient  $^{14}\text{N}$  ( $^{14}\text{N}/^{15}\text{N} < \text{Solar}$ )



## Probe of SN $\nu$ -Flavor Oscillations

### MSW effect:

Mathews, Kajino, Aoki & Fujiya, PR D85, 105023 (2012),  
Kajino, Mathews, Hayakawa, J. Phys. G41 (2014), 044007

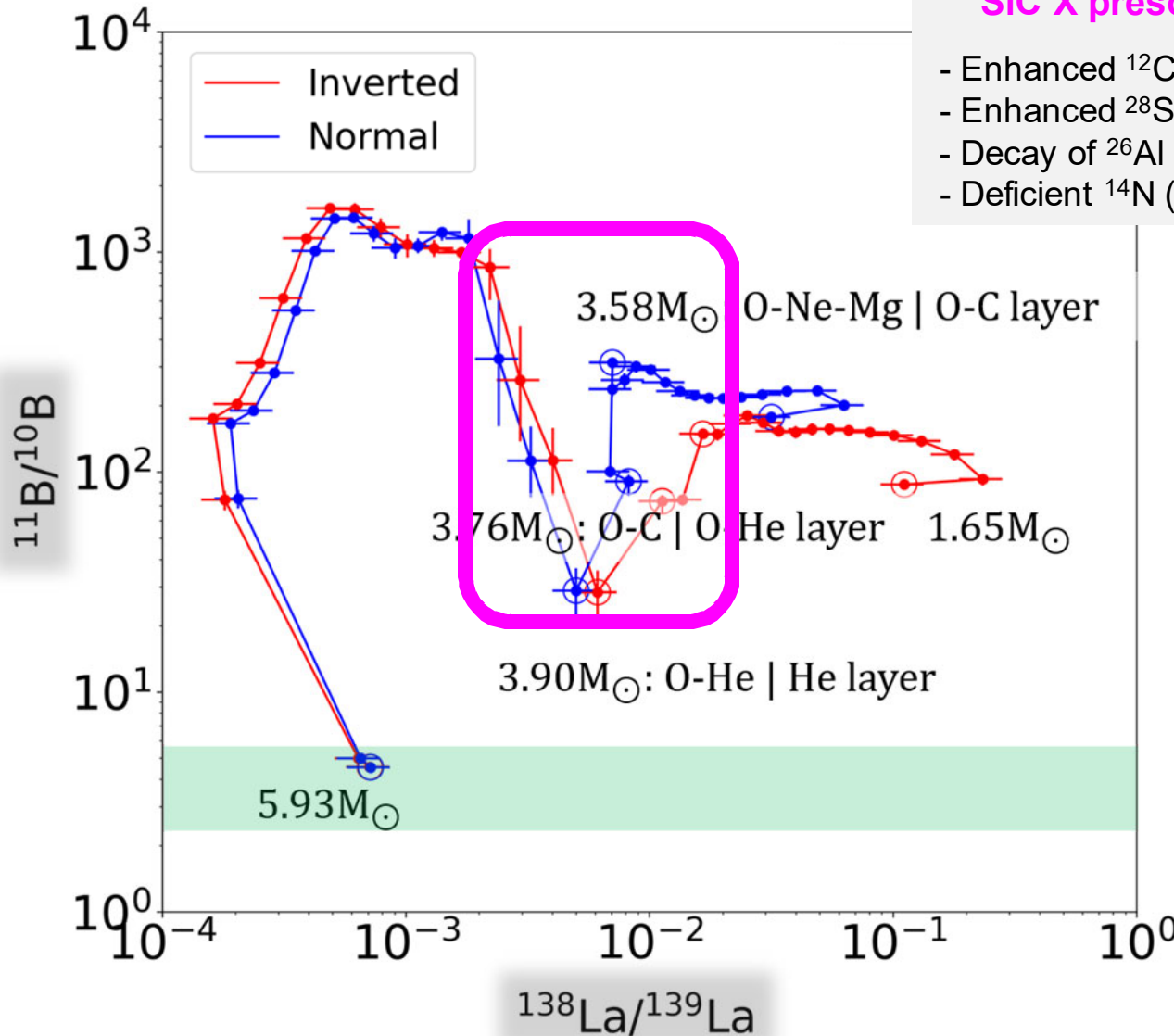
### Collective + MSW effects:

