







Halo nuclei from *ab initio* nuclear theory

International Symposium Commemorating the 40th Anniversary of the Halo Nuclei (HALO-40)

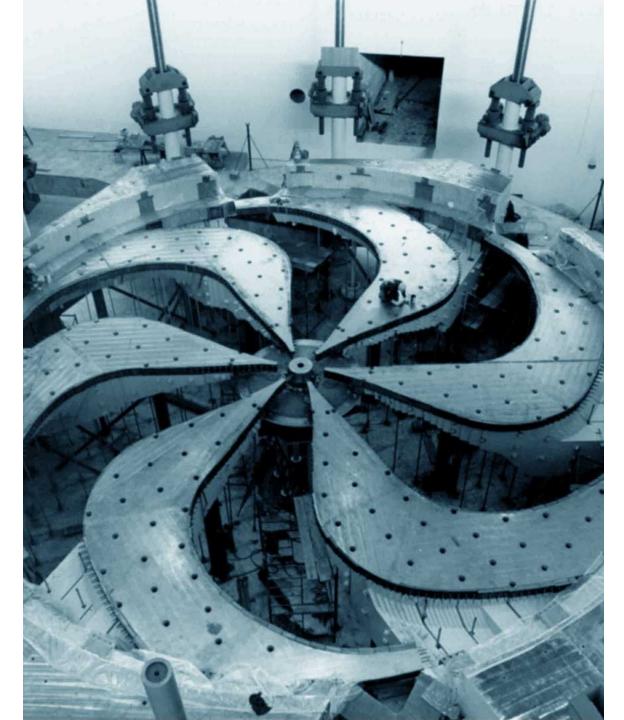
Beijing, October 12-18, 2025

Petr Navratil

TRIUMF

Collaborators:

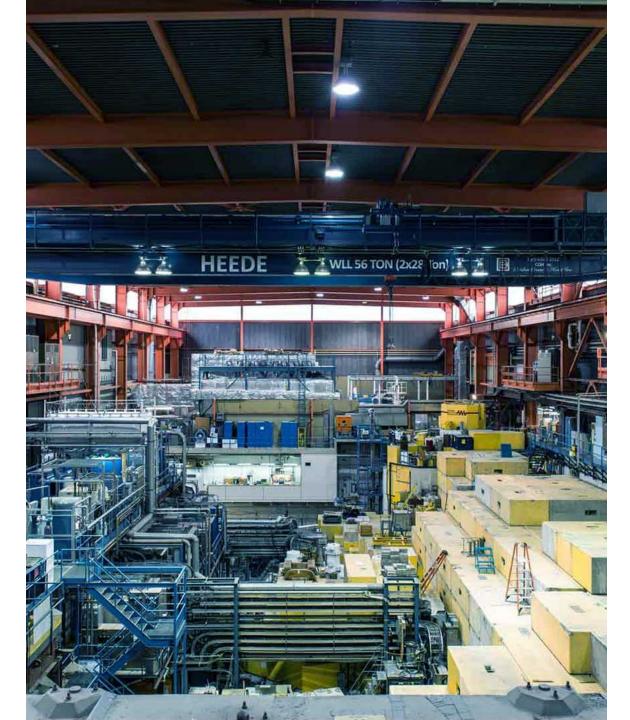
Sofia Quaglioni (LLNL), Kostas Kravvaris (LLNL), Guillaume Hupin (IJCLab), Michael Gennari (Mainz),



Outline

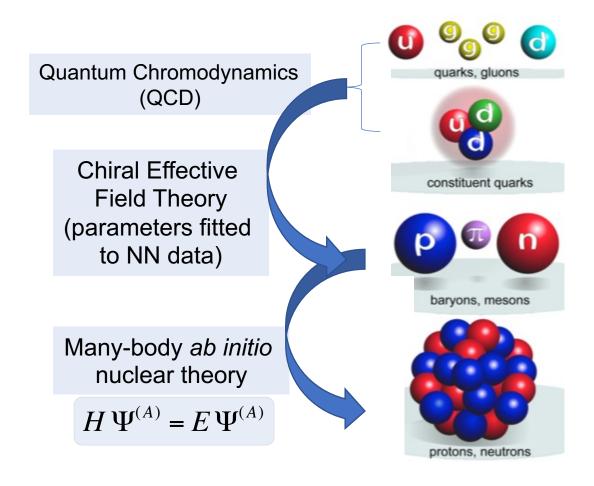
- Introduction Ab initio nuclear theory no-core shell model with continuum (NCSMC)
- Parity inversion in ¹¹Be ground state
- Halo ground state of ¹⁵C
- P-wave halo ground state of ⁸B & radiative capture of protons on ⁷Be
- NCSMC for three-body cluster ⁶He ~ ⁴He + n + n
- ¹¹Li within NCSM (prerequisite for ¹¹Li ~ ºLi + n + n)
- Conclusions

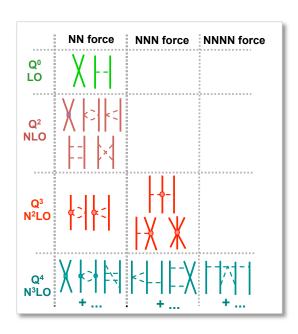
Ab initio nuclear theory no-core shell model with continuum (NCSMC)



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First principles or ab initio nuclear theory





Contents lists available at Sciverse ScienceDirect

Progress in Particle and Nuclear Physics





Conceptually simplest ab initio method: No-Core Shell Model (NCSM)

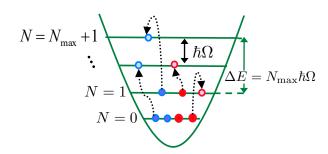
- Basis expansion method (CI)
 - Harmonic oscillator (HO) basis truncated in a particular way (N_{max})
 - Why HO basis?
 - Lowest filled HO shells match magic numbers of light nuclei (2, 8, 20 – ⁴He, ¹⁶O, ⁴⁰Ca)
 - Equivalent description in relative(Jacobi)-coordinate and Slater determinant basis – nuclei self-bound, [H,P_{CM}]=0
 - Exact factorization of CM and intrinsic eigenfunctions at each N_{max}
- Good for well-bound states, approximation of weakly-bound states and narrow resonances

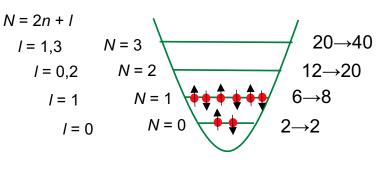


Ab initio no core shell model

Bruce R. Barretta, Petr Navrátilb, James P. Varyc.*

5





$$E = (2n + l + \frac{3}{2})\mathfrak{h}\Omega$$

No-Core Shell Model with Continuum (NCSMC)

$$\Psi^{(A)} = \sum_{\lambda} c_{\lambda} \left| \stackrel{(A)}{\bullet} , \lambda \right\rangle + \sum_{\nu} \int d\vec{r} \ \gamma_{\nu}(\vec{r}) \ \hat{A}_{\nu} \left| \stackrel{r}{\bullet} , \nu \right\rangle$$

No-Core Shell Model with Continuum (NCSMC)

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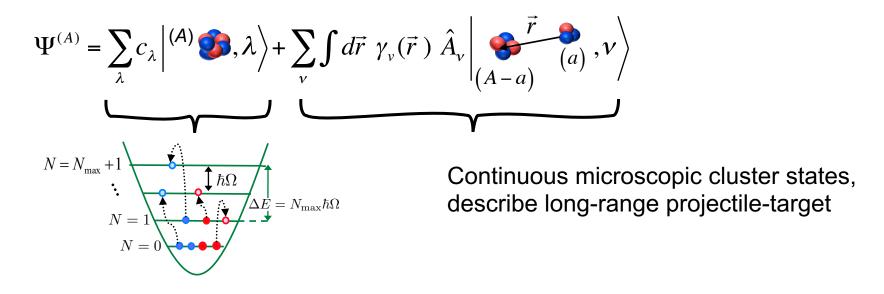
$$N = N_{\text{max}} + 1$$

$$N = 1$$

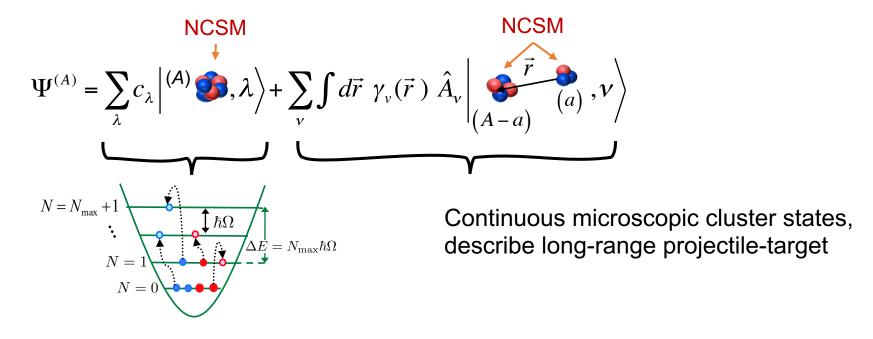
$$N = 0$$

$$N = 0$$

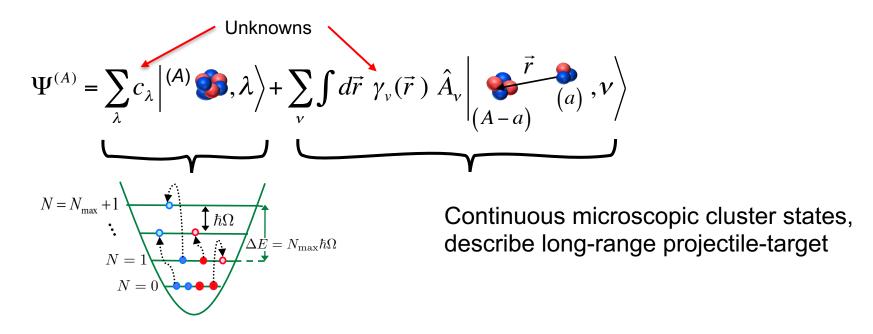
No-Core Shell Model with Continuum (NCSMC)



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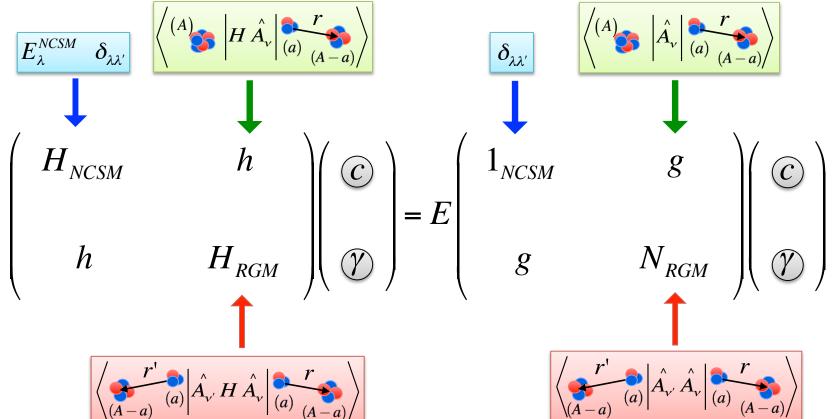
No-Core Shell Model with Continuum (NCSMC)



Coupled NCSMC equations

$$H \Psi^{(A)} = E \Psi^{(A)}$$

$$\Psi^{(A)} = \sum_{\lambda} c_{\lambda} | \stackrel{(A)}{\bullet} , \lambda \rangle + \sum_{\nu} \int d\vec{r} \gamma_{\nu}(\vec{r}) \hat{A}_{\nu} | \stackrel{\vec{r}}{\bullet} \stackrel{(a)}{\bullet} , \nu \rangle$$



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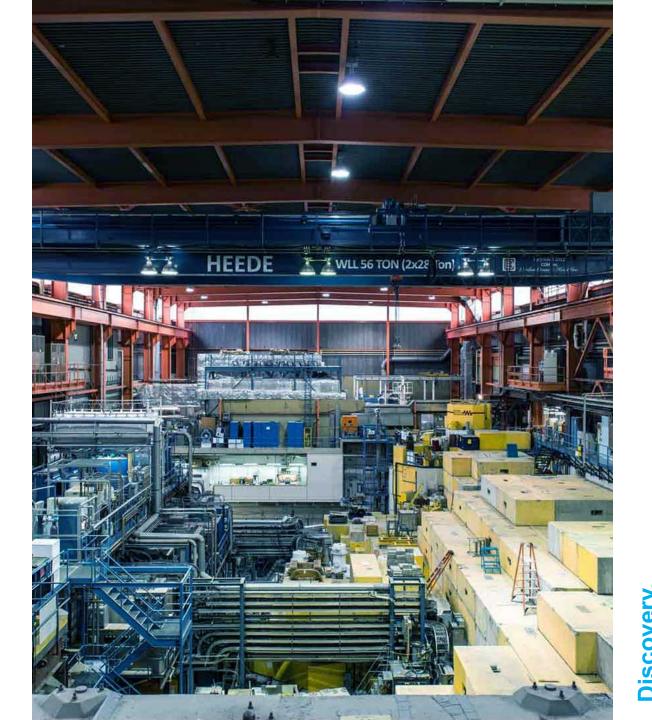
doi:10.1088/0031-8949/91/5/0530

Invited Comme

Unified *ab initio* approaches to nuclear structure and reactions



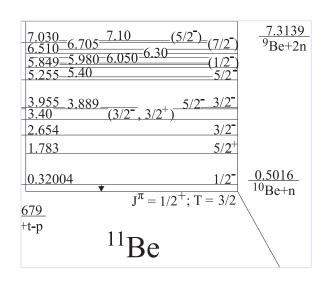
Parity inversion in ¹¹Be ground state



Neutron-rich halo nucleus ¹¹Be

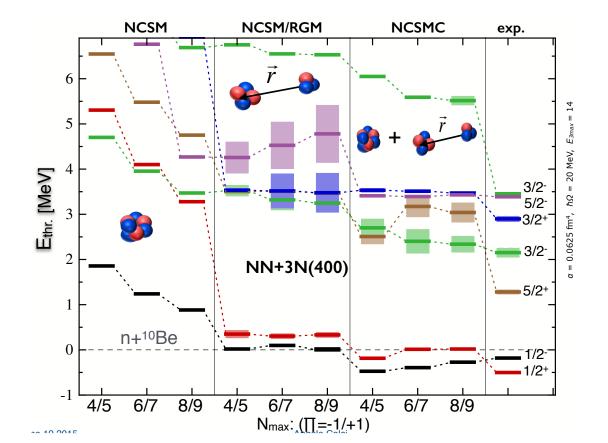
- Z=4, N=7
 - In the shell model picture g.s. expected to be $J^{\pi}=1/2^{-1}$
 - Z=6, N=7 ¹³C and Z=8, N=7 ¹⁵O have J^π=1/2 g.s.
 - In reality, ¹¹Be g.s. is **J**π**=1/2**+ parity inversion
 - Very weakly bound: E_{th}=-0.5 MeV
 - Halo state dominated by ¹⁰Be-n in the S-wave
 - The 1/2- state also bound only by 180 keV
- Can we describe ¹¹Be in ab initio calculations?
 - Continuum must be included
 - Does the 3N interaction play a role in the parity inversion?

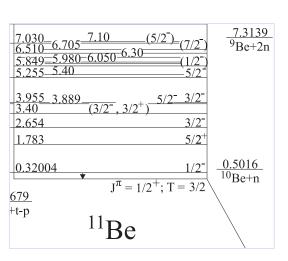




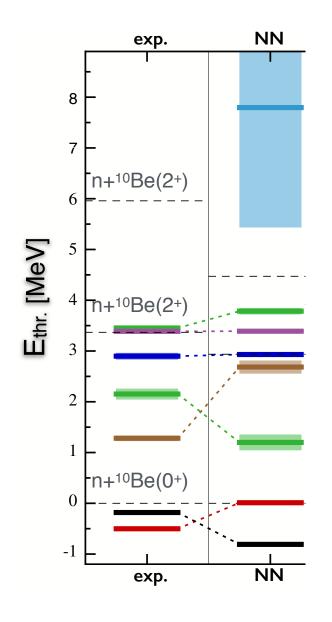
Structure of ¹¹Be from chiral NN+3N forces