Yao, Kajino, Luo, et al., ApJ 980, 247 (2025)

# Obs. Test — SN grain (SiC X)

Yao, Kajino, Luo et al. (2025), ApJ 980, 247.  
Yao, Luo, Kajino et al. (2025), CPC 49, v9.  
Luo, He, Kajino et al. (2026), to be submit.

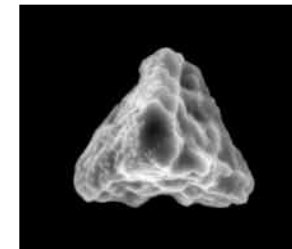
## Isotopic Correlation $^{138}\text{La}/^{139}\text{La}$ vs. $^{11}\text{B}/^{10}\text{B}$



### SiC X presolar grains → SN grain

- Enhanced  $^{12}\text{C}$  ( $^{12}\text{C}/^{13}\text{C} > \text{Solar}$ )
- Enhanced  $^{28}\text{Si}$  ( $^{28}\text{Si}/^{29,30}\text{Si} > \text{Solar}$ )
- Decay of  $^{26}\text{Al}$  ( $t_{1/2}=7\times 10^5\text{yr}$ ),  $^{44}\text{Ti}$  ( $t_{1/2}=60\text{yr}$ )
- Deficient  $^{14}\text{N}$  ( $^{14}\text{N}/^{15}\text{N} < \text{Solar}$ )

SiC-X grains (SN grains),  
largely mixed with  
ISM (~ solar composition)