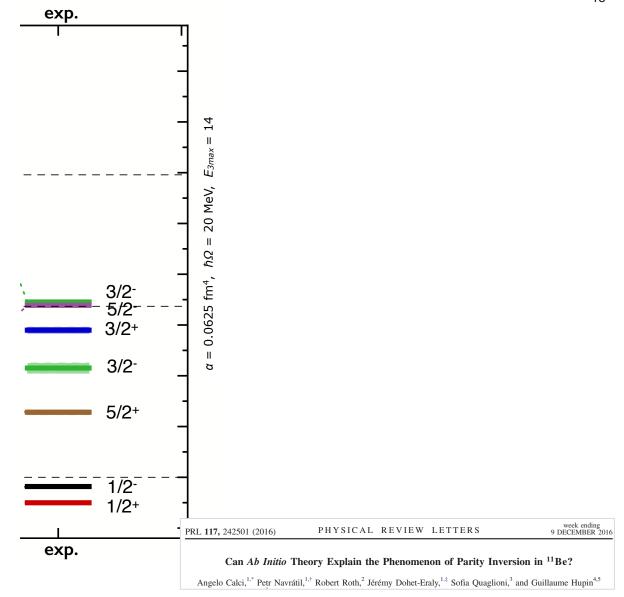
- NCSMC calculations including chiral 3N (NN N³LO+N²LO 3N(400), N²LO_{sat}, NN N⁴LO+3N_{InI})
 - -10Be + 11Be
 - ¹⁰Be: 0+, 2+, 2+ NCSM eigenstates
 - ¹¹Be: \geq 6 π = -1 and \geq 3 π = +1 NCSM eigenstates

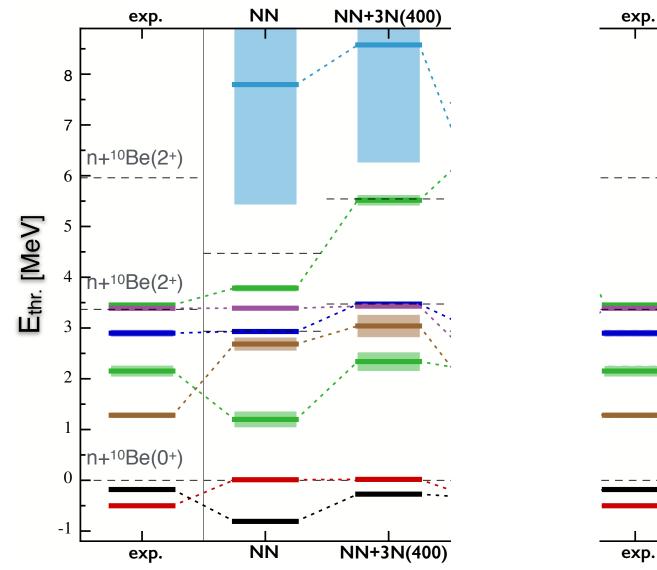


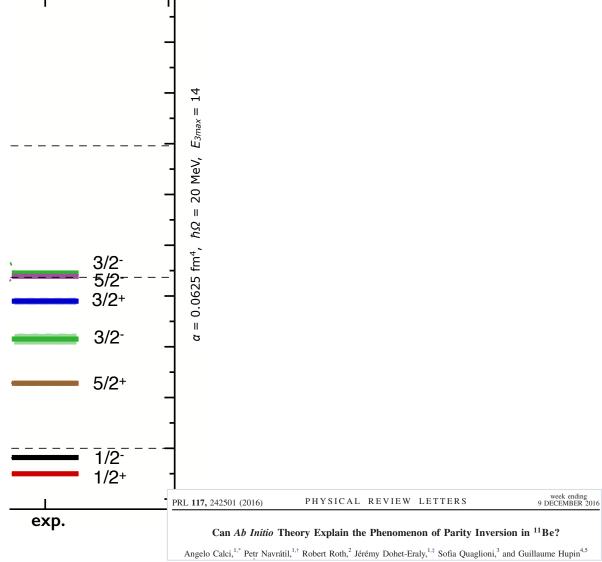


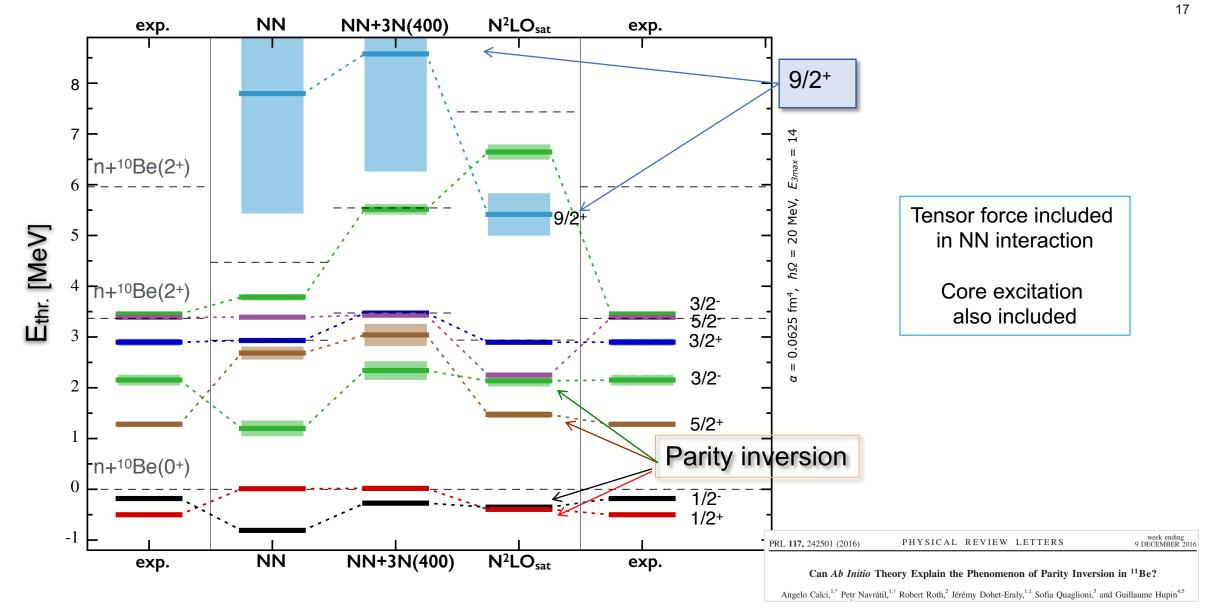




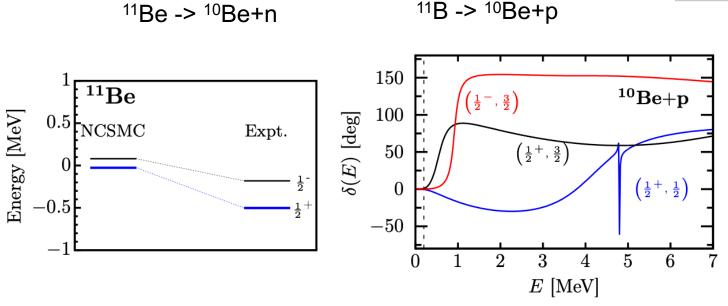




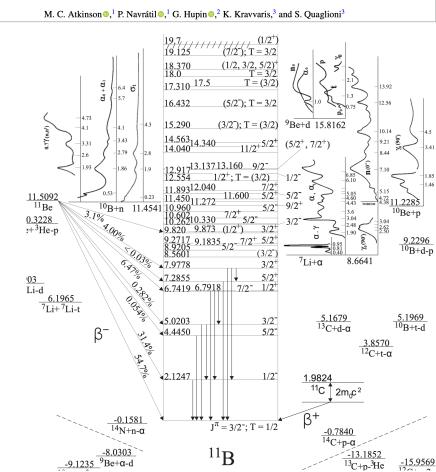








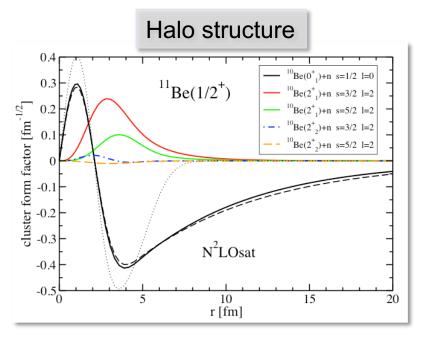
Parity inversion reproduced

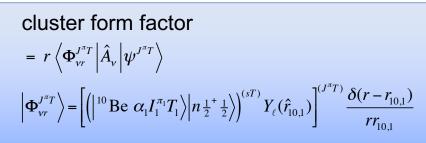


PHYSICAL REVIEW C 105, 054316 (2022)

Ab initio calculation of the β decay from ¹¹Be to a ¹⁰Be + p resonance

Photo-disassociation of ¹¹Be





PRL 117, 242501 (2016)

PHYSICAL REVIEW LETTERS

9 DECEMBER 2016

Can Ab Initio Theory Explain the Phenomenon of Parity Inversion in ¹¹Be?

Angelo Calci,^{1,*} Petr Navrátil,^{1,†} Robert Roth,² Jérémy Dohet-Eraly,^{1,‡} Sofia Quaglioni,³ and Guillaume Hupin^{4,5}

Bound to bound	NCSM	NCSMC-phenom	Expt.
B(E1; $1/2^+ \rightarrow 1/2^-$) [$e^2 \text{ fm}^2$]	0.0005	0.117	0.102(2)

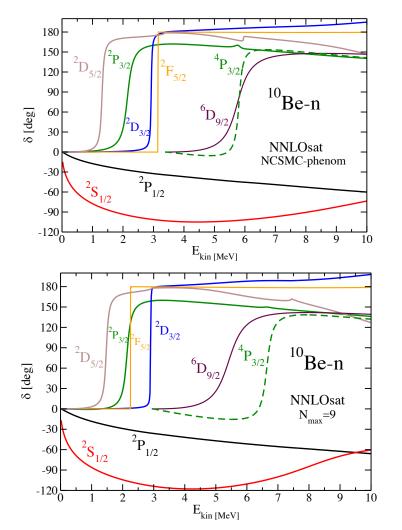
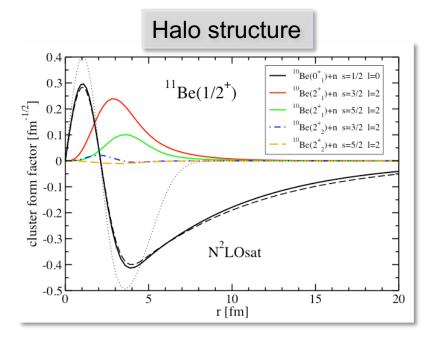
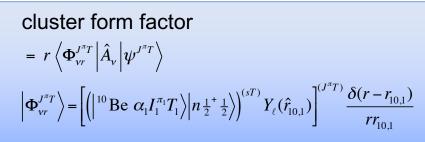


Photo-disassociation of ¹¹Be





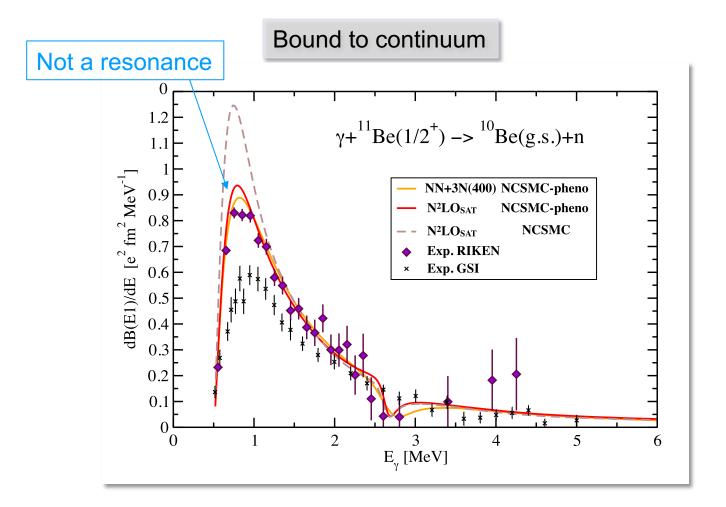
PRL 117, 242501 (2016) PHYSICAL REVIEW LETTERS

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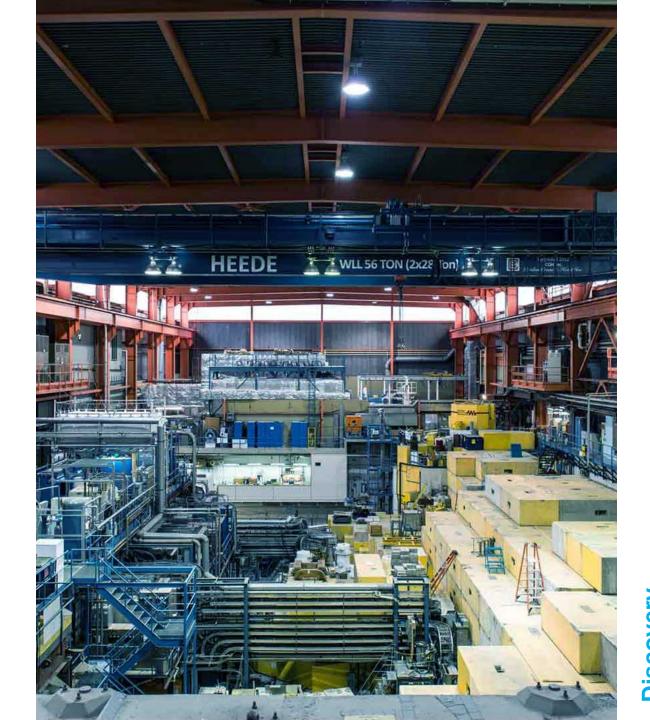
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Halo ground state of ¹⁵C

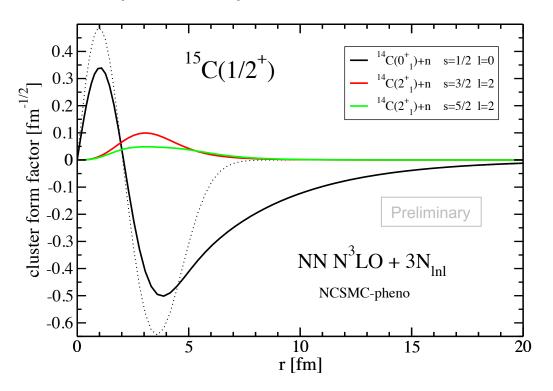


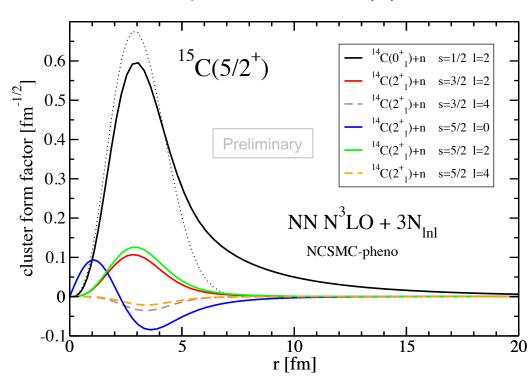
NCSMC application to 15 C \sim 14 C + n – cluster form factor calculations

4.66 3/24.220 5/2
3.103 1/2
0.740 5/2+ $\sqrt{\frac{3\pi_{*1/2}}{1=3/2}}$ 1.21809 $\sqrt{\frac{1.21809}{14}}$ 1.5 C

- 1/2⁺ S-wave and 5/2⁺ D-wave Asymptotic Normalization Coefficients
 - $C_{1/2+}$ = 1.282 fm^{-1/2} compare to Moschini & Capel inferred from transfer data: 1.26(2) fm^{-1/2}
 - $C_{5/2+} = 0.048 \text{ fm}^{-1/2}$

- 0.056(1) fm^{-1/2}
- Spectroscopic factors: 0.96 for 1/2+ and 0.90 for 5/2+ experiments 0.95(5) and 0.69, resp.