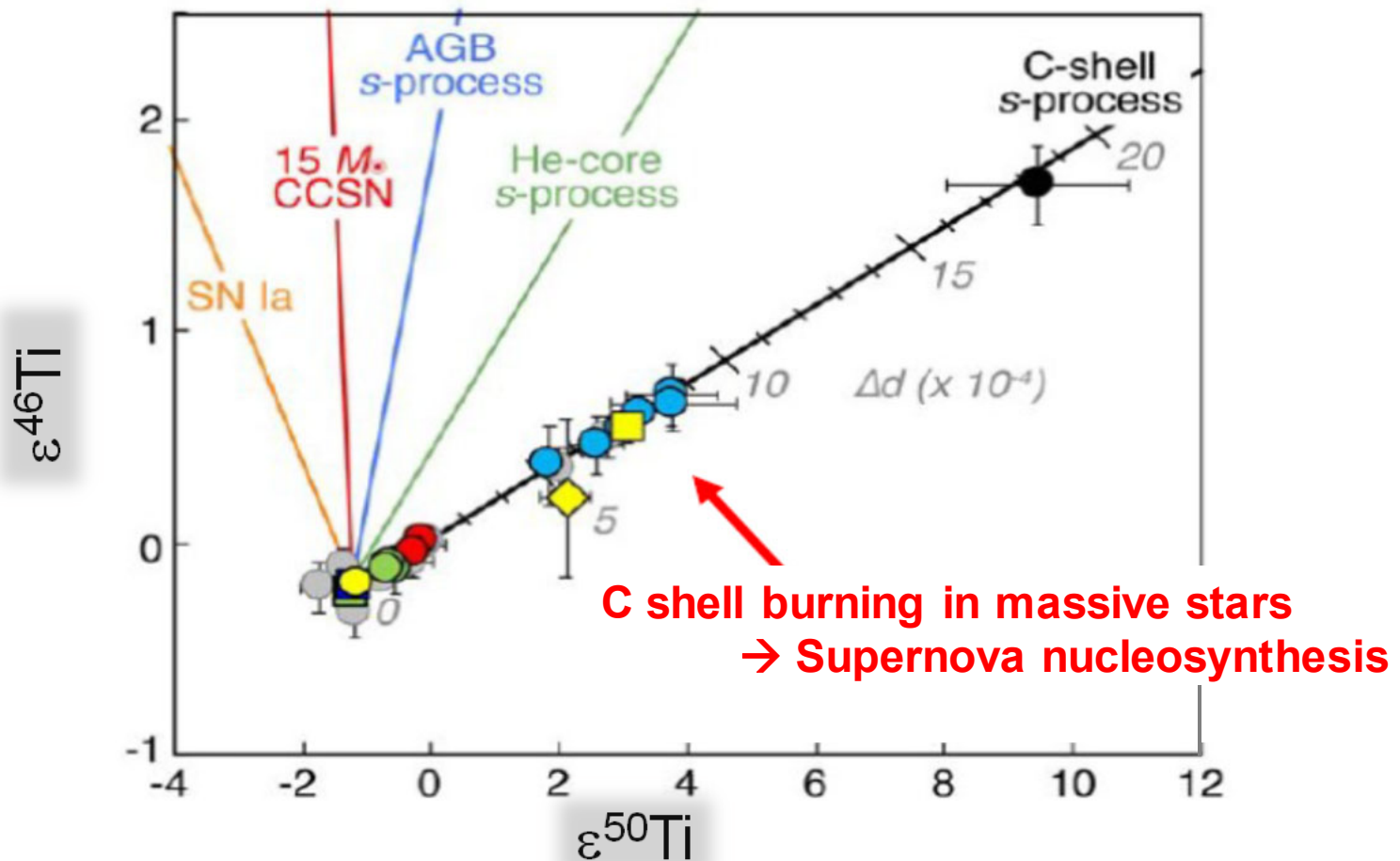
Fujiya, Hoppe, Ott, ApJ 730 (2011), L7; Hoppe, Lodders, Streb, et al., ApJ 551 (2001), 478.

## Obs. Test No. 2 — CAIs

Luo, Yao, Kajino, Hayakawa, et al. (2026),  
to be submitted.