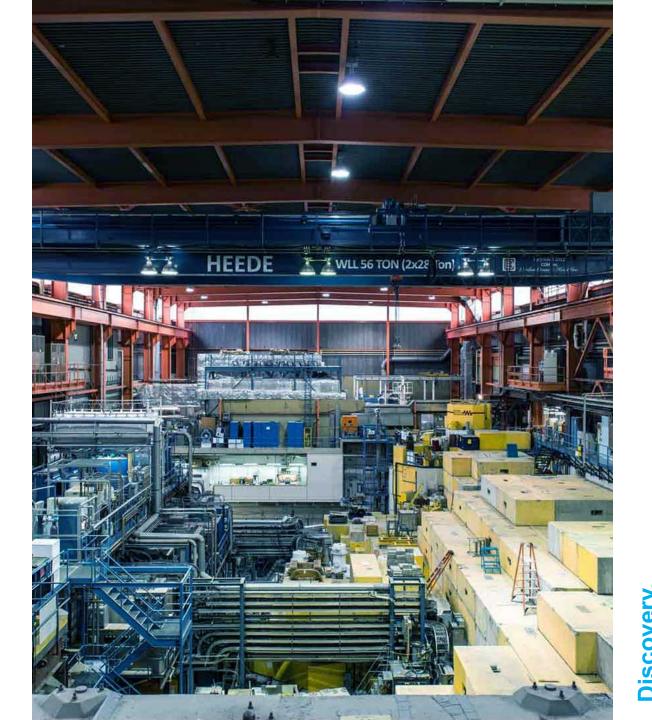


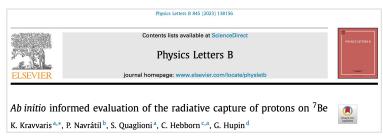


P-wave halo ground state of 8B

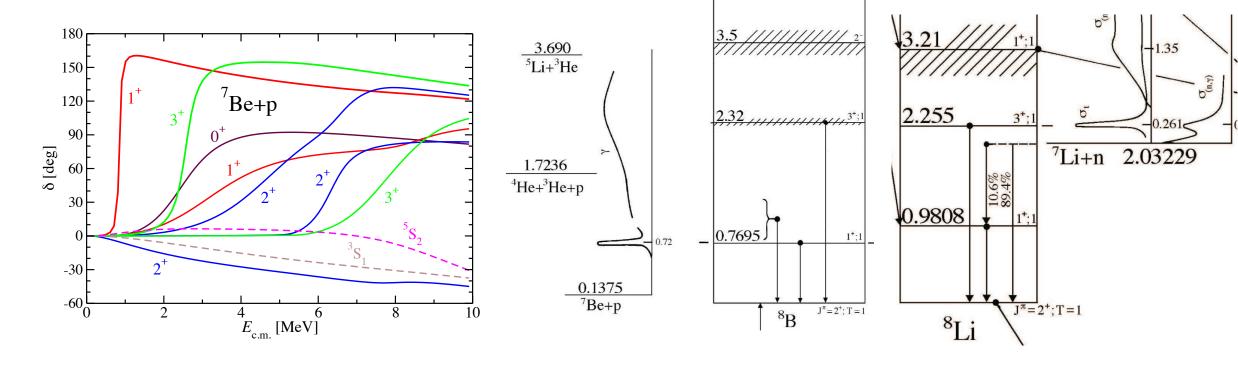
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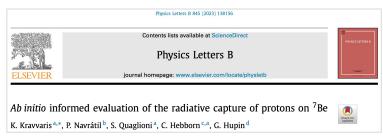
radiative capture of protons on ⁷Be



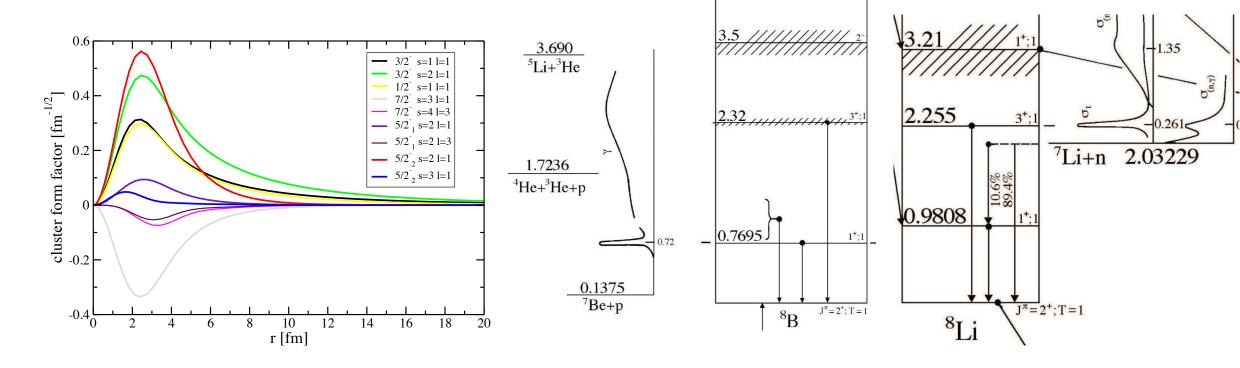


- Solar pp chain reaction, solar ⁸B neutrinos
- NCSMC calculations with a set of chiral NN+3N interactions as input
- Example of ⁸B structure results

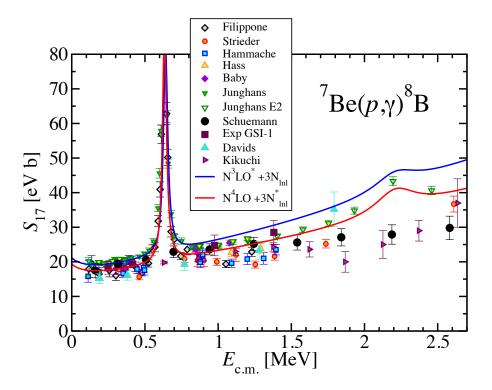




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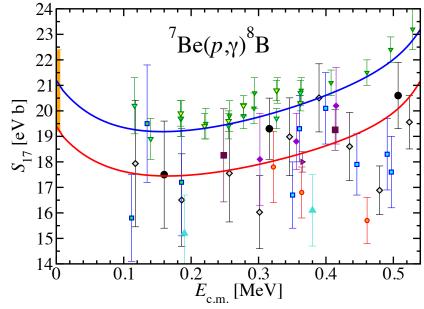


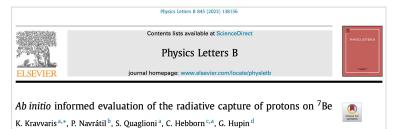
NCSMC S-factor results



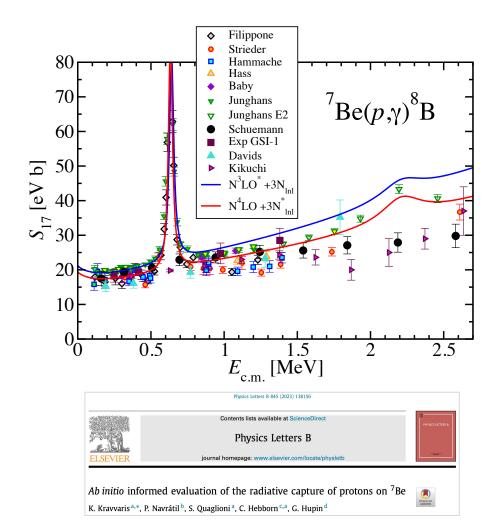
E1 non-resonant, M1/E2 at 1⁺ and 3⁺ resonances

	$C_{p_{1/2}}$	$C_{p_{3/2}}$	a_1	a_2	$S_{17}(0)$
N^2LO+3N_{lnl}	0.384	0.691	4.4(1)	-0.5(1)	23.9
$N^3LO+3N_{\rm lnl}$	0.390	0.678	1.3(1)	-4.7(1)	23.5
$N^4LO + 3N_{\rm lnl}$	0.354	0.669	1.6(1)	-4.4(1)	22.0
$N^4LO+3N^*_{lnl}$	0.343	0.621	1.3(1)	-5.0(1)	19.3
$N^3LO^* + 3N_{\rm lnl}$	0.334	0.663	0.1(1)	-7.7(1)	21.1
$N^3LO^* + 3N_{loc}$	0.308	0.584	2.5(1)	-3.6(2)	16.8
Ref. [41]	0.315(9)	0.66(2)	$17.34^{+1.11}_{-1.33}$	$-3.18^{+0.55}_{-0.50}$	

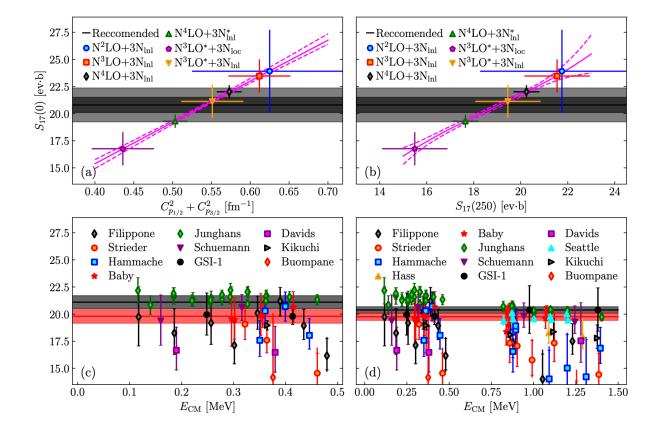




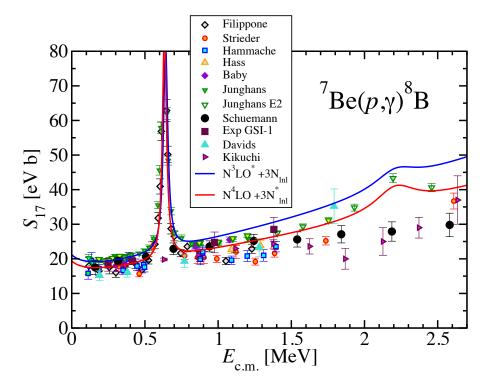
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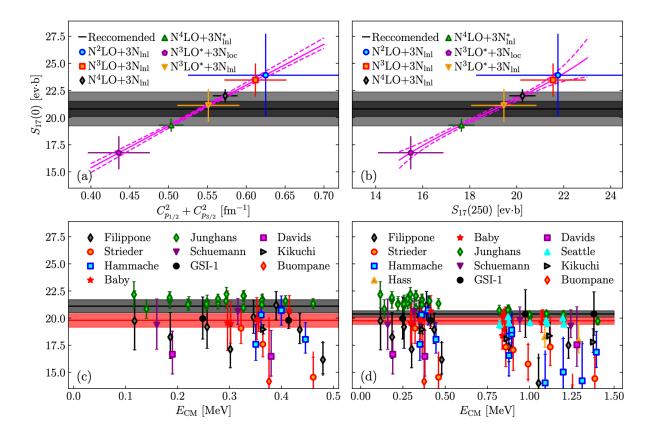
NCSMC S-factor results



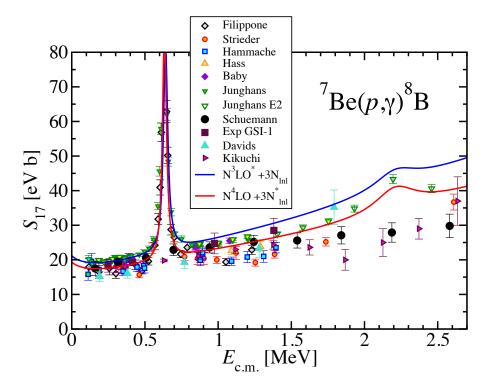
Recommended value $S_{17}(0) \sim 19.8(3) \text{ eV b}$

2011 evaluation in *Rev. Mod. Phys.* **83,**195–245 (2011): $S_{17}(0) = 20.8 \pm 0.7(\text{expt}) \pm 1.4(\text{theory}) \text{ eV b}$

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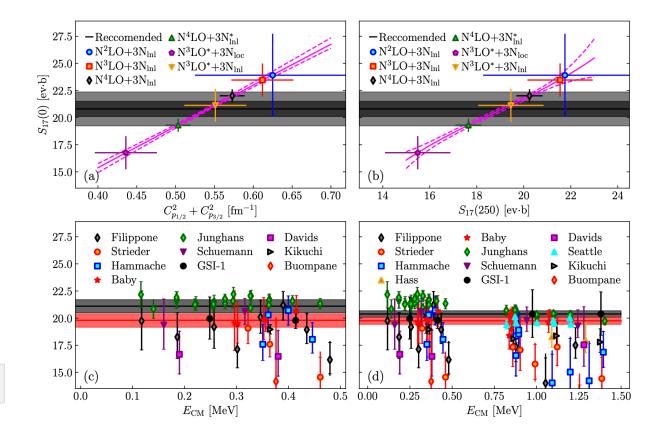
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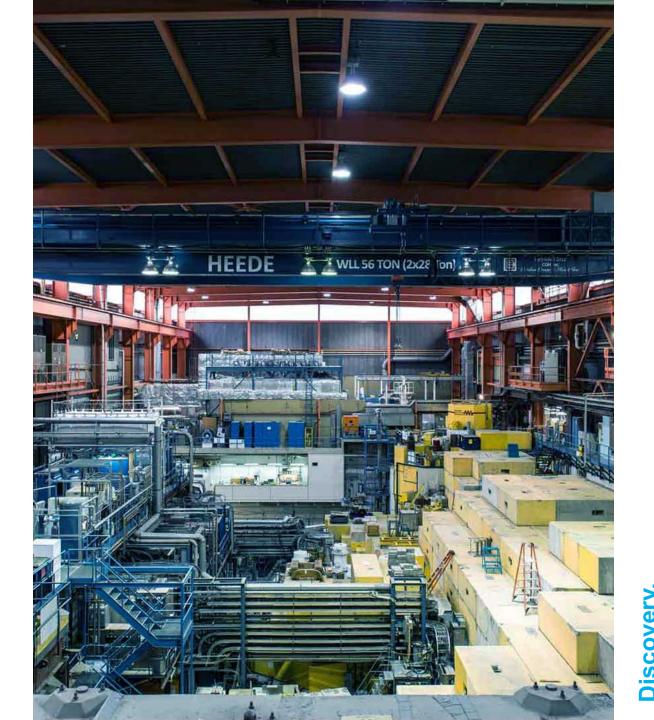
New evaluation in *Rev. Mod. Phys.* **97**, 035002 (2025): $S_{17}(0) = 20.5 \pm 0.7 \text{ eV b}$

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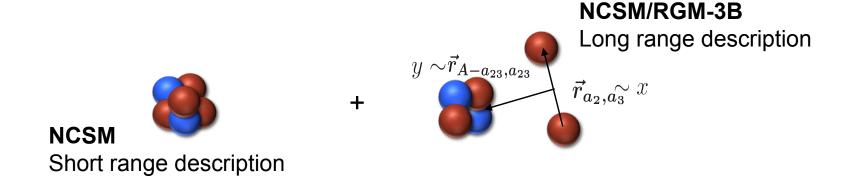


NCSMC for three-body cluster

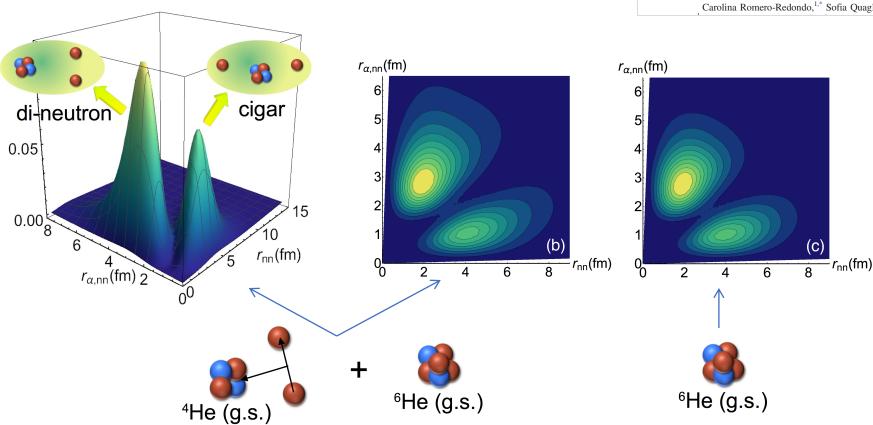
 6 He $\sim {}^{4}$ He + n + n



NCSMC for three-body clusters



$$\Psi^{(A)} = \sum_{\lambda} c_{\lambda} | , \lambda \rangle + \sum_{\nu} \int d\vec{x} \, d\vec{y} \, \psi_{\nu}(\vec{x}, \vec{y}) \, \hat{A}_{\nu} | , \nu \rangle$$
Unknowns



The probability distribution of the ⁶He ground state presents two peaks corresponding to the di-neutron and cigar configurations

Three-cluster dynamics within the *ab initio* no-core shell model with continuum: How many-body correlations and α clustering shape $^6{\rm He}$

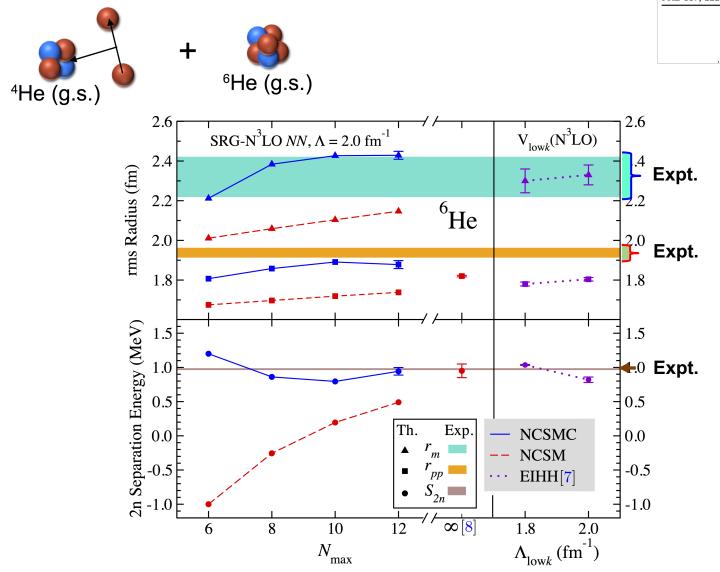
PHYSICAL REVIEW C 97, 034332 (2018)

Sofia Quaglioni, 1,* Carolina Romero-Redondo, 1,† Petr Navrátil, 2,‡ and Guillaume Hupin $^{3,\$}$

PRL 117, 222501 (2016) PHYSICAL REVIEW LETTERS week ending 25 NOVEMBER 2016

How Many-Body Correlations and α Clustering Shape ⁶He

Carolina Romero-Redondo, 1,* Sofia Quaglioni, 1,† Petr Navrátil, 2,‡ and Guillaume Hupin 3,§