## $\delta\text{Ti} - \delta\text{La}$ Correlation in Ca-Al rich Inclusions (CAIs)

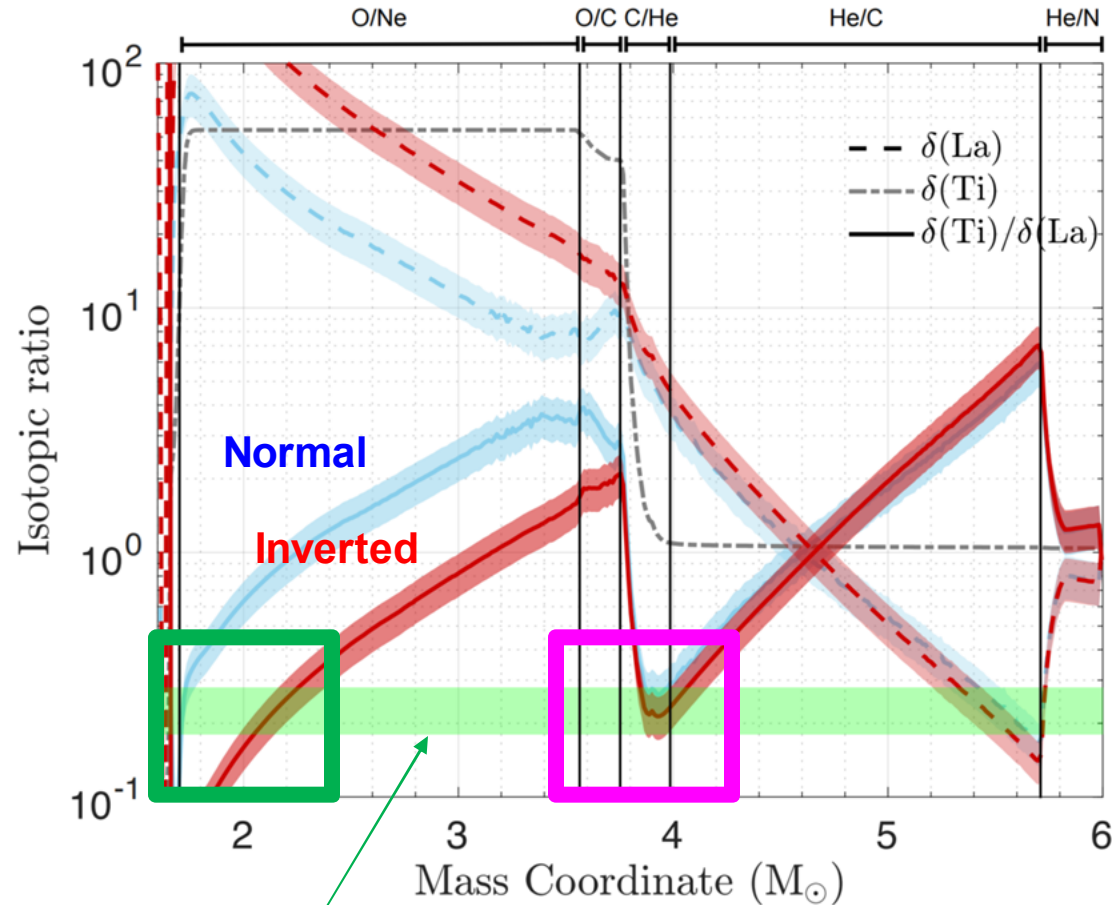
T. Iizuka, et al. ApJL 979 (2025), L29.



# Calculated $\delta\text{Ti} - \delta\text{La}$ correlation

Luo, Yao, Kajino, Hayakawa, et al. (2026),  
to be submitted.

Comparison between measurement and model



$$\delta(\text{Ti}) \equiv f(\text{Ti}) \frac{({}^{50}\text{Ti}/{}^{48}\text{Ti})_{\text{SN}}}{({}^{50}\text{Ti}/{}^{48}\text{Ti})_{\odot}}$$

$$f(\text{Ti}) = \frac{X_{\text{SN}}(\text{Ti}) \cdot m_{\text{eject}}}{X_{\text{CAI}}(\text{Ti})_{\text{CAI}} \cdot m_{\text{CAI}}}$$

$$\delta(\text{La}) \equiv f(\text{La}) \frac{({}^{138}\text{La}/{}^{139}\text{La})_{\text{SN}}}{({}^{138}\text{La}/{}^{139}\text{La})_{\odot}}$$

$\delta(\text{Ti})/\delta(\text{La})$  under **normal** and **inverted hierarchies**

Green band is the coefficient of correlation.

## 1. Cosmic & Galactic Chem. Evolution

- **Single Massive Stars (MHDJ SNe & Collapsars)** dominate r-process over the cosmic evolution, while NSMs come later. → **More astronomical observations, required.**

## 2. Origin of r-process Nuclei and Roles of Fission

- **Fission** takes the key in different **A-distribution** among MHDJ SN, Collapsars, and NSMs.
  - **Fission Fragment Distribution, required !**
  - **Consistency with Mass Model (DDFT), desirable !**
- r-, i- and s-processes can coexist in Collapsar nucleosynthesis.
  - **Fission neutrons and (n,  $\gamma$ ) rates, required !**

**Collaboration between Fission Physics and Astrophys., highly desirable !**

## 3. Origin of $\nu$ -process Nuclei

- SN  $\nu$ / $\nu p$ -process could be a sensitive probe to **constrain still unknown  $\nu$ -mass hierarchy.**
  - **Meteoritic anomaly search, required!**
  - **Nuclear-weak & (n, p) rates (GT + forbidden), required !**