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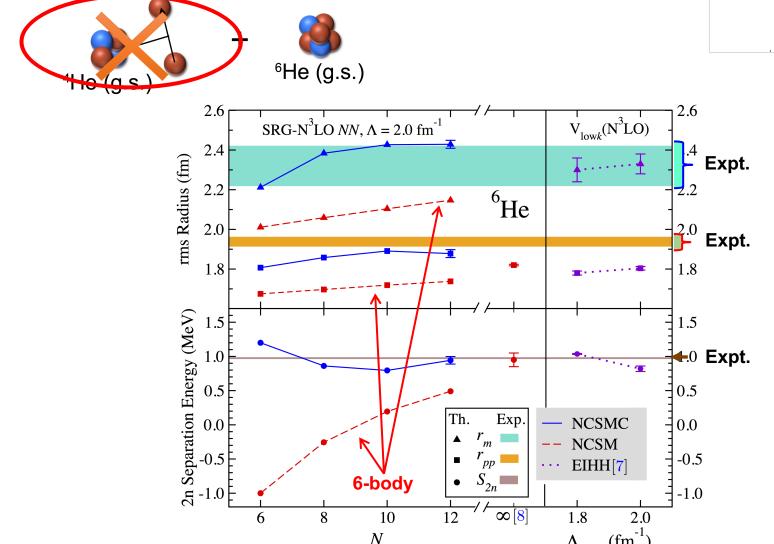
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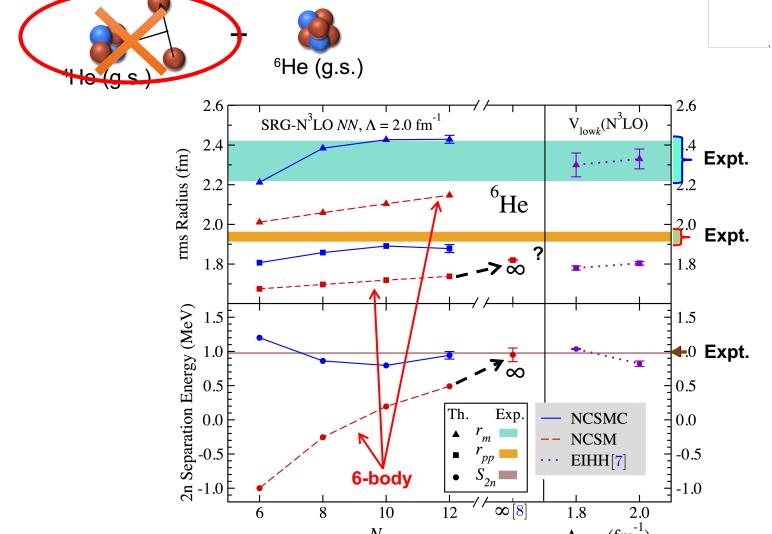
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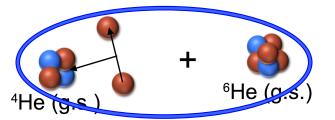
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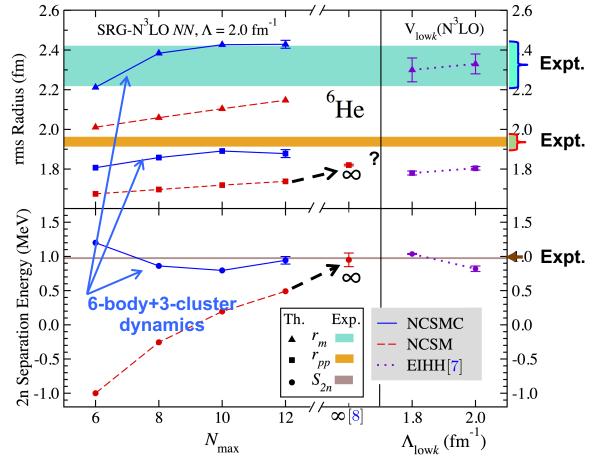
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How Many-Body Correlations and α Clustering Shape ⁶He

Carolina Romero-Redondo, ^{1,*} Sofia Quaglioni, ^{1,†} Petr Navrátil, ^{2,‡} and Guillaume Hupin ^{3,§}





Three-cluster dynamics within the *ab initio* no-core shell model with continuum: How many-body correlations and α clustering shape ⁶He

Sofia Quaglioni, 1,* Carolina Romero-Redondo, 1,† Petr Navrátil, 2,‡ and Guillaume Hupin^{3,§}

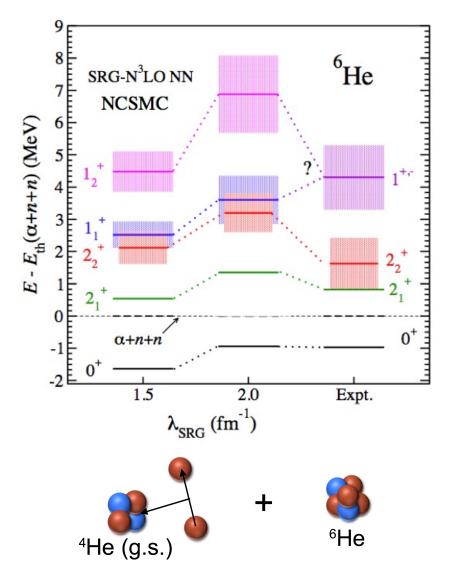
PRL **117**, 222501 (2016)

PHYSICAL REVIEW LETTERS

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PHYSICAL REVIEW C 97, 034332 (2018)

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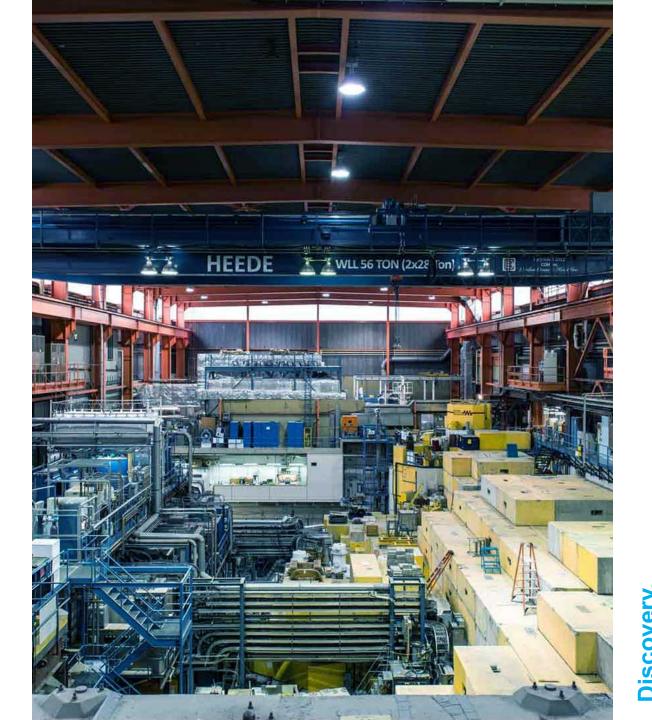
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Quantitative comparison still requires inclusion of 3N forces

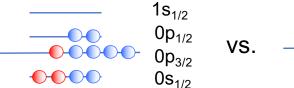
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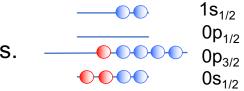
¹¹Li within NCSM

(prerequisite for $^{11}Li \sim ^{9}Li + n + n$)

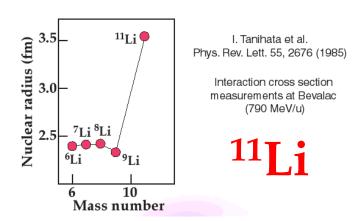


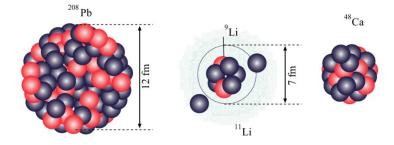
Borromean halo nucleus ¹¹Li

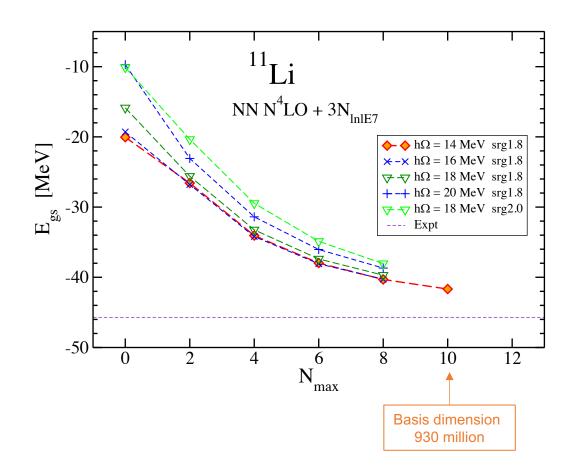


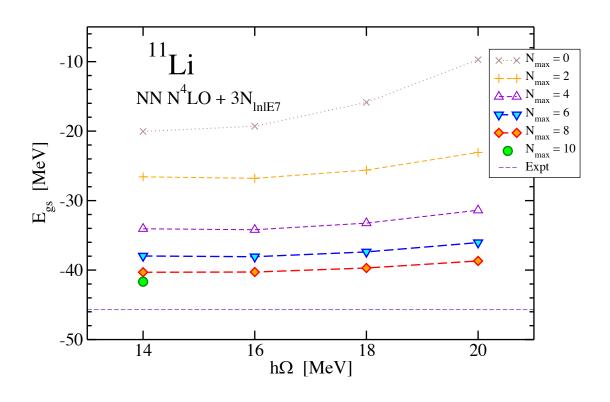


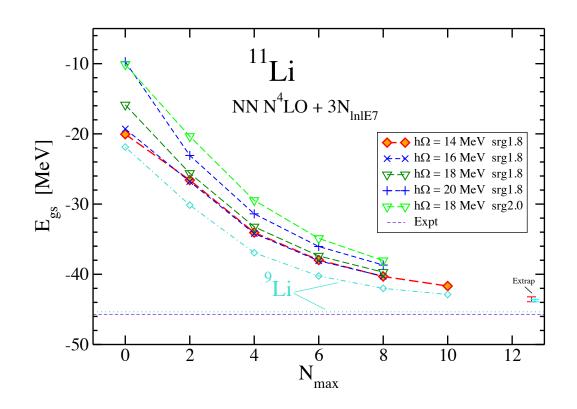
- Z=3, N=8
 - Very weakly bound: E_{th}=-0.3 MeV
 - Halo state dominated by ⁹Li+n+n in the S-wave
 - Configuration mixing, ⁹Li ½- excited state plays a role
- Can we describe ¹¹Li in ab initio calculations?
 - Continuum must be included
 - What role does the 3N interaction play in the configuration mixing?
 - NCSMC needs to be applied very challenging
 - The first step large-scale NCSM

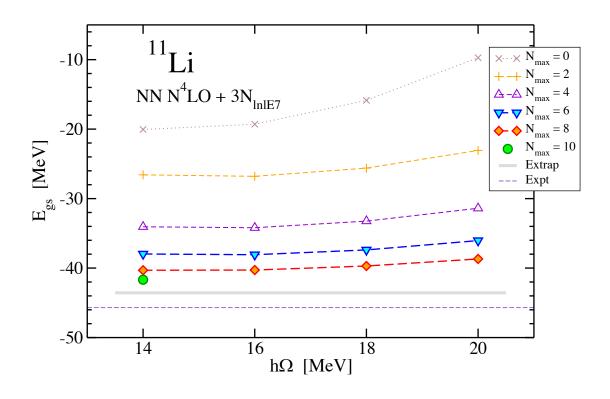


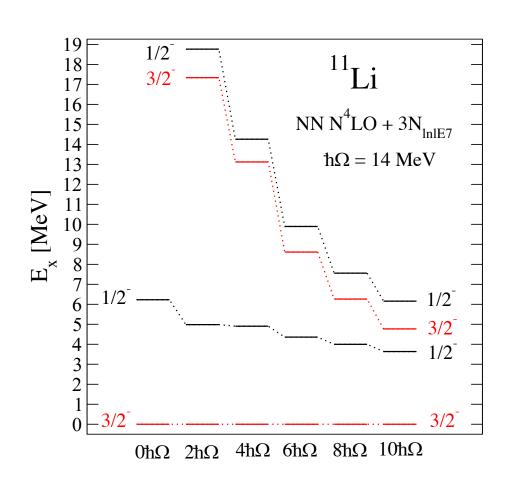


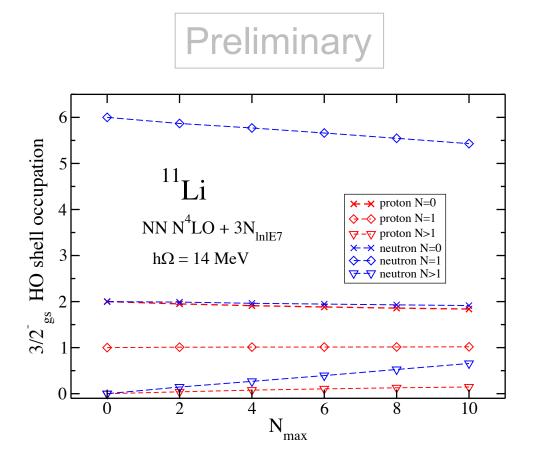


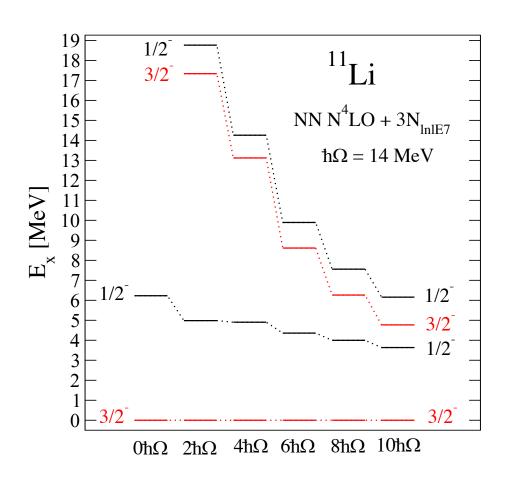


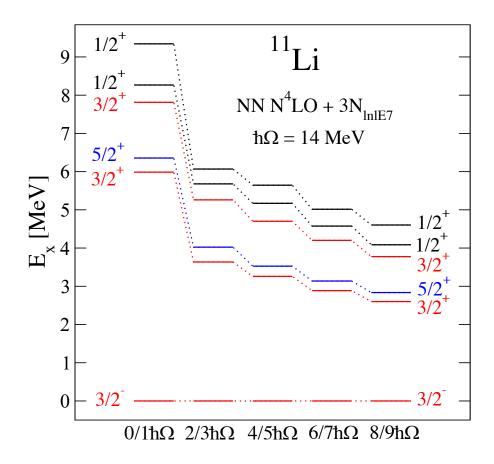


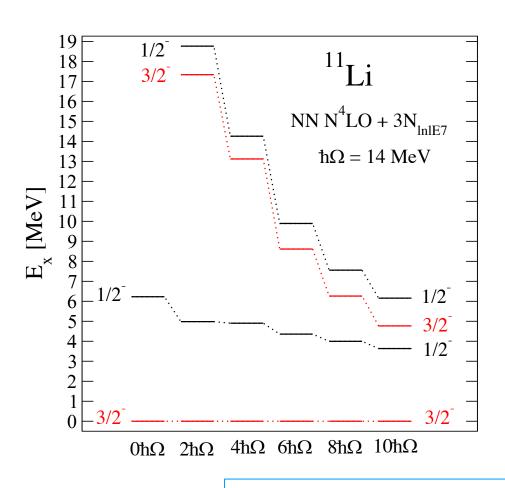


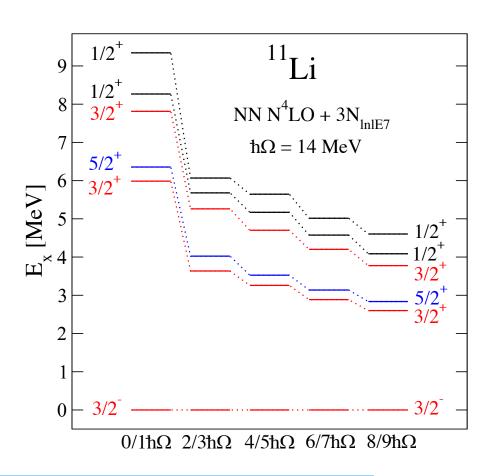












Next step – including continuum via NCSMC – ¹¹Li ~ ⁹Li + n + n

Conclusions

- Ab initio nuclear theory
 - Makes connections between the low-energy QCD and many-nucleon systems
- No-core shell model with continuum capable of describing halo nuclei from first principles
 - Successful reproduction of ¹¹Be parity inversion three-nucleon interaction important
 - Ground-state halo of ⁸B significantly impacts the proton capture on ⁷Be
 - Three-body cluster NCSMC applied to the Borromean halo nucleus ⁶He
- Next frontier *ab initio* NCSMC description of ¹¹Li as a three-cluster ⁹Li + n + n system